

Matlab codes:

1. Finding laplace

`syms t, s`

`laplace (something in way of computer)`

Finding laplace inverse.

`syms (s, t)`

`ilaplace ( " " )`

2. Finding transfer function: $G(s) = \frac{Y(s)}{U(s)}$

`num = [ ]` coefficients of numerator taking into consideration anything

`den = [ ]` equaling 0. coefficients of denominator

`sys = tf (num, den).`

3. Finding zero-pole gain (ZPK): $G(s) = \frac{Y(s)}{U(s)}$

`sys1 = zpk ( [ ], [ ], )`
s = what in numerator s = what in denominator any coefficients outside

or
`s = tf ('s')`

newer matlab.

`G = (something in way of computer)`

4. Finding State-Space models: $G(s) = \frac{Y(s)}{U(s)}$

① $\frac{Y(s)}{U(s)} = \frac{Y}{R} = \frac{X}{R} \times \frac{Y}{X}$

② $R = \text{coef} \cdot \ddot{X} + \text{coef} \cdot \dot{X} + \text{coef} \cdot X$

$Y = \text{coef} \cdot \dot{X} + \text{coef} \cdot X$

$X_1 = X, \quad \boxed{\dot{X}_2 = \dot{X}_1}^*$

$R = \text{coef} \cdot \dot{X}_2 + \text{coef} \cdot X_2 + \text{coef} \cdot X_1$

$\boxed{\dot{X}_2 = -\text{coef} \cdot X_2 + \text{coef} \cdot X_1 + R}^*$

③ $R = \begin{bmatrix} \dot{X}_1 \\ \dot{X}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -\text{coef} & -\text{coef} \end{bmatrix} \times \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} R$

$Y = [\text{coef} \quad \text{coef}] \times \begin{bmatrix} X_1 \\ X_2 \end{bmatrix} + [0] R$

④ $s y s = ss([0 \quad 1]; [-\text{coef} \quad -\text{coef}],$

$[0; 1], [\text{coef} \quad \text{coef}], 0)$

5. finding time response of systems: $G(s)$
(plotting)

impulse ($G(s)$)

step ($G(s)$)

lsim ($G(s)$) (general time response)

conv ($G(s)$) (polynomial multiplication)

deconv ($G(s)$) (polynomial division)

residue ($G(s)$) (partial fraction expansion)

6. finding root locus: $G(s)$

rlocus ($G(s)$)

or

rlocus (tf([$\uparrow$], conv(conv([$\uparrow$], [$\uparrow$]), [$\uparrow$]), [$\uparrow$]))

numerator cef. denominator cef.

7. sisotool.

sisotool ($G(s)$)

remember that:

$$As+B \quad [A \ B]$$

$$As^2+Bs+C \quad [A \ B \ C]$$

$$As^3+Bs^2+Cs+D \quad [A \ B \ C \ D]$$

if anything of those is
missing, its 0

Using numeric way to solve differential equ. in Matlab:

[1] A simple 1st order that has given the parameters:

function $dx = \text{mydiff}(t, x)$

first part.
 $b = 1;$
 $p = 0.5;$] given parameters

$dx = b * x - p * x^2;$ diff. equ.

$tspan = [0, 1]$ time span (from 0 - 1 hour)

$x_0 = 100;$ starting value.

$[t, y] = \text{ode45}(@\text{mydiff}, tspan, x_0);$

$\text{plot}(t, y)$

* tip: always have x initial value before you begin.

* note: we also have ode23

[2] 1st order that has unknown parameters.

Function $dx = \text{mydiff}(t, x, \text{param})$
added to define a and b

$a = \text{param}(1)$; unknown

$b = \text{param}(2)$; unknown

$dx = a * x + b$;

$tspan = [0 \ 5]$;

$x_0 = 1$;

$a = -\frac{1}{5}$; given as $-\frac{1}{5}$

$b = 1$; to make it easy to change

$\text{param}[a, b]$; التكرار في المتغير

$[t, y] = \text{ode45}(@\text{mydiff}, tspan, x_0, [], \text{param})$

$\text{plot}(t, y)$

no idea why this is here.

[3] Not so simple second order (given parameters)

1. begin by making $\ddot{x}$ independent

2. we can't have $\ddot{x}$, so $\underline{x_2 = \dot{x}}$, $x_1 = x$

after putting those in original it is ②

3. function $dx = \text{mydiff}(t, x)$

$[m, n] = \text{size}(x);$] I have no idea why we put these.
 $dx = \text{zeros}(m, n)$

$dx(1) = x(2);$ ①

$dx(2) = (2 - 2 * t * x(2) - 3 * x(1)) / (1 + t * x(2));$ ②

$tspan [0 \ 5];$

$x_0 = [0; 1];$

$[t, x] = \text{ode23}(@\text{mydiff}, tspan, x_0);$

$\text{plot}(t, x)$

$\text{legend}('x_1', 'x_2')$

$tspan [0, 5];$

$x_0 = [0; 1];$

$\text{plot}(t, x(:, 2))$

$[t, x] = \text{ode23}(@\text{mydiff}, tspan, x_0);$

Symbolic way to solve differential equations:

$$① \frac{dy}{dt} = ay.$$

syms y(t) a $\rightarrow$ a variable
equation
eqn = diff(y, t) == a * y;
S = dsolve(eqn) $\rightarrow \frac{dy}{dt}$
solution diff.

$$② \frac{dy}{dt} = z \quad \frac{dz}{dt} = -y \quad (\text{system})$$

syms y(t) z(t)
eqns = [diff(y, t) == z, diff(z, t) == -y];

S = dsolve(eqns) $\Rightarrow$ without assignment

or
[ysol(t), zsol(t)] = dsolve(eqns) $\Rightarrow$ with assignment

$$(3) \frac{dy}{dx} = \frac{1}{x^2} e^{-\frac{1}{x}}$$

syms y(x)

$$\text{eqn} = \text{diff}(y) == \exp(-1/x) / x^2;$$

$$y_{\text{sol}}(x) = \text{dsolve}(\text{eqn}) \Rightarrow \text{without specifying initial condition}$$

or

$$\text{cond} = y(0) == 1; \Rightarrow \text{specifying initial condition to eliminate constants from solutions.}$$

$$s = \text{dsolve}(\text{eqn}, \text{cond})$$

$$(4) \frac{d^2 y}{dx^2} = a^2 y, \quad y(0) = b, \quad y'(0) = 1$$

syms y(t) a b

second order

$$\text{eqn} = \text{diff}(y, t, 2) == a^2 * y;$$

$$Dy = \text{diff}(y, t); \text{ assigning diff}(y, t) \text{ to } Dy$$

$$\text{cond} = [y(0) == b, Dy(0) == 1];$$

conditions

$$y_{\text{sol}}(t) = \text{dsolve}(\text{eqn}, \text{cond}).$$