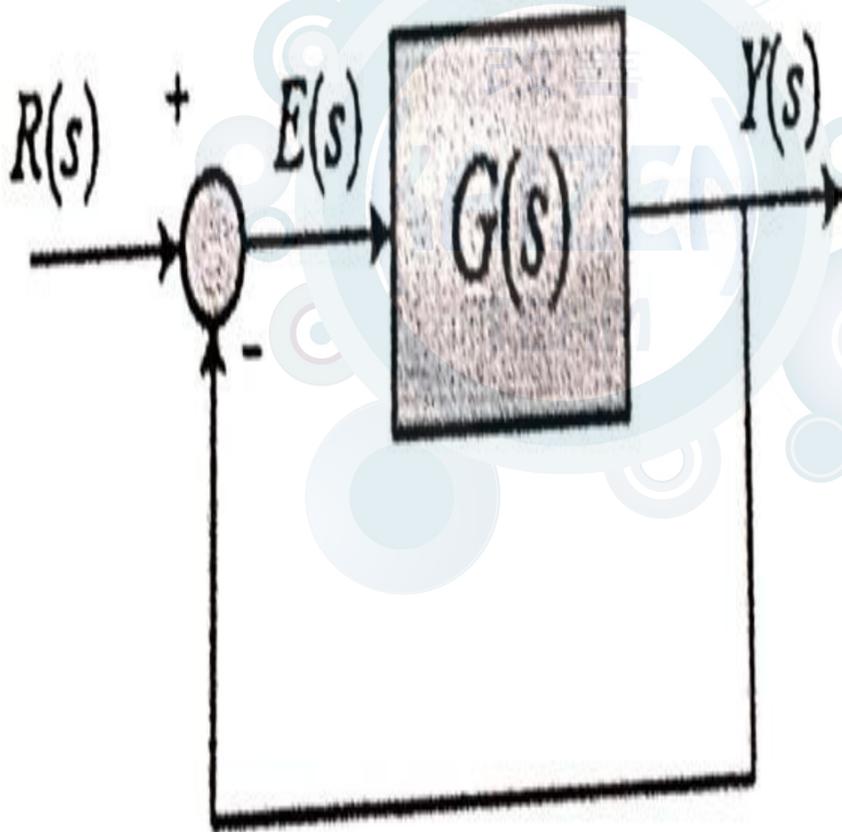
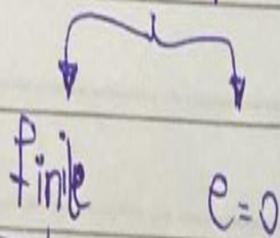


Q1) find the K value to achieve a steady state error of < 0.1 for a unit step input

$$G(s) = \frac{K(s+1)}{(s+5)(s+7)}$$



④ step input $e < 0.1$



when $N=0$

when $N \geq 1$

$$K_p = \lim_{s \rightarrow 0} K(s+1)$$

$$\lim_{s \rightarrow 0} \frac{K}{s} (s+1) = \infty$$

$$s \rightarrow 0 \frac{(s+5)(s+7)}{35}$$

$$s \rightarrow 0 \frac{K}{s} \frac{(s+5)(s+7)}{(s+5)(s+7)}$$

$$= \frac{K}{35}$$

$$e = \frac{1}{1+K_p} = 0$$

$$\frac{1}{1+K} < 0.1$$

$$\frac{1}{35}$$

改善

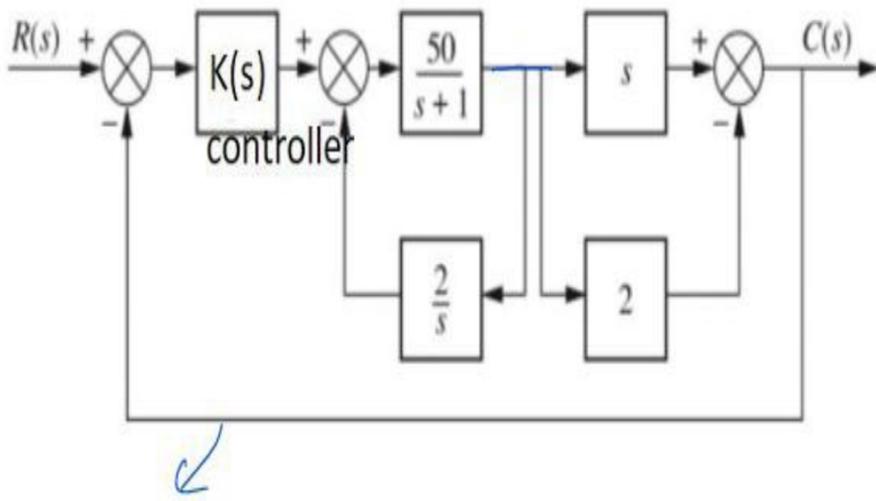
K if $K > 315$

$$\frac{K}{s} > K$$

$$\frac{1+K}{35} > 10$$

$$\frac{K}{35} > 9$$

$$K > 315$$



$$\frac{\frac{50}{s+1}}{1 + \frac{2}{s} \cdot \frac{50}{s+1}}$$

$$e_{ss} < 2$$

$$\frac{1}{K_v} < 2$$

$$\frac{K(s) \cdot 50 \cdot s}{(s+1) + 100} \quad v \quad s=2$$

$$K_v = \lim_{s \rightarrow 0} s \frac{K(s) \cdot 50s \cdot (s-2)}{s^2(s+1) + 100} = \frac{K(s) \cdot 50(-2)}{101}$$

$$\frac{0.99}{s^2} < K(s)$$

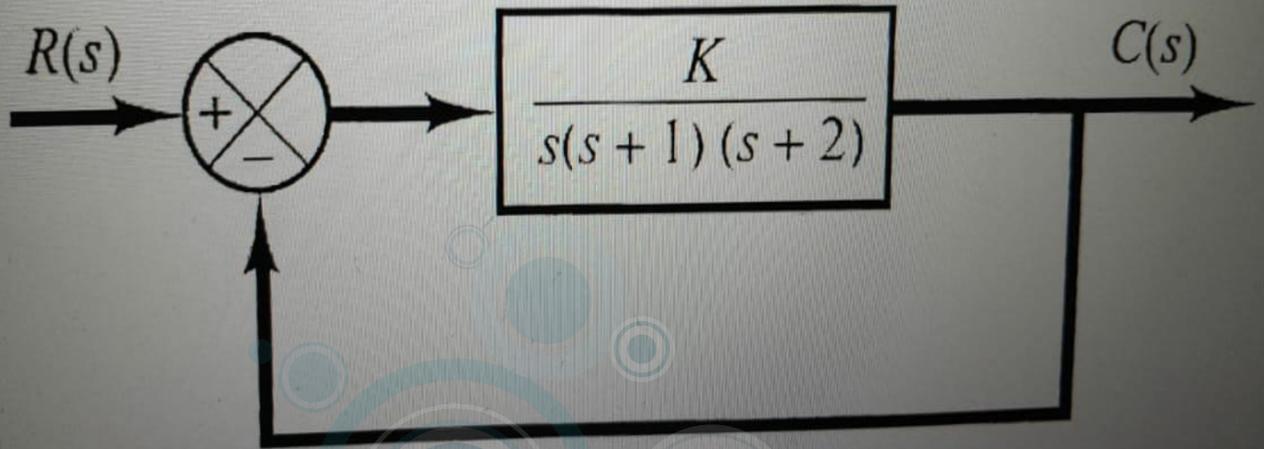
$$\frac{1}{K(s) - 0.99} < 2$$

Quiz 4 Industrial control systems Prof. M. Barghash IE dept SoC UoJ 13/11/2024

Name _____

ID: _____

For following system what is the steady state error for $R = 3u(t) + 5t$



$$\frac{3}{1 + K_p} + \frac{5}{K_v} = \frac{3}{\infty} + \frac{5}{\frac{K}{2}} = 0 + \frac{10}{K}$$

$$K_p = \lim_{s \rightarrow 0} \frac{K}{s(s+1)(s+2)} = \frac{K}{0} = \infty$$

$$K_v = \lim_{s \rightarrow 0} s \left(\frac{K}{s(s+1)(s+2)} \right) = \frac{K}{2}$$

ID:

rise time for the following system

$$G(s) = \frac{7}{s^2 + 14s + 40}$$

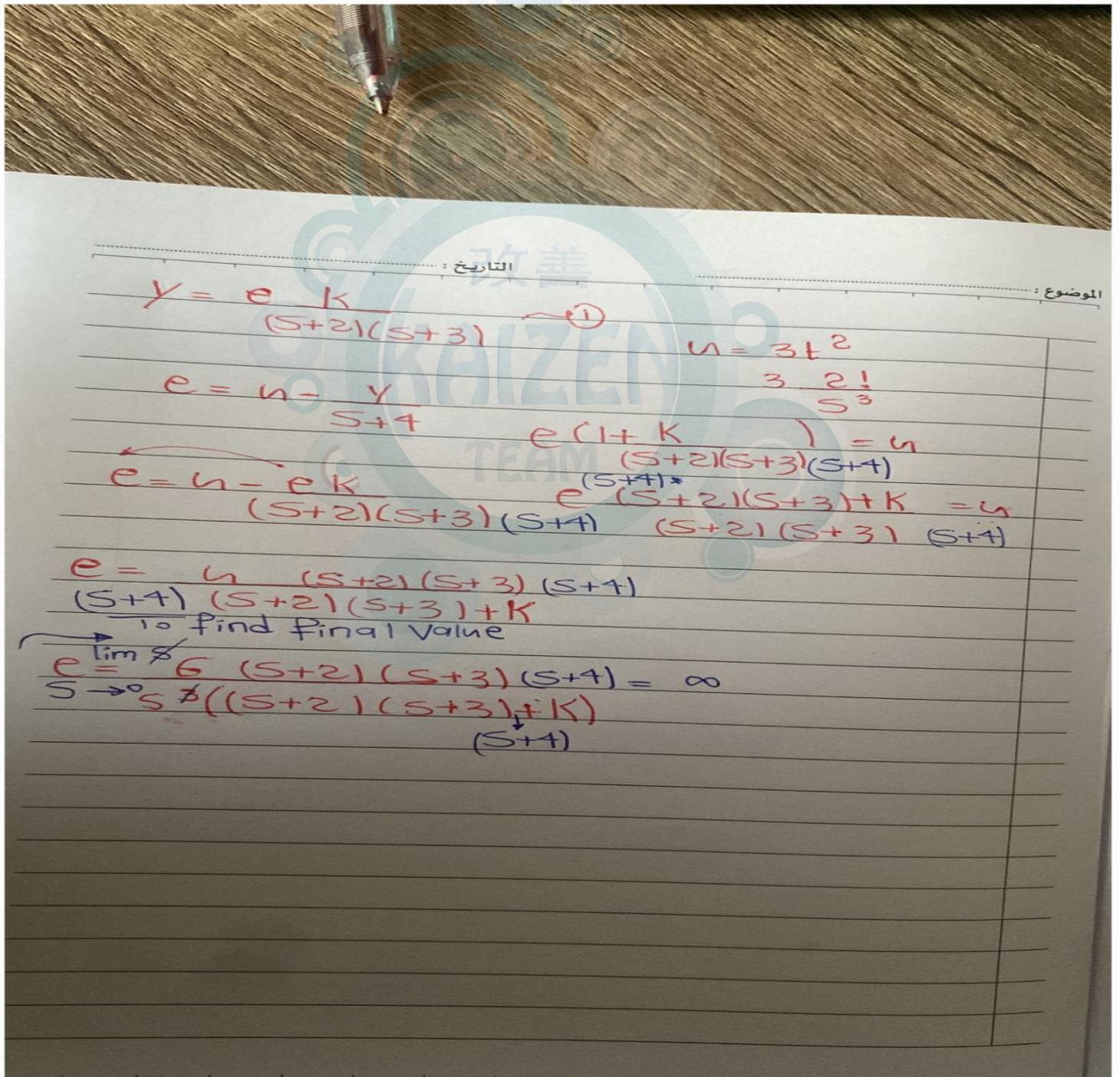
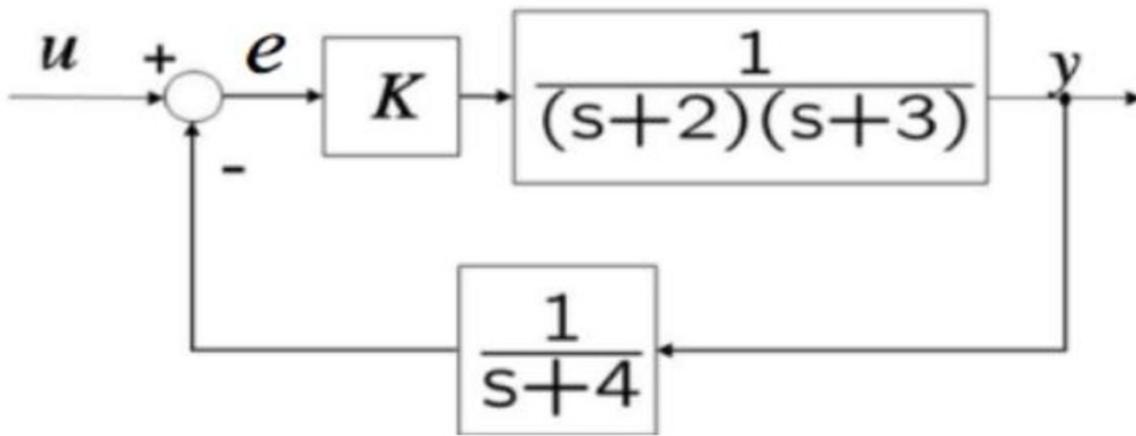
$$(s+4)(s+10)$$

$$T_r = 2.2 \tau = 0.55$$

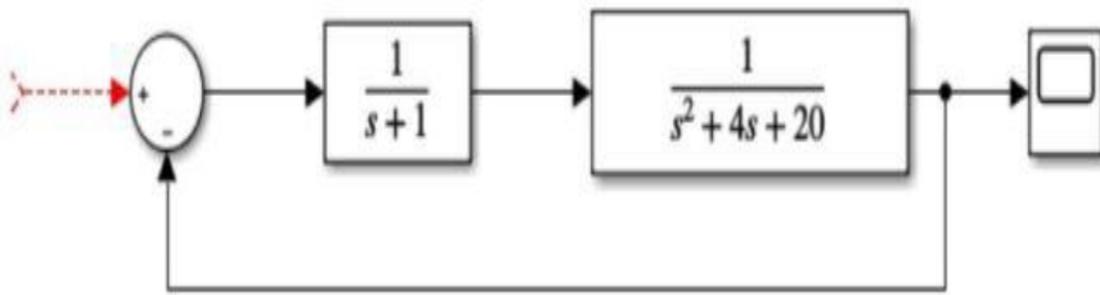
$$\tau = \frac{1}{a} = \frac{1}{4}$$

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Q2) calculate the steady state error if $u(t) = 3t^2$



Q2 a) (2.5 points) Find the steady state error to a step input the following



Solution

$$K_p = \lim_{s \rightarrow 0} \frac{1}{s+1} \frac{1}{s^2+4s+20} = \frac{1}{20}$$

$$e = \frac{1}{1+K_p} = \frac{1}{1+\frac{1}{20}} = \frac{20}{21}$$

Controller =

Ess =

b) (2.5 points) For the a part design add a controller to achieve steady state error = 1; when the input is $1/s^2$.

Solution:

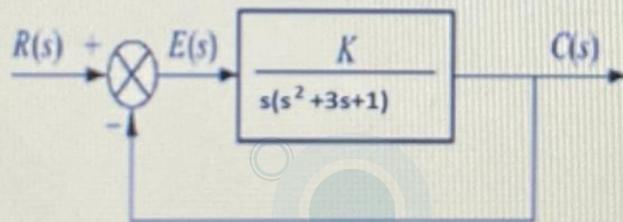
ramp
input
finite
when
 $N=1$

$$K_v = \lim_{s \rightarrow 0} s \frac{1}{s+1} \frac{1}{s^2+4s+20} \frac{k}{s} = \frac{k}{20}$$

$$e = \frac{1}{K_v} = 1 = \frac{1}{k/20} \quad k = 20$$

Controller = $\frac{20}{s}$

Q5) find the steady state error for $R = 2 + 3t$ (5 points)



► Subject :

$$R = 2 + 3t$$

ramp

$$k_v = \lim_{s \rightarrow 0} s \cdot \frac{k}{s(s^2 + 3s + 1)}$$

$$= \frac{k}{1} = k$$

step

k

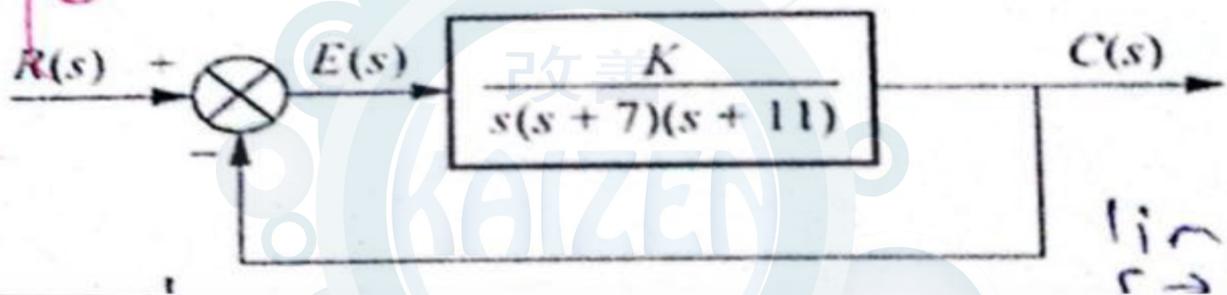
$$k_p = \lim_{s \rightarrow 0} s(s^2 + 3s + 1) = \infty$$

$$e = \frac{3}{k} = \frac{3}{k}$$

$$e = \frac{1 \times 2}{1 + k_p} = 0$$

$$\text{error} = \frac{3}{k}$$

Q4) Find the steady state error for a step input (5 points)



Step

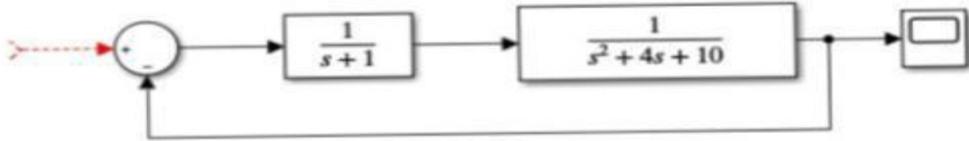
$$|K_p = \lim_{s \rightarrow 0} \frac{1}{s(s+7)(s+11)} = \infty$$

$$e = \frac{1}{1+|K_p|} = \frac{1}{1+\infty} = 0$$

OR we can simply say

$N=1 \rightarrow$ zero error for step

Q2 a) (5 points) Find the steady state error to a step input the following



Solution

step input

$$K_p = \lim_{s \rightarrow 0} \frac{1}{s+1} \frac{1}{s^2+4s+10}$$

$$= \frac{1}{10}$$

$$e = \frac{1}{1 + \frac{1}{10}} = \frac{10}{11} \approx 0.91$$



The steady state error for input $= 5u(t)$ is

Step input

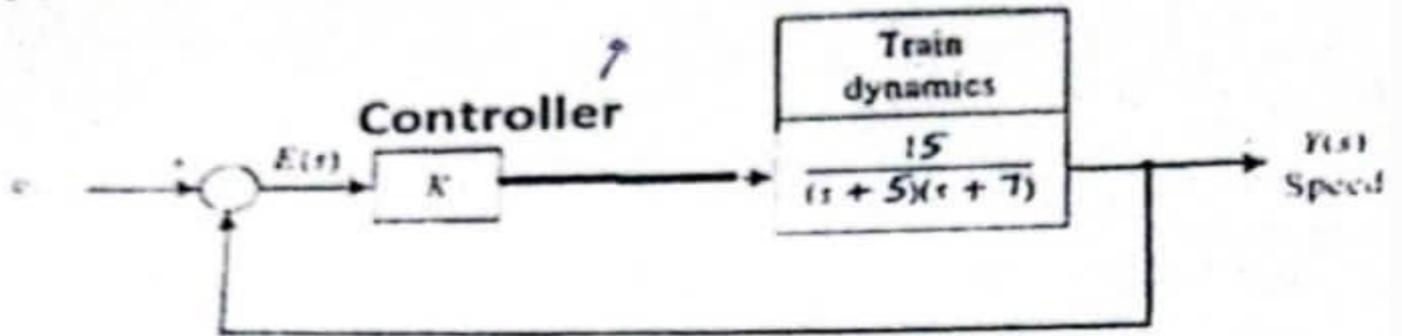
$$|K_p = \lim_{s \rightarrow 0} 100 \cdot \frac{10}{s(s+5)}$$

$$s \rightarrow 0 \quad \frac{1000}{s(s+5)}$$

$$= \infty$$

or we can say $N=0$, step
 so $e=0$

Q3) For the following system



a) Find the steady state error to a step input (3.5)

step input $\left[\frac{15K}{s} \right] - \left[\frac{3}{2} K \right]$

$$1_{KP} = \lim_{s \rightarrow 0} \frac{15K}{s(s+5)(s+7)}$$

$$= \frac{15K}{3 \cdot 7}$$

$$\frac{1}{1 + \frac{15K}{7}} = \frac{7}{7 + 15K}$$

$$G(s) = \frac{(s+z_1)(s+z_2)}{s^n(s+p_1)(s+p_2)}$$

if G is the open loop function and unity feedback is used

if $n=1$; and input $A=1/s$ input $B=1/s^2$ input $C=1/s^3$

then for which functions the steady state is finite (constant) not equal to zero

$N=1$

finite

for

$\frac{1}{s^2}$

So input B

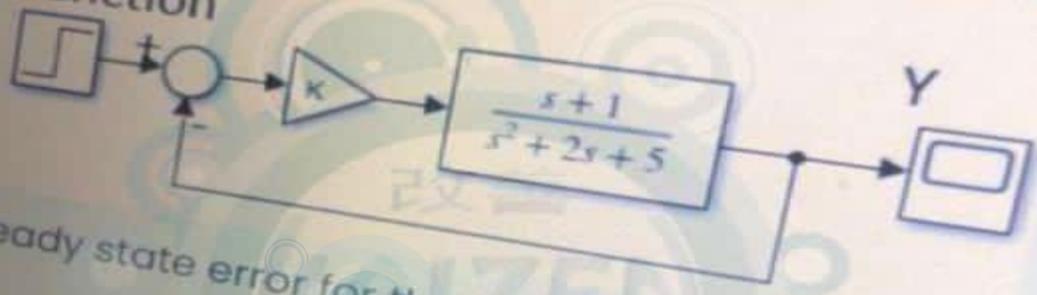
改善

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8

Input R(t)
step function



the steady state error for the above system is

a. $5/(5+K)$

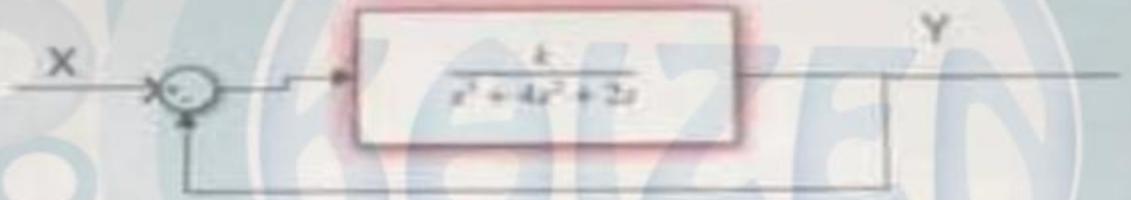
Step input

$$|K_p = \lim_{s \rightarrow 0} \frac{K(s+1)}{s^2+2s+5}$$

$$= \frac{K}{5}$$

$$e = \frac{1 + \frac{K}{5}}{5 + K}$$

$$= \frac{5 + K}{5 + K}$$



the steady state error to a ramp ($1/s^2$) input is

Ramp

$$|k_v = \lim_{s \rightarrow 0} s |k$$

$$s \rightarrow 0 \quad \frac{K}{s(s^2 + 4s + 2)}$$

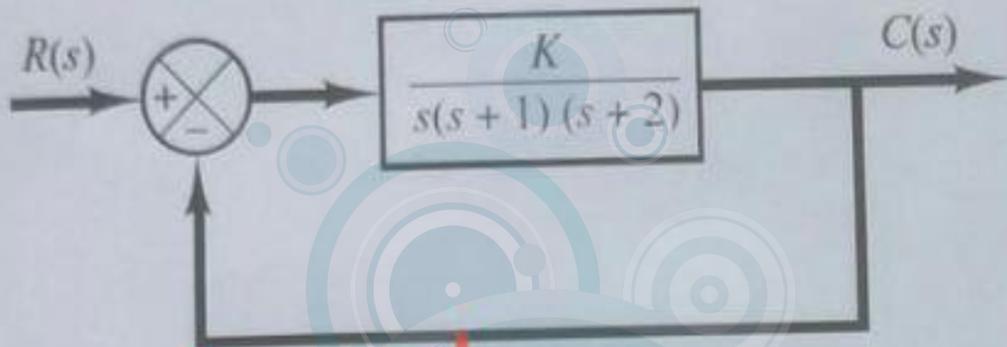
$$= \frac{K}{2}$$

$$e = \frac{1}{K/2} = \frac{2}{K}$$

Name _____

ID: _____

For following system what is the steady state error for $R=3u(t)+5t$



$3u(t) + 5t$
 ~~~~~  
 Step ramp

$$|K_p = \lim_{s \rightarrow 0} \frac{K}{s(s+1)(s+2)} = \infty$$

$$|K_v = \lim_{s \rightarrow 0} \frac{s}{K}$$

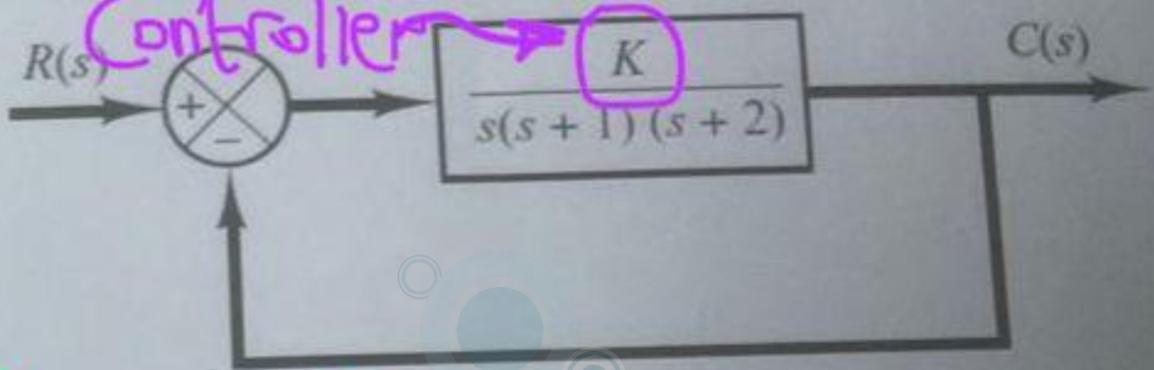
$$= \frac{K}{s+1}(s+2) \Big|_{s=0} = \frac{K}{2}$$

$$E = \frac{3}{1+\infty} + \frac{5}{K/2} = \boxed{\frac{10}{K}}$$

Name \_\_\_\_\_

ID: \_\_\_\_\_

For following system design k to achieve 0.1 steady state error for a ramp input



Ramp  
input  
finite  
when  
 $N=1$   
which is  
our case  
so the  
controller  
is  $k$

$$k_v = \lim_{s \rightarrow 0} s k$$

$$s(s+1)(s+2)$$

$$= \frac{k}{2}$$

$$\frac{k}{2} = 10$$

$$k/2 = 10$$

$$k = 20$$

- ① shear force (v)
- ② bending

Quiz 4 Industrial control systems Prof. M. Barghash IE dept Soc UoJ 13/11/2024

Name \_\_\_\_\_ ID: \_\_\_\_\_

For following system add a controller to achieve 0.1 steady state error for a step input



Step input -  
 Finite when  $\mu=0$   
 $K_p = \lim_{s \rightarrow 0} s \frac{1}{(s+1)(s+2)}$

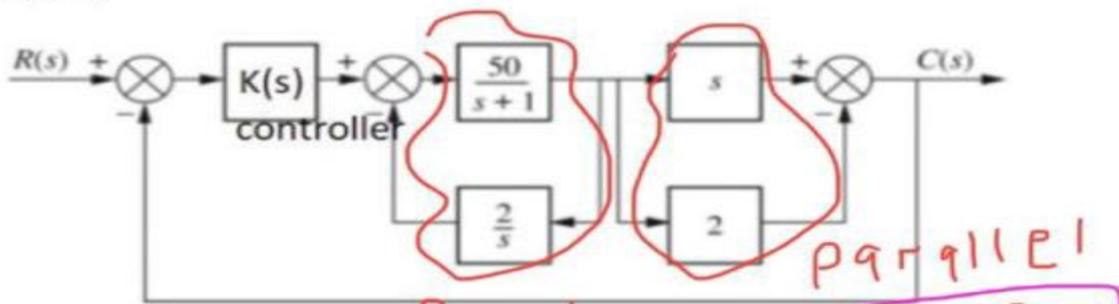
Handwritten calculations for steady state error:

$$1 + \frac{K}{2} = 0.1$$

$$1 + \frac{K}{2} = 10$$

$$K = 18$$

Q2) for the following system design the steady state error for a step input to be zero and for a ramp input to be less than 2 (design the controller)? (note  $K(s)$  is any function of  $s$  to be suitably designed) (10 points)



parallel  
feedback

$$\frac{50}{s+1}$$

$$1 + \frac{50}{s+1} \frac{2}{s}$$

$$= \frac{50s}{s^2 + s + 100}$$

series

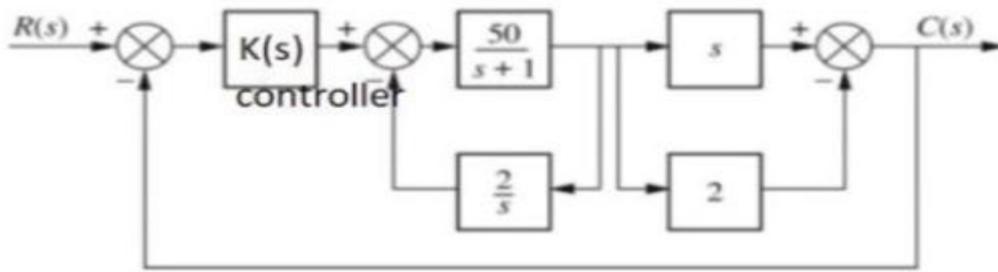
$$G(s) = \frac{50s(s-2)}{s^2 + s + 100}$$

9) a step to be zero when  $N \geq 1$

So  $|K(s)| = \frac{|k|}{s^2}$  as there is an 's' in the Numerator

(1)

Q2) for the following system design the steady state error for a step input to be zero and for a ramp input to be less than 2 (design the controller)? (note  $K(s)$  is any function of  $s$  to be suitably designed) (10 points)



$$G(s) = \frac{50s(s-2)}{s^2 + s + 100}$$

For a ramp to be less than  $\boxed{2}$

Case 1

$$e = 0$$

when  $N \geq 2$

$$\text{So } K(s) = \frac{k}{s^3}$$

$$k \neq 0$$

as there is an 's' in the

Numerator

$$(2) \quad \boxed{k \leq \frac{1}{2}} \quad ?$$

Case 2

$e$  finite

and  $\leq 2$

when  $N = 1$

$$k_v =$$

$$\lim_{s \rightarrow 0} \frac{50s(s-2)}{s^2 + s + 100}$$

$$= -1k$$

$$\frac{1}{-k} \leq 2$$

$$-k \geq \frac{1}{2}$$

Controller

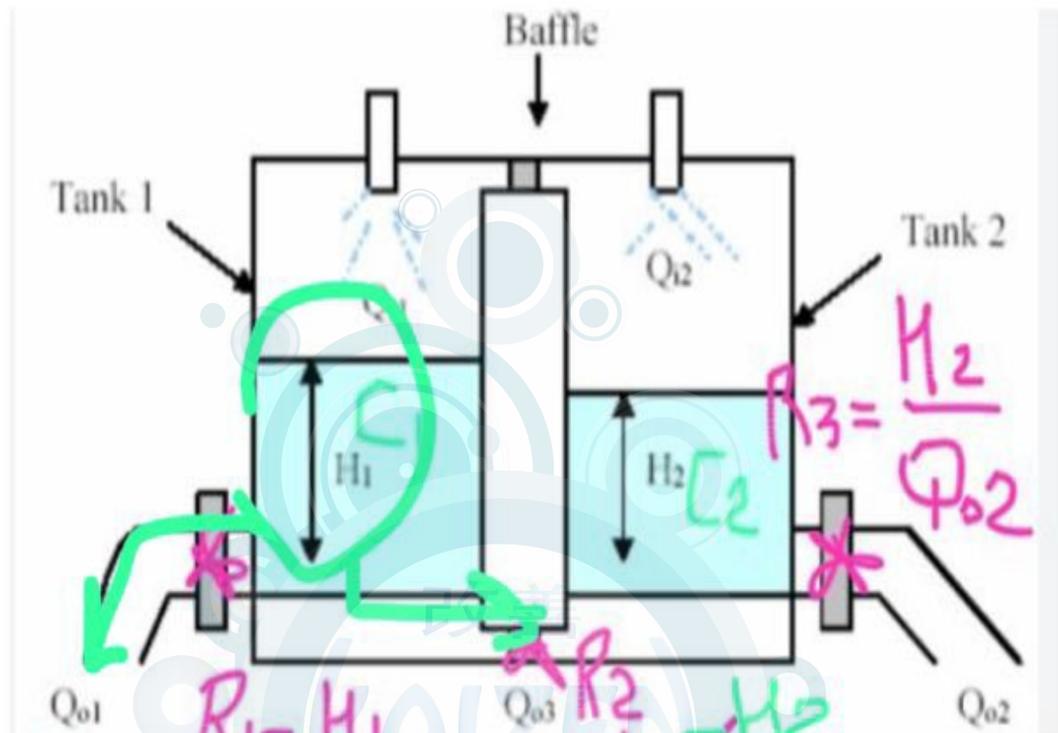
$$\frac{k}{s^2}$$

Name \_\_\_\_\_

ID \_\_\_\_\_

Answer the following question

Q1) write the differential equations describing the level system



TANK 1

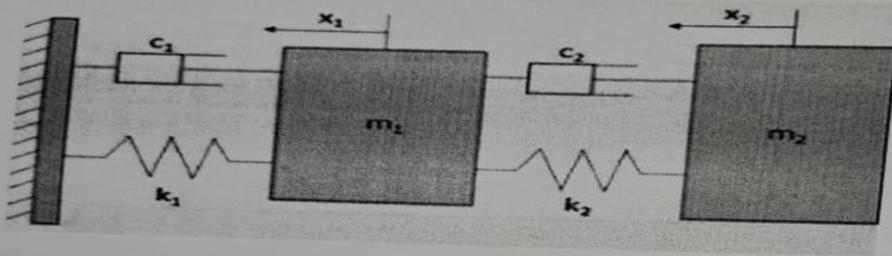
$$R_1 = \frac{H_1}{Q_{01}} = \frac{H_1}{Q_{03}}$$

$$Q_{i1} - Q_{o1} - Q_{o3} = C_1 \frac{dh_1}{dt}$$

TANK 2

$$Q_{i2} + Q_{o3} - Q_{o2} = C_2 \frac{dh_2}{dt}$$

Write the equations describing the model



$$\frac{1}{c_1 s} + k_1 + \frac{1}{c_2 s} + k_2$$

$$x_1 = \frac{1}{\sqrt{k_1^2 + c_1^2}} \frac{c_1 s + m_1}{k_1}$$

$$x_2 = \frac{k_2}{c_2 s + m_2}$$

Node 1

$$0 = m_1 \ddot{x}_1 + c_1 \dot{x}_1 + k_1 x_1 + c_2 (\dot{x}_1 - \dot{x}_2) + k_2 (x_1 - x_2)$$

Node 2

$$0 = m_2 \ddot{x}_2 + c_2 (\dot{x}_2 - \dot{x}_1) + k_2 (x_2 - x_1)$$

$$0 = m_1 \ddot{x}_1 + k_1 (x_1 - x_2)$$

Second Cart (TMD)

$$0 = m_2 \ddot{x}_2 + k_1 (x_2 - x_1) + b \dot{x}_2 + k_2 x_2$$

Tank ①

$$q_1 - q_2 = C_1 d h_1 / dt$$

$$R_1 = \frac{H_1 - H_2}{Q_2}$$

Tank ②

$$q_2 - q_s = C_2 d h_2 / dt$$

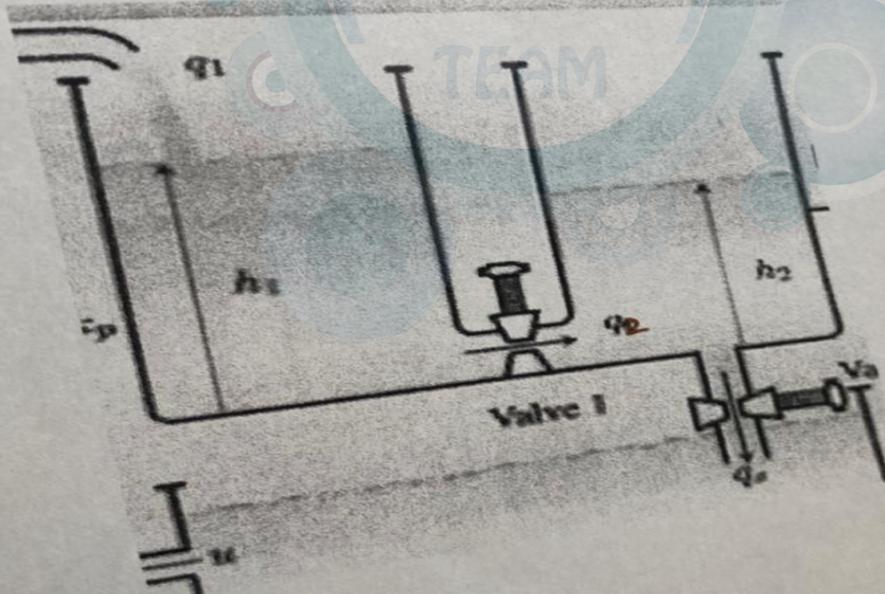
$$R_2 = \frac{H_2}{Q_s}$$

Quiz Industrial control 改善 Prof. M. Barghash IE SoC UoJ 6/1/2025

Name: \_\_\_\_\_

ID: \_\_\_\_\_

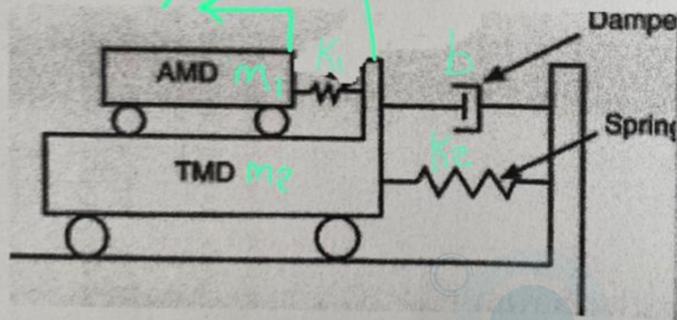
Q) Write the equations describing the following system add needed symbols.



Name:

ID:

Write the diff equations ?



first Cart (AMD)

$$0 = m_1 \ddot{x}_1 + K_1 (x_1 - x_2)$$

Second Cart (TMD)

$$0 = m_2 \ddot{x}_2 + K_1 (x_2 - x_1) + b \dot{x}_2 + K_2 x_2$$

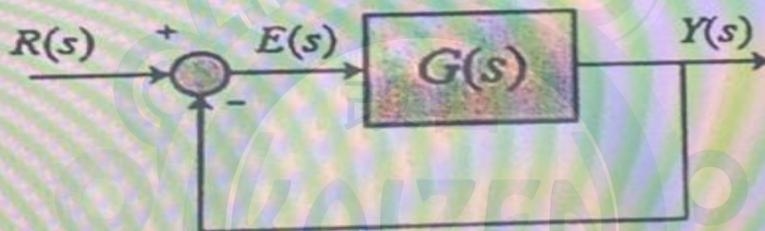
Quiz industrial control systems IE dept SoC UoJ Prof. M. Barghash 21/11/2024

Name \_\_\_\_\_

ID \_\_\_\_\_

Q1) find the steady state error for  $R = (4+3t)u(t)$

$$G(s) = \frac{K(s+1)}{s(s+5)(s+7)}$$



$$\lim_{s \rightarrow \infty} \frac{K(s+1)}{s(s+5)(s+7)} = 0$$

$$\frac{4}{1+\infty} = 0$$

$$\lim_{s \rightarrow 0} \frac{K(s+1)}{s(s+5)(s+7)}$$

$$= \frac{K \times 1}{35}$$

$$\frac{1 \times 1}{\frac{K}{35}} = \frac{35}{3K}$$

$$\frac{35}{3K}$$

Highlighter

التاريخ :

الموضوع :

$$\begin{array}{l} \text{Step} \\ K_p = \lim_{S \rightarrow 0} K(S+1) = \infty \\ S(S+5)(S+7) \end{array} \quad \begin{array}{l} \text{ramp} \\ K_v = \lim_{S \rightarrow 0} \frac{K(S+1)}{S(S+5)(S+7)} \\ = \frac{K}{35} \end{array}$$

$$e = \frac{4}{1+\infty} + \frac{3}{\frac{K}{35}}$$

$$= 0 + \frac{105}{K} = \boxed{\frac{105}{K}}$$

Step Finite when  $N=0$

$K \rightarrow$  Controller

$$K_p = \lim_{S \rightarrow 0} \frac{K(S+1)}{(S+5)(S+7)} = \frac{K}{35}$$

$$e = \frac{1}{1+K} < 0.1$$

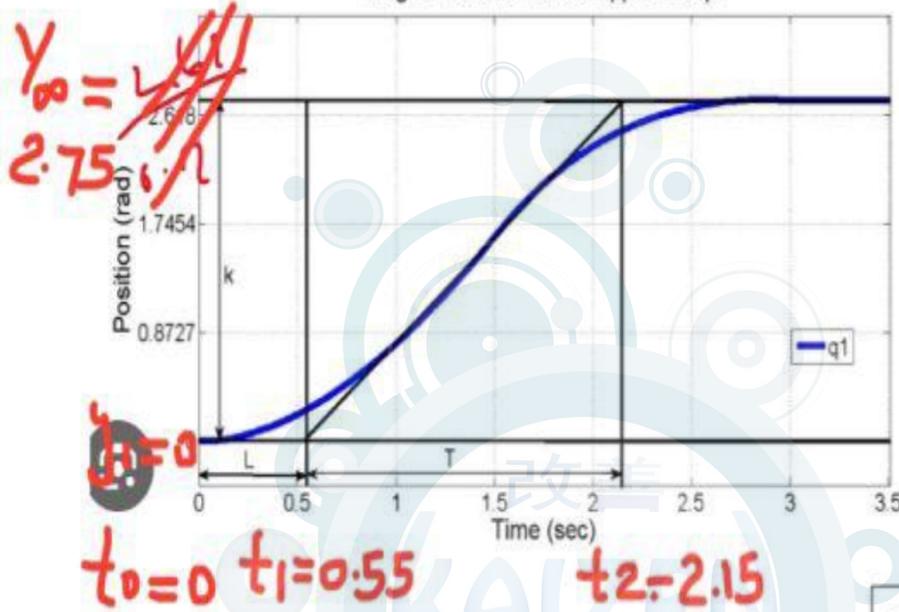
$$\frac{1}{1+K} > 10$$

$$\boxed{K > 315}$$

Name \_\_\_\_\_

ID \_\_\_\_\_

Ziegler-Nichols method applied to q1



$$K_0 = \frac{2.75 - 0}{0.3 - 0.1}$$

$$= 13.75$$

$$\text{rad/KW}$$

$$T_0 = 0.55 \text{ s}$$

$$V_0 = 1.6 \text{ s}$$

The response when we changes the input from 0.1 to 0.3 KW the output changed according to the figure

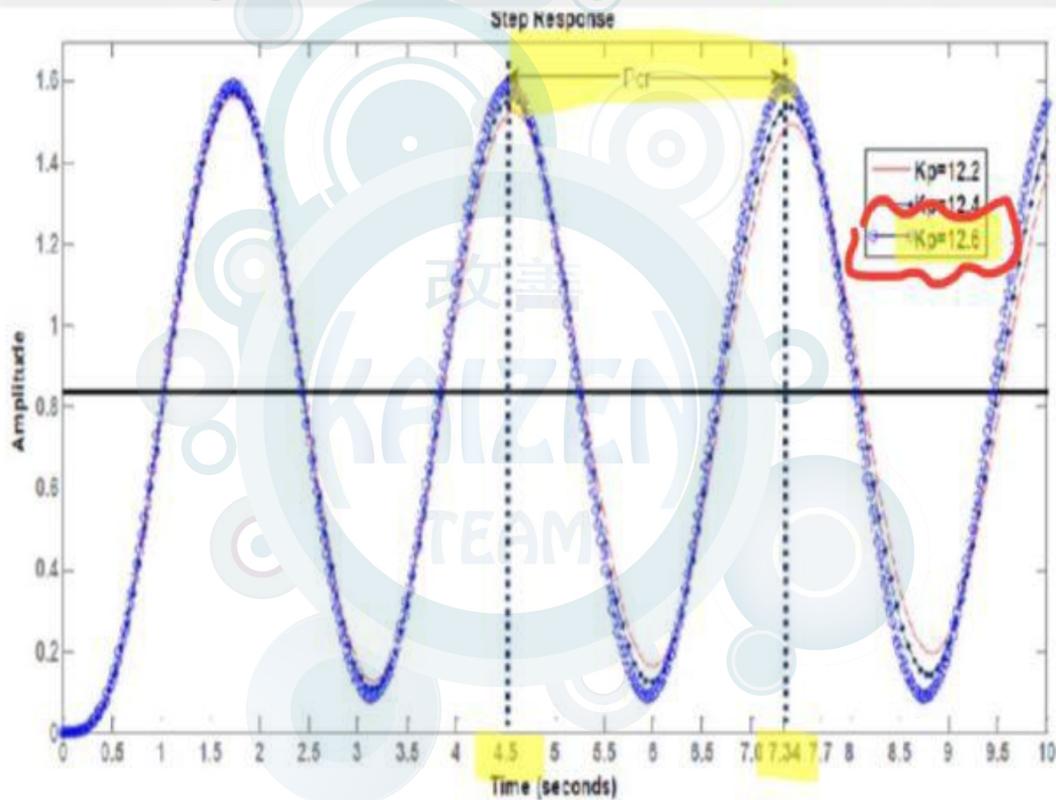
|     | $K_p$                                     | $T_r$           | $T_d$              |
|-----|-------------------------------------------|-----------------|--------------------|
| P   | $\frac{V_0}{K_0 T_0}$<br><del>0.212</del> | —               | —                  |
| PI  | $\frac{0.9 V_0}{K_0 T_0}$<br>0.190        | $3 T_0$<br>1.65 | —                  |
| PID | $\frac{1.2 V_0}{K_0 T_0}$<br>0.254        | $2 T_0$<br>1.1  | $0.5 T_0$<br>0.275 |

Name \_\_\_\_\_

ID \_\_\_\_\_

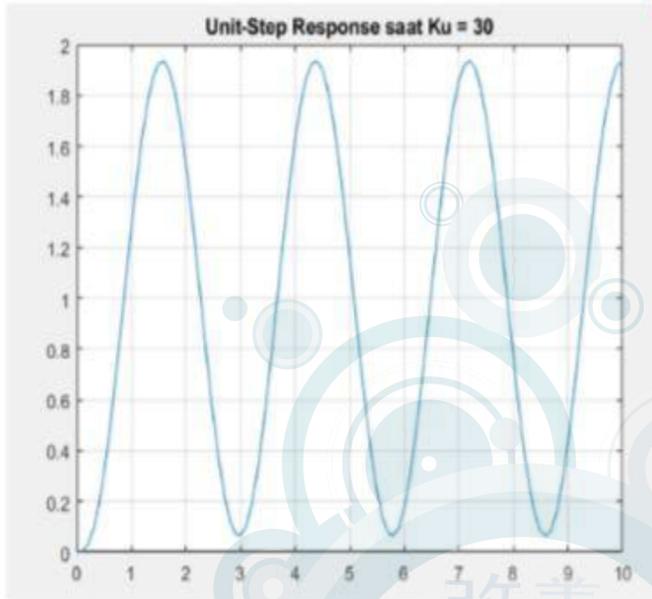
Q) Tune the PID controller using the zeigler nichols oscillation technique

| Type of Controller | $K_p$                   | $T_i$                   | $T_d$                      |
|--------------------|-------------------------|-------------------------|----------------------------|
| P                  | $0.5K_{cr}$             | $\infty$                | 0                          |
| PI                 | $0.45K_{cr}$            | $\frac{1}{1.2}P_{cr}$   | 0                          |
| PID                | $0.6K_{cr}$ <b>7.56</b> | $0.5P_{cr}$ <b>1.42</b> | $0.125P_{cr}$ <b>0.359</b> |



$P = 2.84 \text{ s}$

Q) Tune the PID controller using the zeigler nichols oscillation technique



$P = 10 / 3.5$   
 $= 2.86 s$   
 $K = 30$

The response above is obtained for the system for the PID auto tuning Ziegler Nichols oscillation method. What is the PID controller

| Type of Controller | $K_p$        | $T_i$                | $T_d$         |
|--------------------|--------------|----------------------|---------------|
| P                  | $0.5K_{cr}$  | $\infty$             | 0             |
| PI                 | $0.45K_{cr}$ | $\frac{1}{12}P_{cr}$ | 0             |
| PID                | $0.6K_{cr}$  | $0.5P_{cr}$          | $0.125P_{cr}$ |

$1.8$   
 $1.43$   
 $0.3575$

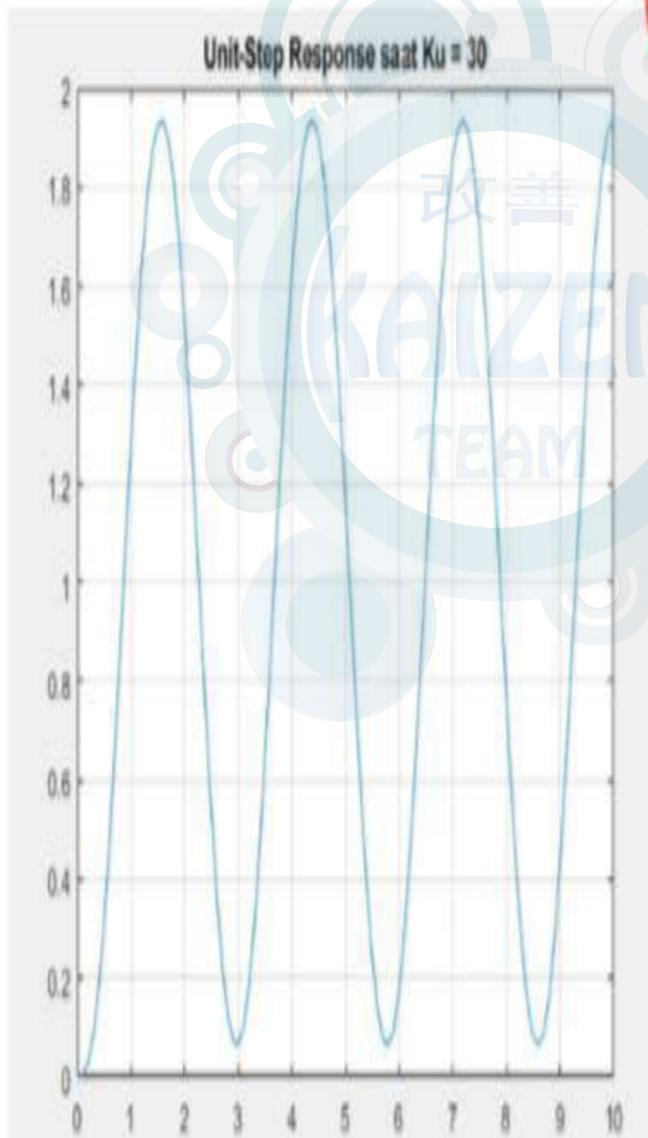
Quiz Industrial control

UoJ IE M. Barghash

Name \_\_\_\_\_

ID \_\_\_\_\_

Q) Tune the PID controller using the zeigler nichols oscillation technique



$$P = 1.0 / 3.5$$

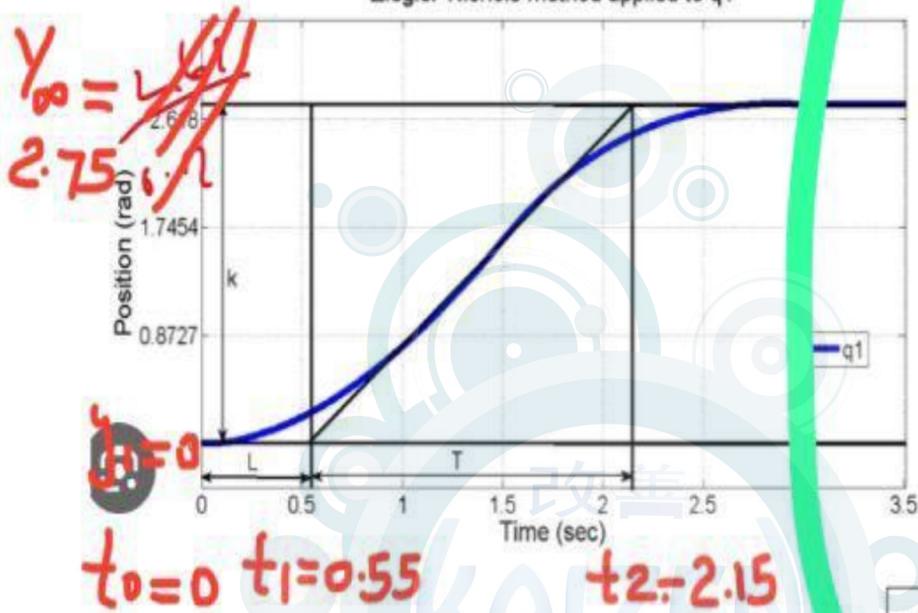
$$I = 2.865$$

$$K = 30$$

Name \_\_\_\_\_

ID \_\_\_\_\_

Ziegler-Nichols method applied to q1



$$K_0 = \frac{2.75 - 0}{0.3 - 0.1} = 13.75 \text{ rad/KW}$$

$$T_0 = 0.55 \text{ s}$$

$$V_0 = 1.6 \text{ s}$$

The response when we changes the input from 0.1 to 0.3 KW the output changed according to the figure

|     | $K_p$                             | $T_r$          | $T_d$             |
|-----|-----------------------------------|----------------|-------------------|
| P   | $\frac{V_0}{K_0 T_0} = 0.212$     | —              | —                 |
| PI  | $\frac{0.9 V_0}{K_0 T_0} = 0.190$ | $3 T_0 = 1.65$ | —                 |
| PID | $\frac{1.2 V_0}{K_0 T_0} = 0.254$ | $2 T_0 = 1.1$  | $0.5 T_0 = 0.275$ |

Flag question

$$s^4 + 3s^3 + 3s^2 + 2s^4 + K$$

what is the value for K for stability

改善

negative

$s_0$

|       |    |              |   |
|-------|----|--------------|---|
| $s^4$ | 3  | 3            | K |
| $s^3$ | 3  | 0            | 0 |
| $s^2$ | 3  | <del>3</del> | 0 |
| $s^1$ | -K | 0            | 0 |
| $s^0$ | K  | 0            | 0 |

$0 < K < 14/9$   
 $s^4$  1 3 K  
 $s^3$  3 2 0  
 $s^2$  1/3 K 0  
 $s^1$  14-9K 0 0  
 $s^0$  K 0 0

$14-9K > 0$   
 $14 > 9K$

$K > 0$   
 $K < 0$   
 $K > 0$

won't be stable!

if Q was wrong  $s^4 + 3s^3 + 3s^2 + 2s + K$

$$s^3 + s^2 + 2s + K = 0$$

what is the value for K for stability

|       |       |   |   |
|-------|-------|---|---|
| $s^3$ | 1     | 2 | 0 |
| $s^2$ | 1     | K | 0 |
| $s^1$ | $2-K$ | 0 | 0 |
| $s^0$ | K     | 0 | 0 |

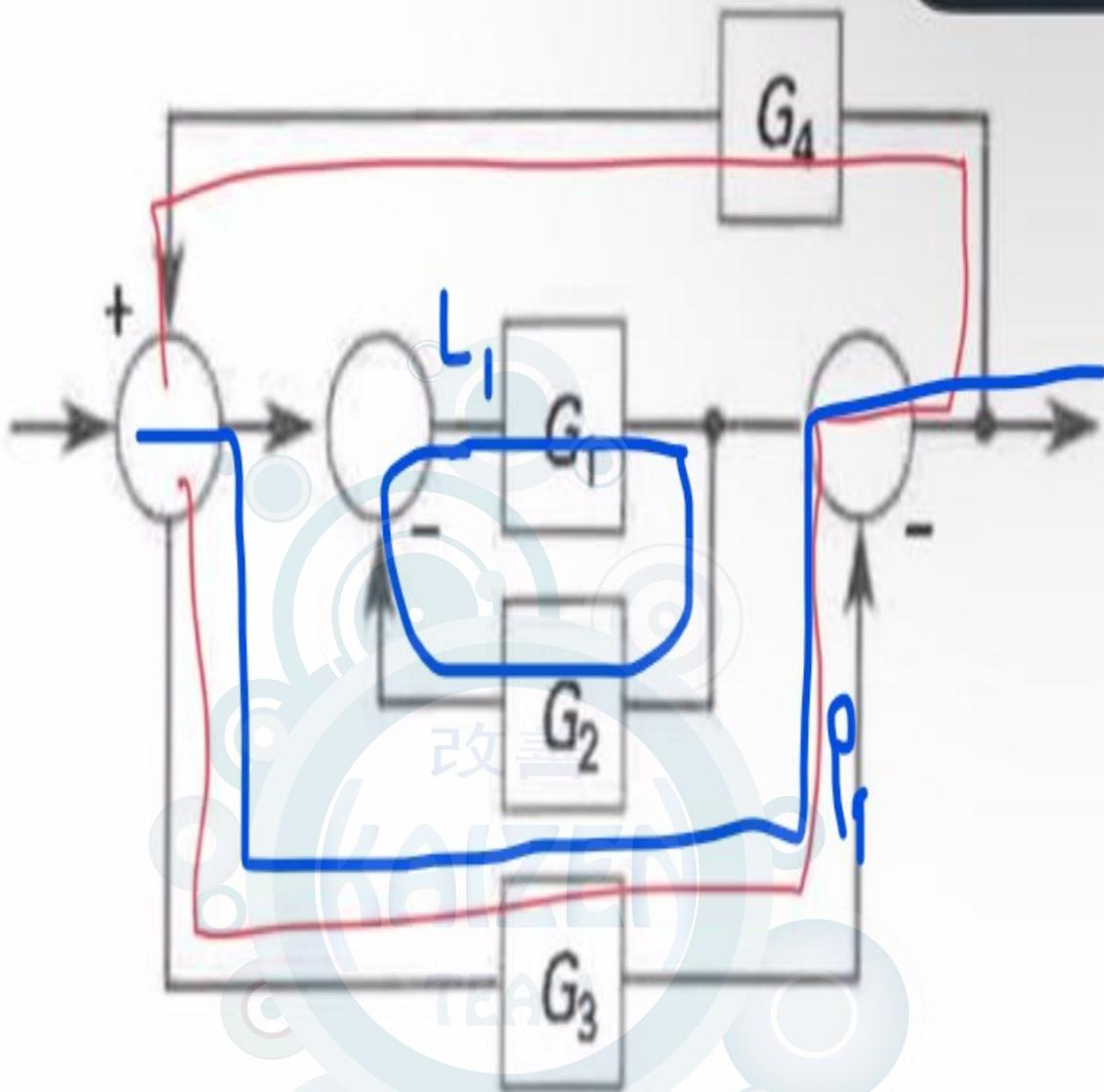
$$2 - K > 0$$

$$K > 0$$

$$2 > K$$

$$2 > K > 0$$

equivalent transfer function for



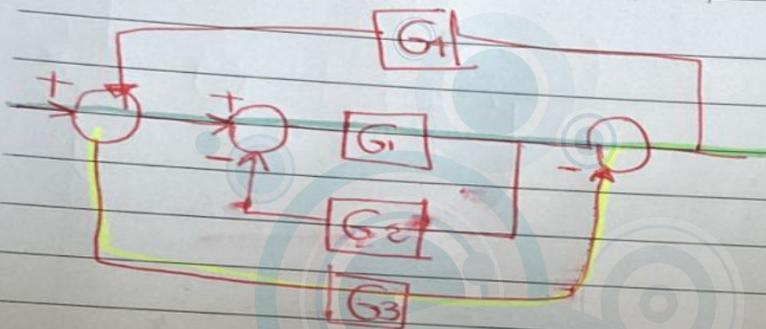
$$G_1 - G_3$$

---


$$1 - (-G_1 G_2 + G_1 G_4 - G_3 G_4) + (G_1 G_2 G_3 G_4)$$

التاريخ :

الموضوع :



paths

①  $G_1 \quad \Delta_1 = 1$

②  $-G_3 \rightarrow$  if we removed the path we would still have the loop  
 $-G_1G_2 \quad \Delta_2 = 1 + G_1G_2$

loops

Nontouching

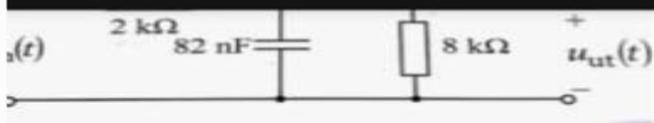
①  $+G_1G_4$

②/③  $G_1G_2G_3G_4$

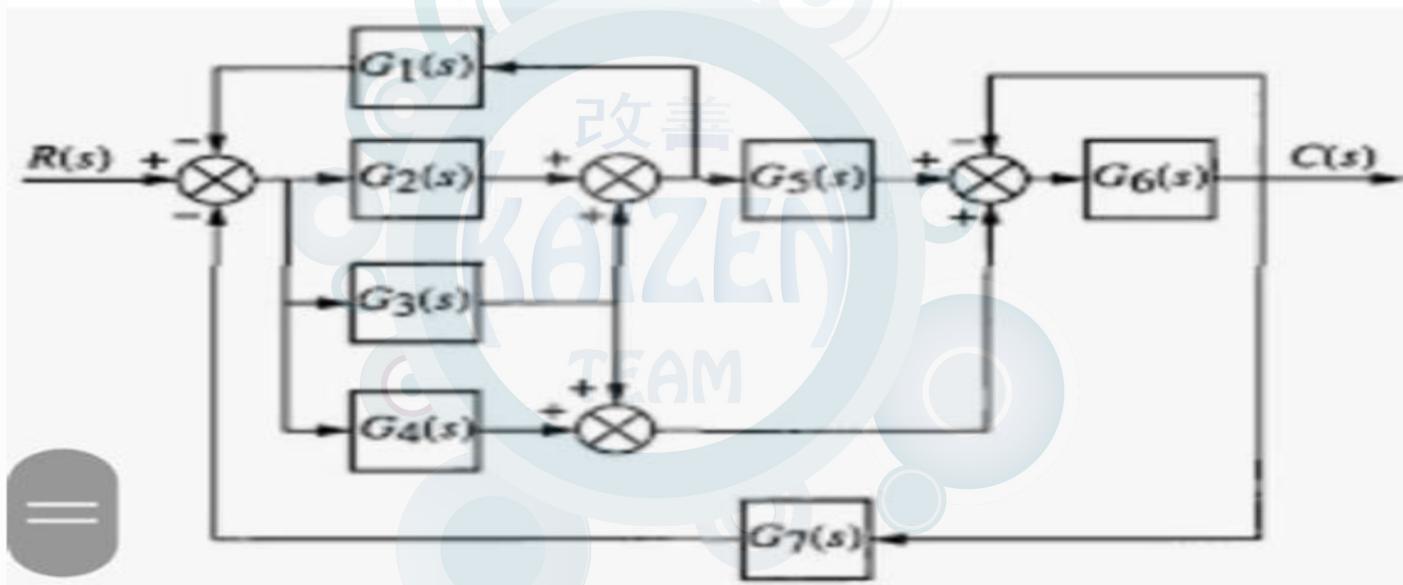
②  $-G_1G_2$

③  $+G_3G_4$

$$1 - G_1G_4 + G_1G_2 + G_3G_4 - G_1G_2G_3G_4$$



Find the equivalent transfer function for (5 points)



Subject: .....

paths:-

1  $G_2 G_5 G_6 \quad \Delta_1 = 1$

2  $G_3 G_5 G_6 \quad \Delta_2 = 1 \quad C(s)/R(s) =$

3  $G_4 G_6 \quad \Delta_3 = 1$

4  $G_3 G_6 \quad \Delta_4 = 1 \quad \frac{G_2 G_5 G_6 + G_3 G_5 G_6 + G_4 G_6 + G_3 G_6}{1 + G_1 G_2 + G_6 + G_2 G_5 G_6 G_7 + G_3 G_5 G_6 G_7}$

loops:-

1  $-G_2 G_1$

2  $-G_6$

3  $-G_2 G_5 G_6 G_7$

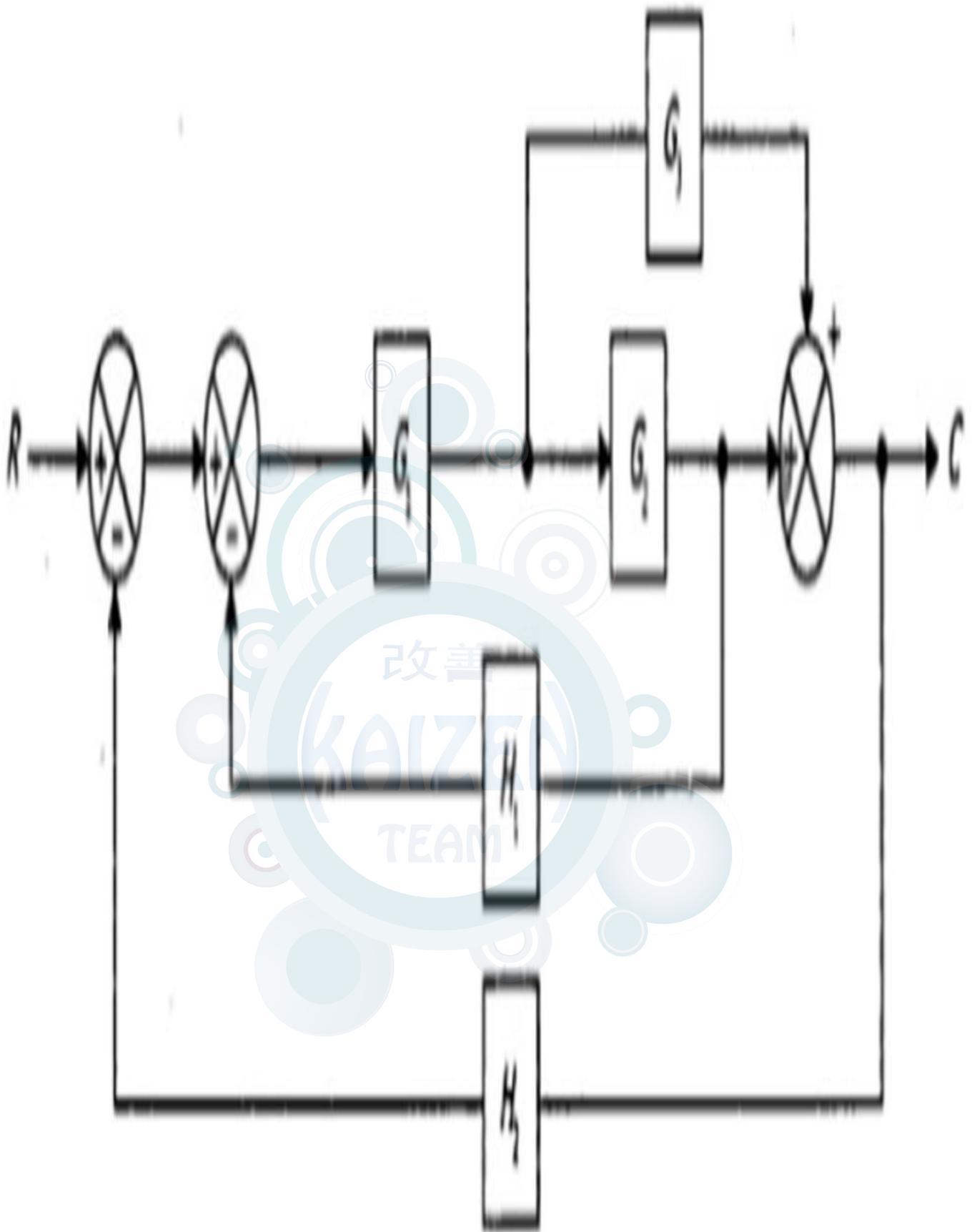
4  $-G_3 G_5 G_6 G_7$

5  $-G_4 G_6 G_7$

6  $-G_3 G_6 G_7$

non touching loops

1/2  $G_1 G_2 G_6$



loop

paths

loops

$$\boxed{1} \quad G_1 G_2$$

$$\boxed{1} \quad -G_1 G_2 H_1$$

$$\boxed{2} \quad G_1 G_3$$

$$\boxed{2} \quad -G_1 G_2 H_2$$

$$\Delta_1 = 1$$

$$\boxed{3} \quad -G_1 G_3 H_2$$

$$\Delta_2 = 1$$

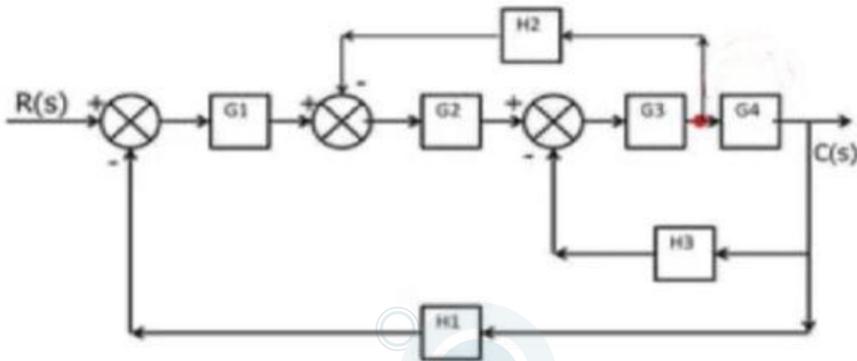
No non touching loops

$$\underline{G_1 G_2 + G_1 G_3}$$

$$1 + G_1 G_2 H_1 + G_1 G_2 H_2$$

$$+ G_1 G_3 H_2$$

Q4) Find the equivalent transfer function for (5 points)



Paths

$P_1: G_1 G_2 G_3 G_4$

loops

$$\boxed{1} \quad -G_2 G_3 H_2$$

$$\boxed{2} \quad -G_1 G_2 G_3 G_4 H_1$$

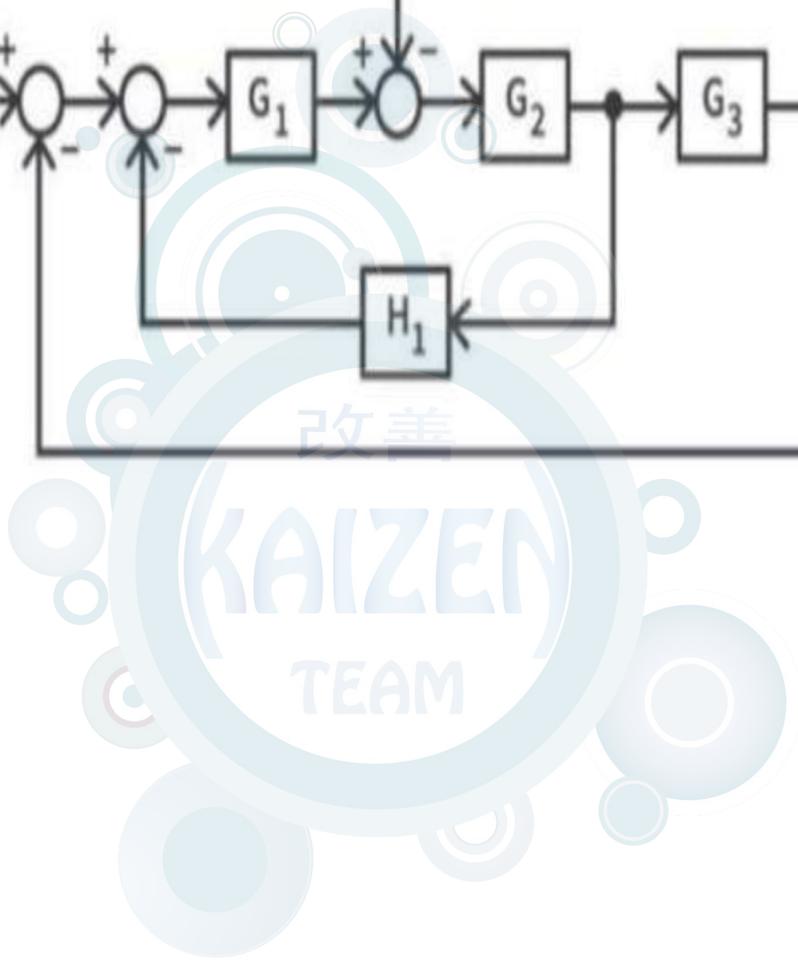
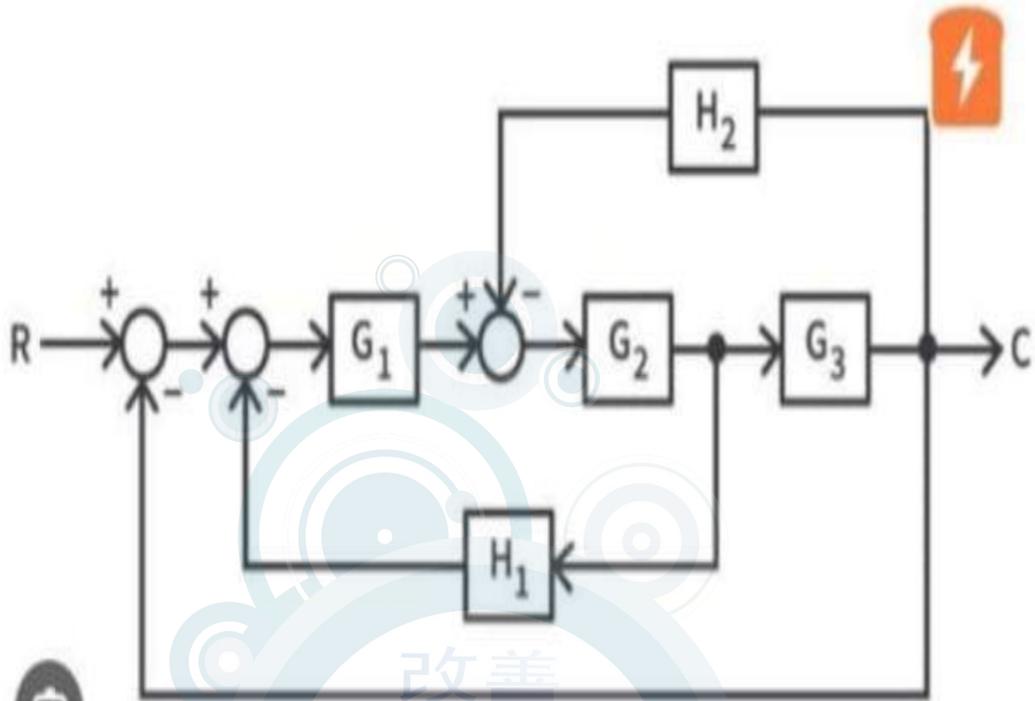
$$\boxed{3} \quad -G_3 G_4 H_3$$

$$\frac{C}{R} = \frac{G_1 G_2 G_3 G_4}{1 + G_2 G_3 H_2 + G_1 G_2 G_3 G_4 H_1 + G_3 G_4 H_3}$$

Name: \_\_\_\_\_

ID: \_\_\_\_\_

Find the equivalent transfer function



Paths:

loops:

$$P_1: G_1 G_2 G_3$$

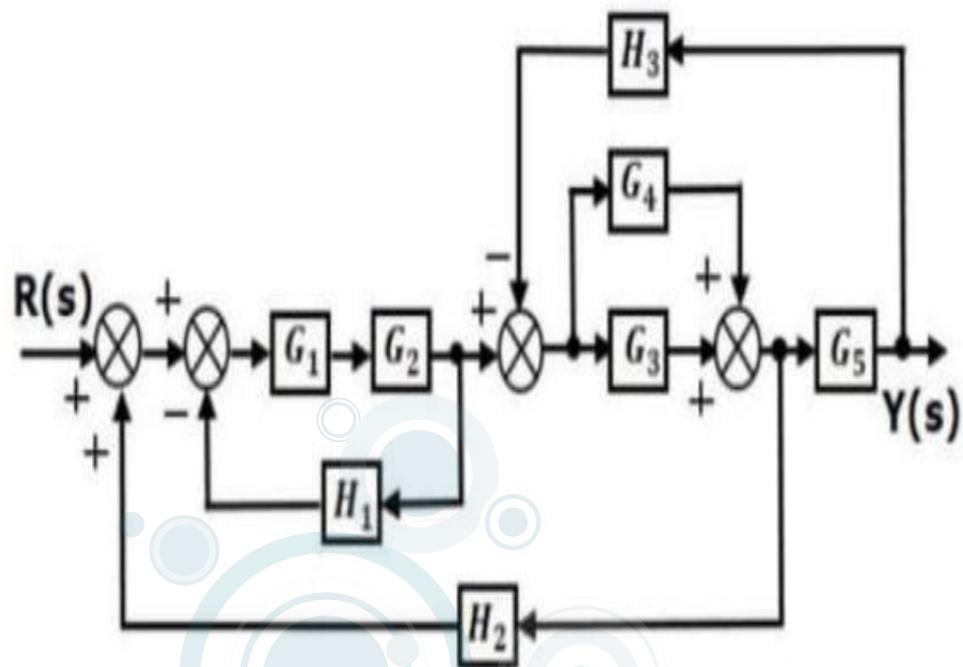
$$\boxed{1} \quad -G_1 G_2 H_1$$

$$\boxed{2} \quad -G_1 G_2 G_3$$

$$\boxed{3} \quad -G_2 G_3 H_2$$

$$\frac{C}{R} = \frac{G_1 G_2 G_3}{1 + G_1 G_2 H_1 + G_1 G_2 G_3 + G_2 G_3 H_2}$$

Find the equivalent transfer function



paths

loops:

$$P_1: G_1 G_2 G_3 G_5$$

$$\boxed{1} - G_1 G_2 H_1$$

$$P_2: G_1 G_2 G_4 G_5$$

$$\boxed{2} G_1 G_2 G_3 H_2$$

$$\boxed{3} - G_3 G_5 H_3$$

$$\boxed{4} - G_4 G_5 H_3$$

$$\boxed{5} G_1 G_2 G_4 H_2$$

Non touching loops

$$\boxed{1} + \boxed{4} G_1 G_2 G_4 G_5 H_1 H_3$$

$$\boxed{2} + \boxed{3} G_1 G_2 G_3 G_5 H_1 H_3$$

$$\frac{Y}{R} = \frac{G_1 G_2 G_3 G_5 + G_1 G_2 G_4 G_5}{1 + G_1 G_2 H_1 - G_1 G_2 G_3 H_2 + G_3 G_5 H_3 + G_4 G_5 H_3 - G_1 G_2 G_4 H_2 + G_1 G_2 G_4 G_5 H_1 H_3 + G_1 G_2 G_3 G_5 H_1 H_3}$$

29/9

```
Const int LED1=6, LED2=5, LED3=4;
```

```
Void setup()
```

```
{
```

```
pinMode(LED1, OUTPUT);
```

```
pinMode(LED2, OUTPUT);
```

```
pinMode(LED3, OUTPUT);
```

```
}
```

```
Void loop()
```

```
{
```

```
digitalWrite(LED1, HIGH);
```

```
delay(100);
```

```
digitalWrite(LED2, HIGH);
```

```
delay(100);
```

```
digitalWrite(LED3, HIGH);
```

```
}
```

Quiz Industrial control systems Prof. M. Barghash IE Dept SoC UoJ 7/1/2025

Name ID

---

Solve the following differential equation using ODE45 for t from 0 to 5

$$\ddot{W} + \dot{W} + 2W = \sin(t) \quad W(0) = 0 \quad \dot{W}(0) = 1 \quad \ddot{W}(0) = 2;$$

Quiz Industrial control systems Prof. M. Barghash IE Dept SoC UoJ 7/1/2025

Name ID

---

Solve the following differential equation using symbolic

$$\ddot{W} + \dot{W} + 2W = \sin(t) \quad W(0) = 0 \quad \dot{W}(0) = 1 \quad \ddot{W}(0) = 2;$$

## ODE 45

$w_1, w_2, w_3$

$$\dot{w}_2 = \dot{w}_1 \sim \textcircled{1}$$

$$\dot{w}_3 = \dot{w}_2 \sim \textcircled{2} = \ddot{w}_1$$

$$\dot{w}_3 + w_3 + w_2 + 2w_1 = \sin(t)$$

$$\dot{w}_3 = \sin(t) - w_3 - w_2 - 2w_1 \sim \textcircled{3}$$

function  $dw = \text{quiz}(t, w)$

$$[m, n] = \text{size}(w)$$

$$dw = \text{zeros}(m, n);$$

$$dw(1) = w(2);$$

$$dw(2) = w(3);$$

$$dw(3) = \sin(t) - w(3) - w(2) - 2 * w(1);$$

$$tspan = [0 5];$$

$$w_0 = [0; 1; 2];$$

$$[t, w] = \text{ode45}(@\text{quiz}, tspan, w_0)$$

## Symbolic

Syms w(t)

eqn = diff(w,t,3) + diff(w,t,2) + diff(w,t)  
+ 2\*w == sin(t);

dw = diff(w,t);

dw2 = diff(dw,t);

Cond = [ w(0) == 0, dw(0) == 1, dw2(0) == 2 ];

Sol = dsolve(eqn, Cond)

## Arduino

```
const int TPin = 0;
```

```
void setup()
```

```
{ Serial.begin(9600); }
```

```
void loop()
```

```
{ double Voltage, Temperature;
```

```
Voltage = getVoltage(TPin);
```

```
Temperature = (Voltage - 0.5) * 100;
```

```
Serial.print("T is: ");
```

```
Serial.println(Temperature);
```

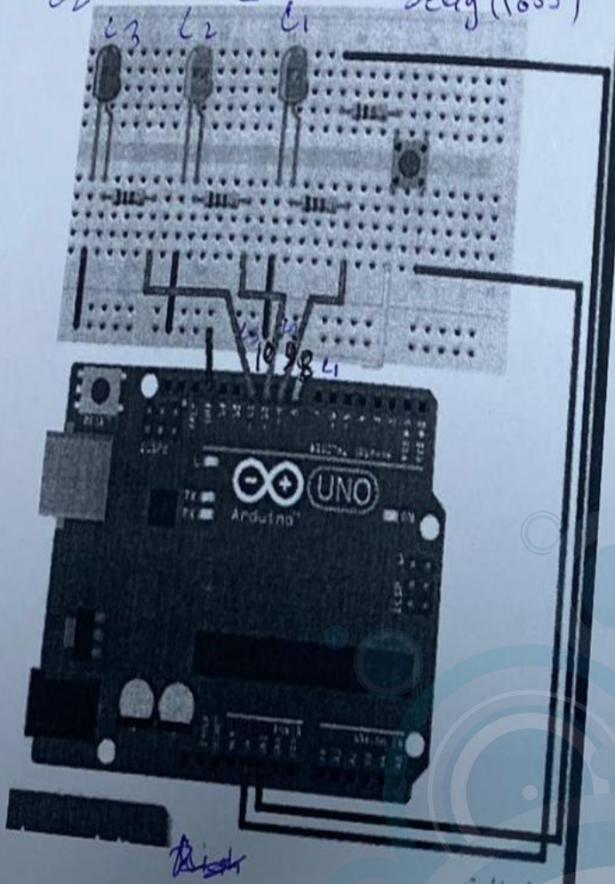
```
delay(1000); }
```

```
double getVoltage(int TPin)
```

```
{ return (analogRead(TPin) * 5/1024); }
```

For the following Arduino LED write the code for the lighting sequence right then middle then left then middle, separate each with 1 second delay

$L_2$   $L_3$   $L_2$   $L_1$  delay(1000)



const int L1=8, L2=9, L3=10;

void setup()

{

pinMode(L1, OUTPUT);

pinMode(L2, OUTPUT);

pinMode(L3, OUTPUT);

}

void loop()

{

digitalWrite(L1, HIGH);

digitalWrite(L2, LOW);

digitalWrite(L3, LOW);

delay(1000);

digitalWrite(L1, LOW);

digitalWrite(L2, HIGH);

digitalWrite(L3, LOW);

delay(1000);

digitalWrite(L1, LOW);

digitalWrite(L2, LOW);

digitalWrite(L1, LOW);

digitalWrite(L2, HIGH);

digitalWrite(L3, LOW);

delay(1000);

}

Solve the following differential equation using ODE45  $t \in [0, 5]$

$$\ddot{x} + 3x + 2t = 0 \quad x(0) = 0 \quad \dot{x}(0) = 1;$$

$$\ddot{x} = -3x - 2t$$

$$\dot{x}_2 = -3x_1 - 2t$$

$$\begin{aligned} x &= x_1 \\ \dot{x} &= x_2 \\ \ddot{x} &= \dot{x}_2 \\ x_1 &= x_2 \end{aligned}$$

function dx = quiz(t, X)

[m, n] = size(X);

dx = zeros(m, n);

dx(1) = X(2);

dx(2) = -3 \* X(1) - 2 \* t;

tspan = [0 5];

X0 = [0; 1];

[t, X] = ode45(@quiz, tspan, X0);

plot(t, X)  
Quiz Industrial control systems

Name

ID

Prof. M. Barghash

IE Dept SoC UoJ 7/1/2025

Solve the following differential equation using symbolic

$$\ddot{x} + 3x + 2t = 0 \quad x(0) = 0 \quad \dot{x}(0) = 1;$$

syms x(t)

equ = diff(x, t, 2) + 3 \* x + 2 \* t == 0;

dx = diff(x, t);

conds = [x(0) == 0, dx(0) == 1];

S = dsolve(equ, conds)

$$\ddot{x} + 1 = t \quad x(0) = 0 \quad \dot{x}(0) = 0$$

a)

$x_1, x_2$

$$\dot{x}_1 = x_2 \sim \textcircled{1}$$

$$\dot{x}_2 + 1 = t$$

$$\dot{x}_2 = t - 1 \sim \textcircled{2}$$

function  $dx = \text{quiz}(t, x)$

$$[m, n] = \text{size}(x);$$

$$x = \text{zeros}(m, n);$$

$$dx(1) = x(2);$$

$$dx(2) = t - 1;$$

b)

Syms  $x(t)$

$$\text{eqn} = \text{diff}(x, t) + 1 == t;$$

$$dx = \text{diff}(x, t);$$

$$\text{Cond} = [x(0) == 0, dx(0) == 0];$$

$$\text{Sol} = \text{dsolve}(\text{eqn}, \text{Cond});$$

$tspan = [0 \ 10];$   $\rightarrow$  he should have given us

$$x_0 = [0; 0];$$

This

$$[t \ x] = \text{ode45}(@\text{quiz}, tspan, x_0)$$

```
Const int LED1=6, LED2=5, LED3=4;
```

```
Void setup()
```

```
{
```

```
pinMode(LED1, OUTPUT);
```

```
pinMode(LED2, OUTPUT);
```

```
pinMode(LED3, OUTPUT);
```

```
}
```

```
Void loop()
```

```
{
```

```
digitalWrite(LED1, HIGH);
```

```
delay(100);
```

```
digitalWrite(LED2, HIGH);
```

```
delay(100);
```

```
digitalWrite(LED3, HIGH);
```

```
}
```

```
Const int TPin = 0;
```

```
Void setup()
```

```
{  
  Serial.begin(9600);  
}
```

```
Void loop()
```

```
{  
  double voltage, temperature;
```

```
  voltage = getVoltage(TPin);
```

```
  temperature = (voltage - 0.5) * 100;
```

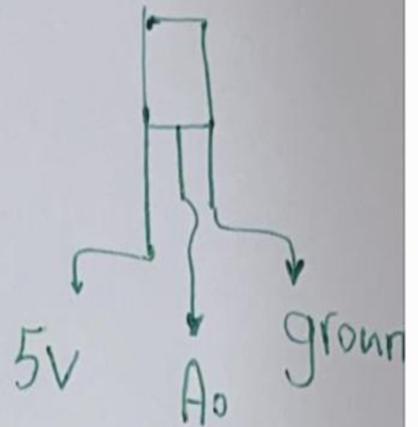
```
  Serial.print("T is: ");
```

```
  Serial.println(temperature);  
  delay(1000);  
}
```

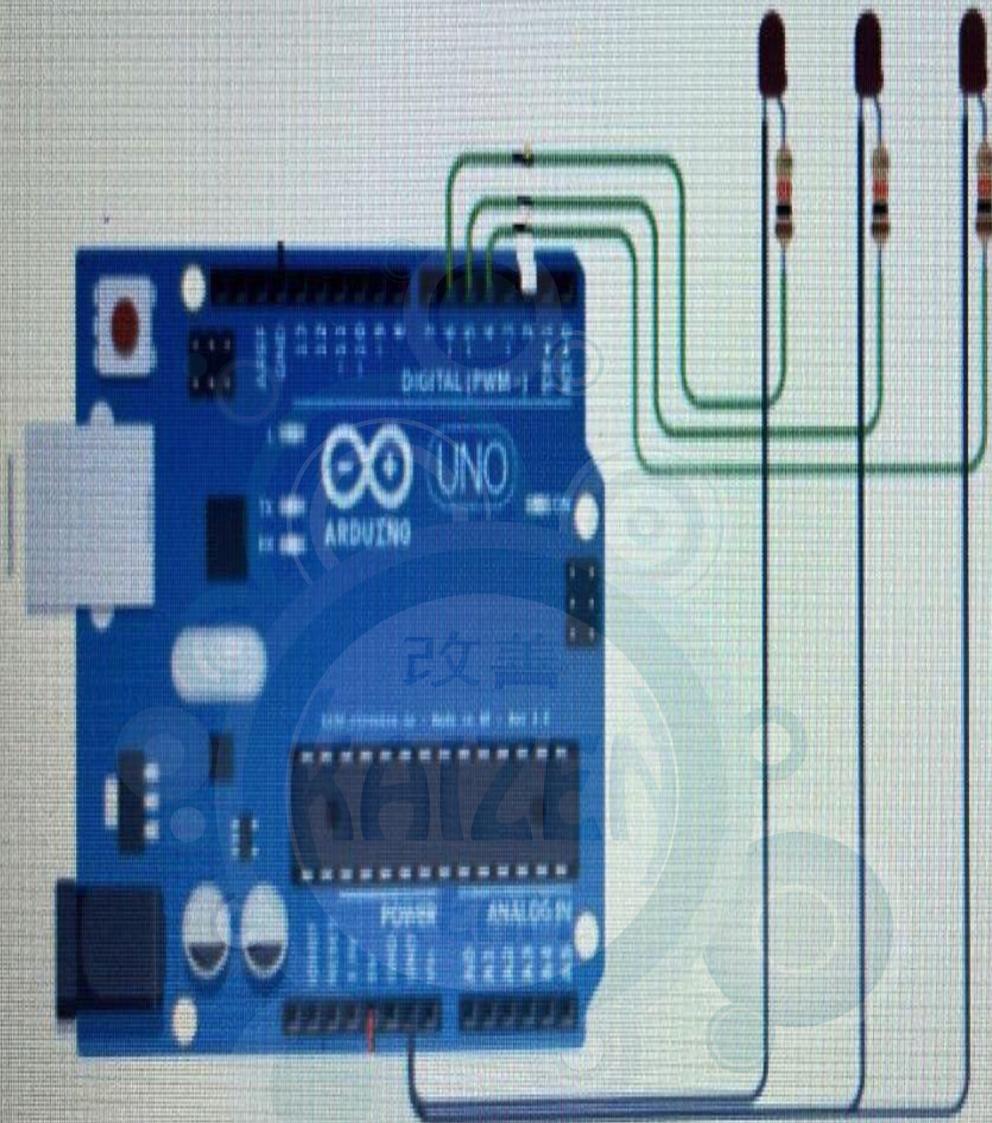
```
double getVoltage(int TPin)
```

```
{
```

```
  Return (analogRead(TPin) * 5 / 1024);  
}
```



Q) Write the code for the light to start from left to right; separated by 0.1 seconds



Your Answer





# Quiz Industrial contro...



Quiz Industrial control systems Prof M. Barghash IE dept Sch o Eng UoJ 23/7/2024

Name: \_\_\_\_\_ ID: \_\_\_\_\_

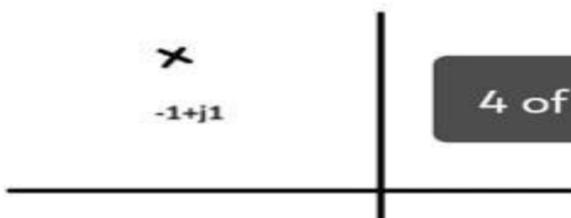
For the following pole find the peak time



Quiz Industrial control systems Prof M. Barghash IE dept Sch o Eng UoJ 23/7/2024

Name: \_\_\_\_\_ ID: \_\_\_\_\_

For the following pole find the percent overshoot



4 of 7



$$\omega_n \xi = 1$$

$$\omega_n \sqrt{1 - \xi^2} = 1$$

$$T_s = \frac{1}{\omega_n \xi} = 4 \text{ s}$$

$$po\% = \exp\left(\frac{-\pi \xi}{\sqrt{1 - \xi^2}}\right) \cdot 100\%$$

改善

$$= 4.32\%$$

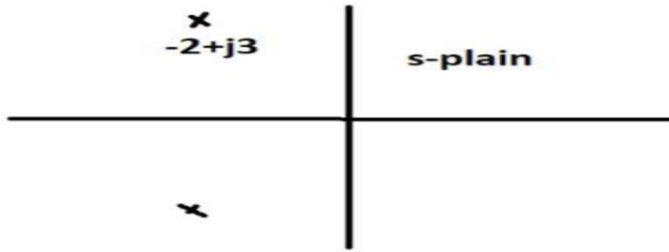
$$T_p = \frac{\pi}{\omega_n \sqrt{1 - \xi^2}} = 3.14 \text{ s}$$

$$T_r = 2.36 \text{ s} \leftarrow \text{extra}$$

NAME: \_\_\_\_\_

ID: \_\_\_\_\_

For the following system with roots shown in the following s-plane find the rise time, settling time and percent overshoot



$$\omega_n \xi = 2$$

$$\omega_n \sqrt{1 - \xi^2} = 3$$

$$T_r = \frac{\pi - \theta}{\omega_n \sqrt{1 - \xi^2}}$$

$$= \frac{\pi - \tan^{-1}\left(\frac{3}{2}\right)}{3}$$

$$= 0.7196 \text{ s}$$

$$T_s = \frac{4}{\omega_n \xi} = \frac{4}{2} = 2 \text{ seconds}$$

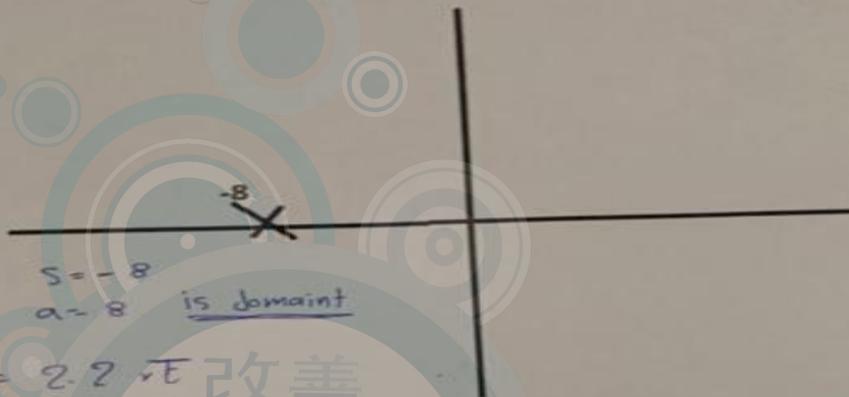
$$\text{PO\%} = \exp\left(\frac{-\pi \xi}{\sqrt{1 - \xi^2}}\right) \times 100\%$$

$$= 12.31\%$$

Name \_\_\_\_\_

ID: \_\_\_\_\_

Find the rise time for the following dominant pole



$$s = -8$$

$$\alpha = 8$$

is dominant

$$T_r = 2.2 \sqrt{\tau}$$

Your solution

$$2.2 \times \frac{1}{\alpha}$$

KAIZEN

TEAM

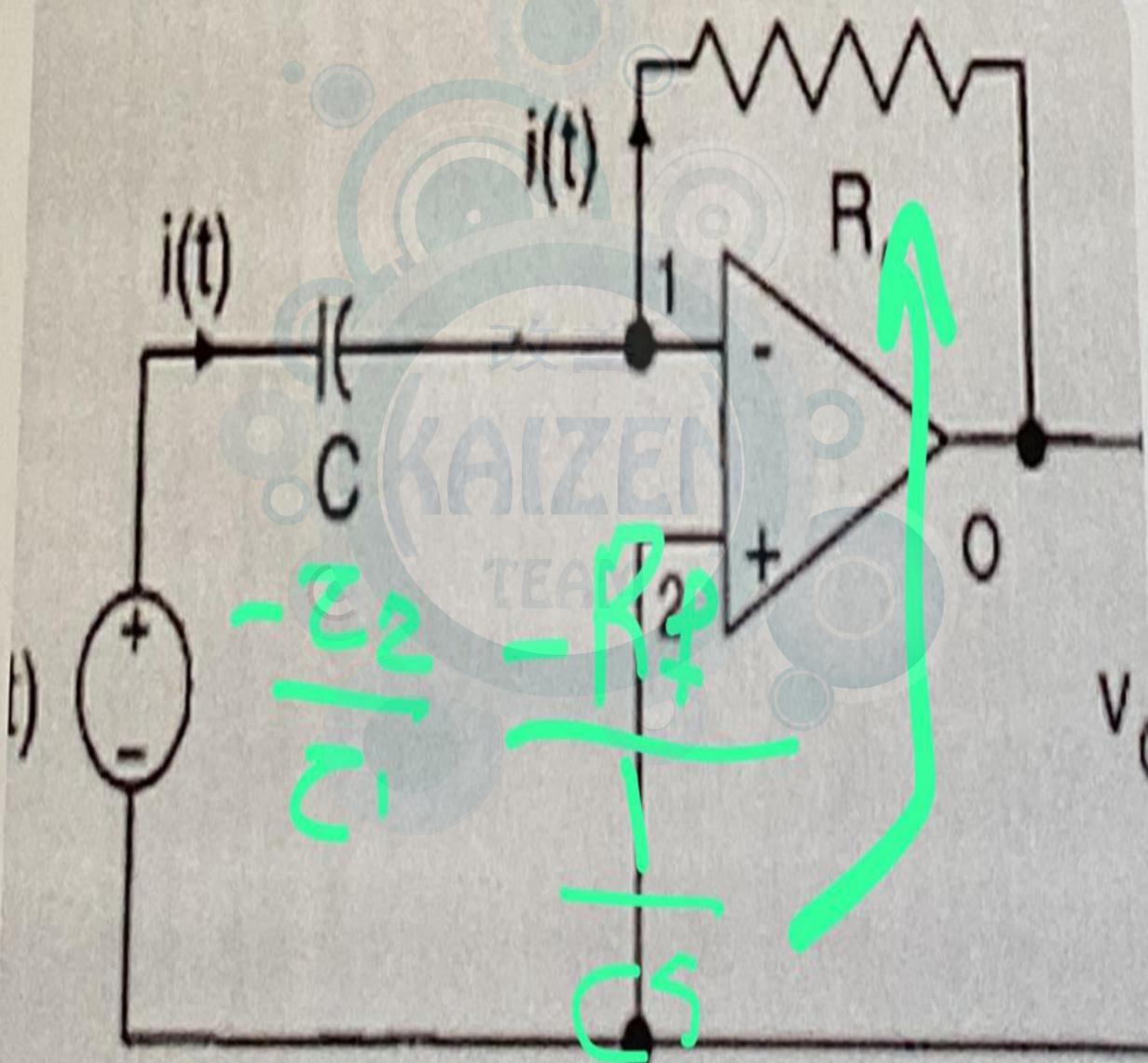
Quiz control 5/1/2025

Name

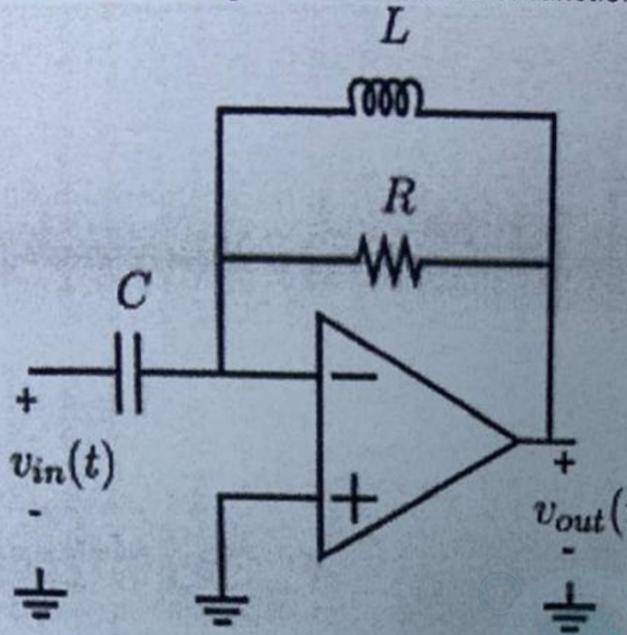
ID

-RPS

Model the following and find the transfer function



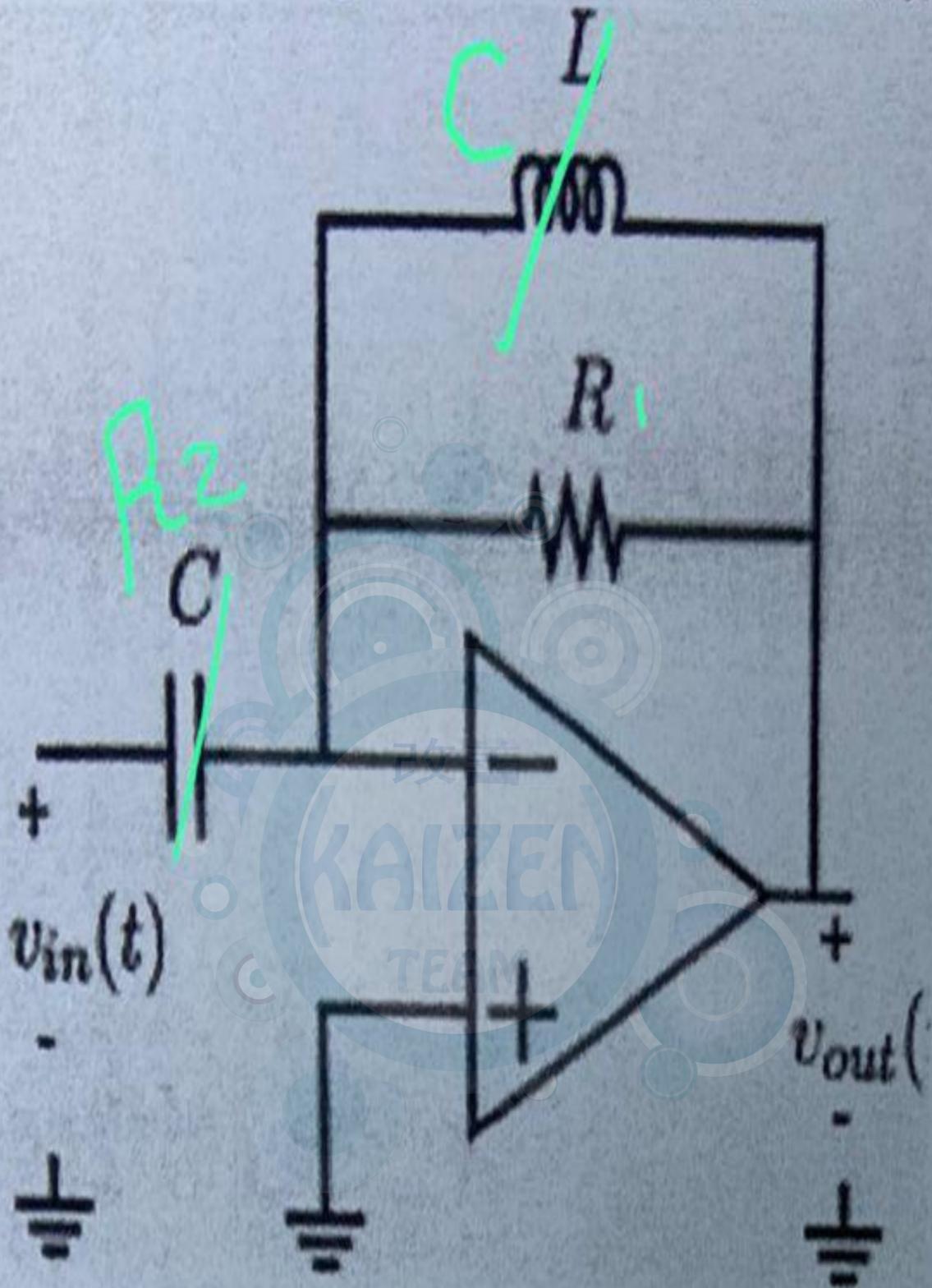
Model the following and find the transfer function



$$-\frac{Z_2}{Z_1} = \frac{Ls * R}{Ls + R}$$

$$\frac{LRS^2}{Ls + R}$$

Model the following and find the transfer function



NAME:

ID:

For the following system find the rise time, settling time and percent overshoot

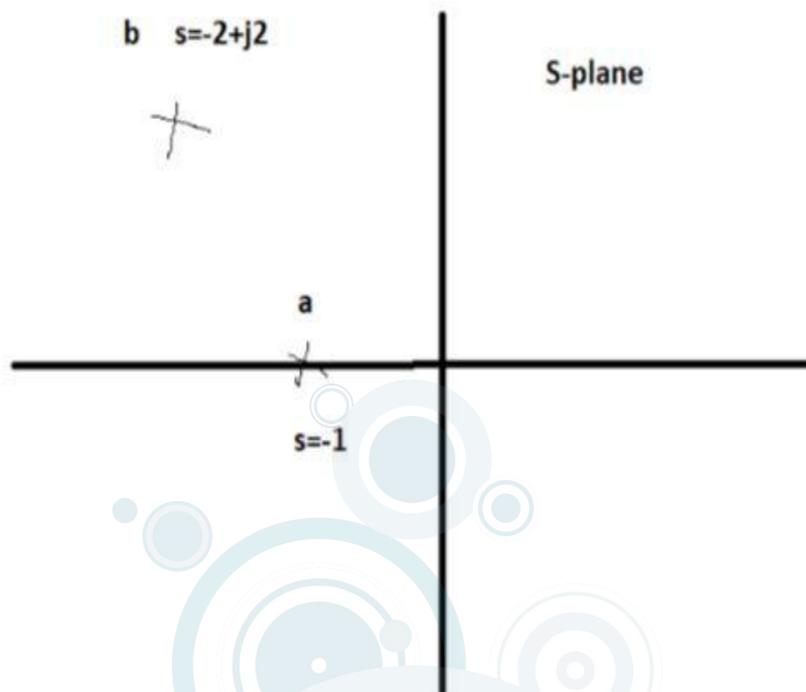
$$\frac{C}{R} = \frac{s+3}{s^2+s+4.25}$$

$$\frac{s+3}{s^2+s+4.25} \quad \text{Complex}$$
$$(0.5^2)$$
$$0.25 < 4.25$$
$$\omega_n = \sqrt{b} = \sqrt{4.25}$$
$$\xi = \frac{a}{2\sqrt{b}} = \frac{1}{2\sqrt{4.25}}$$
$$T_r = \frac{\pi}{\omega_n \sqrt{1 - \xi^2}} = \frac{\pi}{\sqrt{4.25} \sqrt{1 - \left(\frac{1}{2\sqrt{4.25}}\right)^2}}$$

$$0.908 \checkmark$$
$$T_s = \frac{4}{\omega_n \xi} = 8.9 \checkmark$$

$$P.O. = 45.6\% \checkmark$$

Q5) a) For a and b poles in the following find the associated settling time and percent overshoot (5 points)

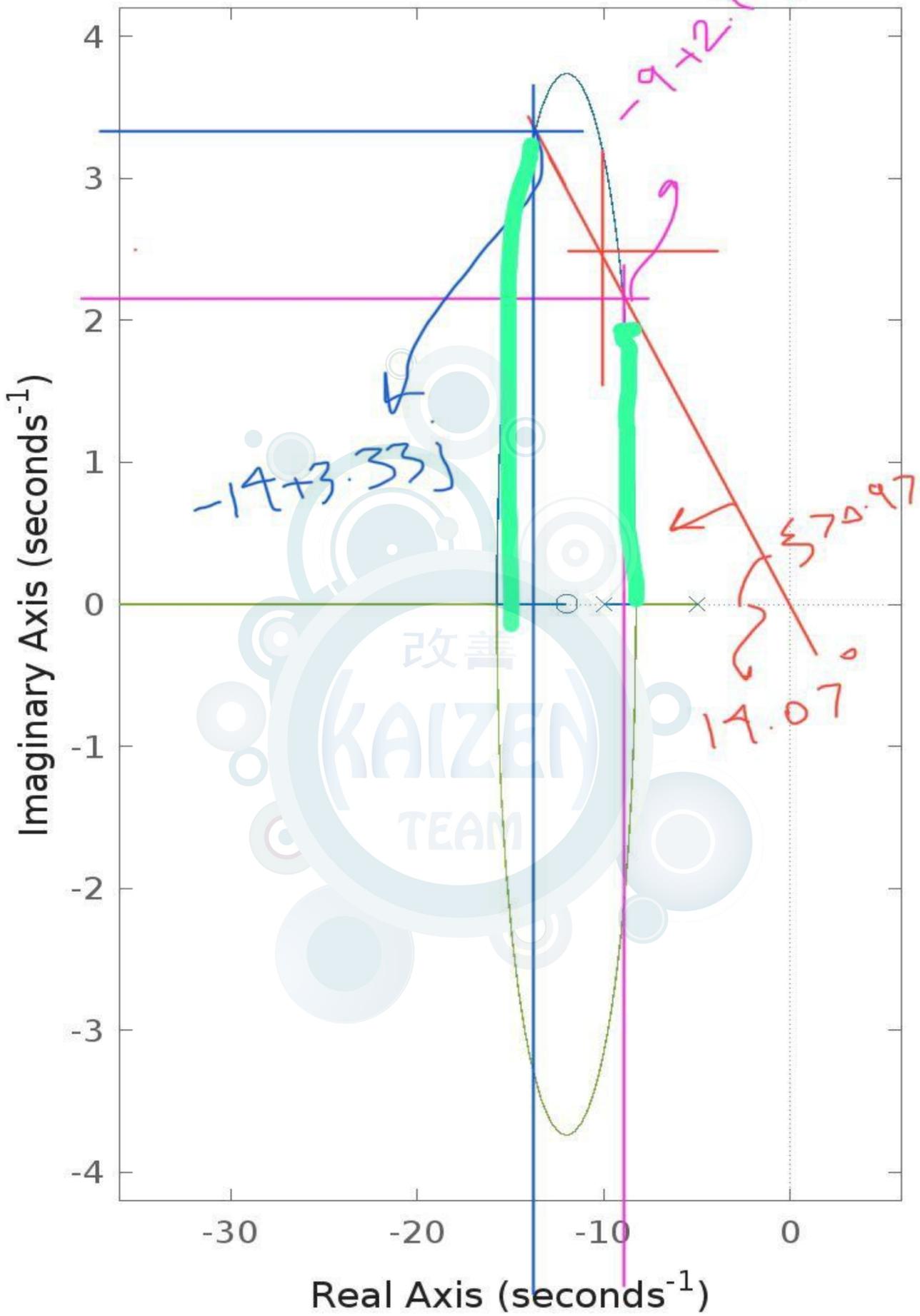


Dominant pole ( $s = -1$ )

$$T_s = \frac{4}{1} = 4$$

Po%:  $\rightarrow$  there is no Po%  
(first order)

# Root Locus



$$\xi > 0.97 \quad \begin{matrix} 30 \rightarrow 10 \\ 27 \quad ? \end{matrix}$$

first point

$$\xi = 0.97$$

$$\begin{matrix} 30 \rightarrow ? \\ 5 \end{matrix}$$

$$-9 + 2.17j = 5$$

$$\theta = \cos^{-1} 0.97$$

$$= 14.07^\circ$$

$$\frac{k(s+12)}{(s+10)(s+5)} = 1$$

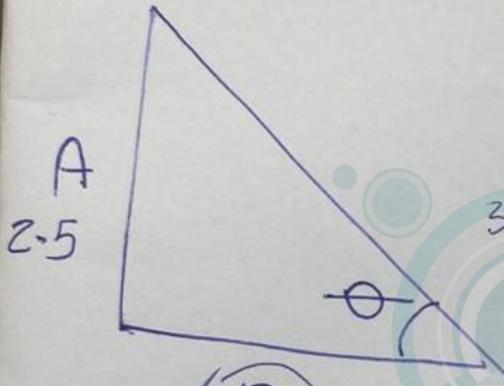
$$\tan \theta = 0.25 = \frac{A}{B}$$

Case 1

$$k = 2.94$$

$$|k| < 2.94$$

second point



(B)

10

$$\begin{matrix} 30 \rightarrow 10 \\ 12 \rightarrow ? \end{matrix}$$

$$\begin{matrix} 30 \rightarrow 1 \\ 10 \rightarrow ? \end{matrix}$$

改善

$$\frac{k(s+12)}{(s+10)(s+5)} = 1$$

$$k = 12.86$$

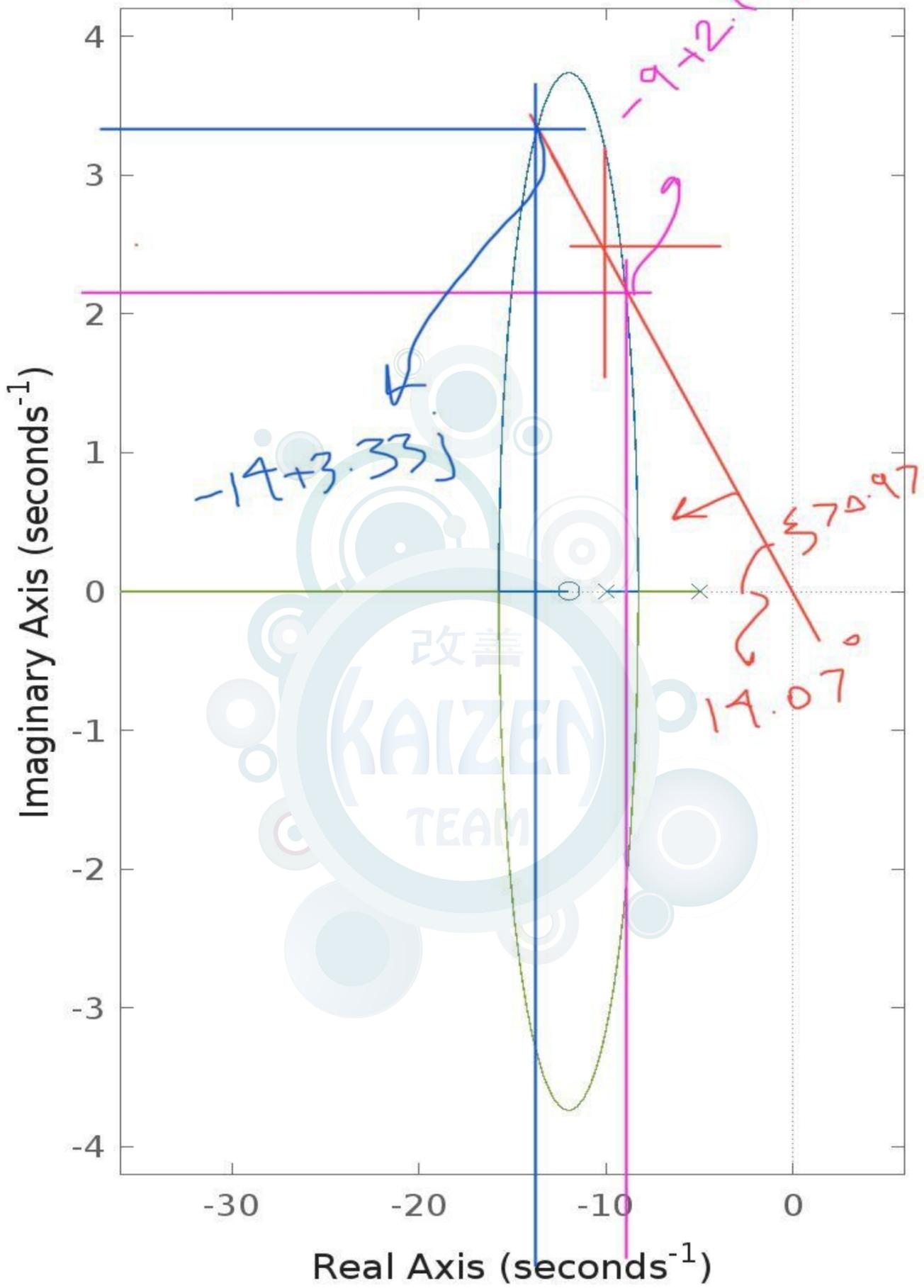
$$|k| > 12.86$$

we want below the line

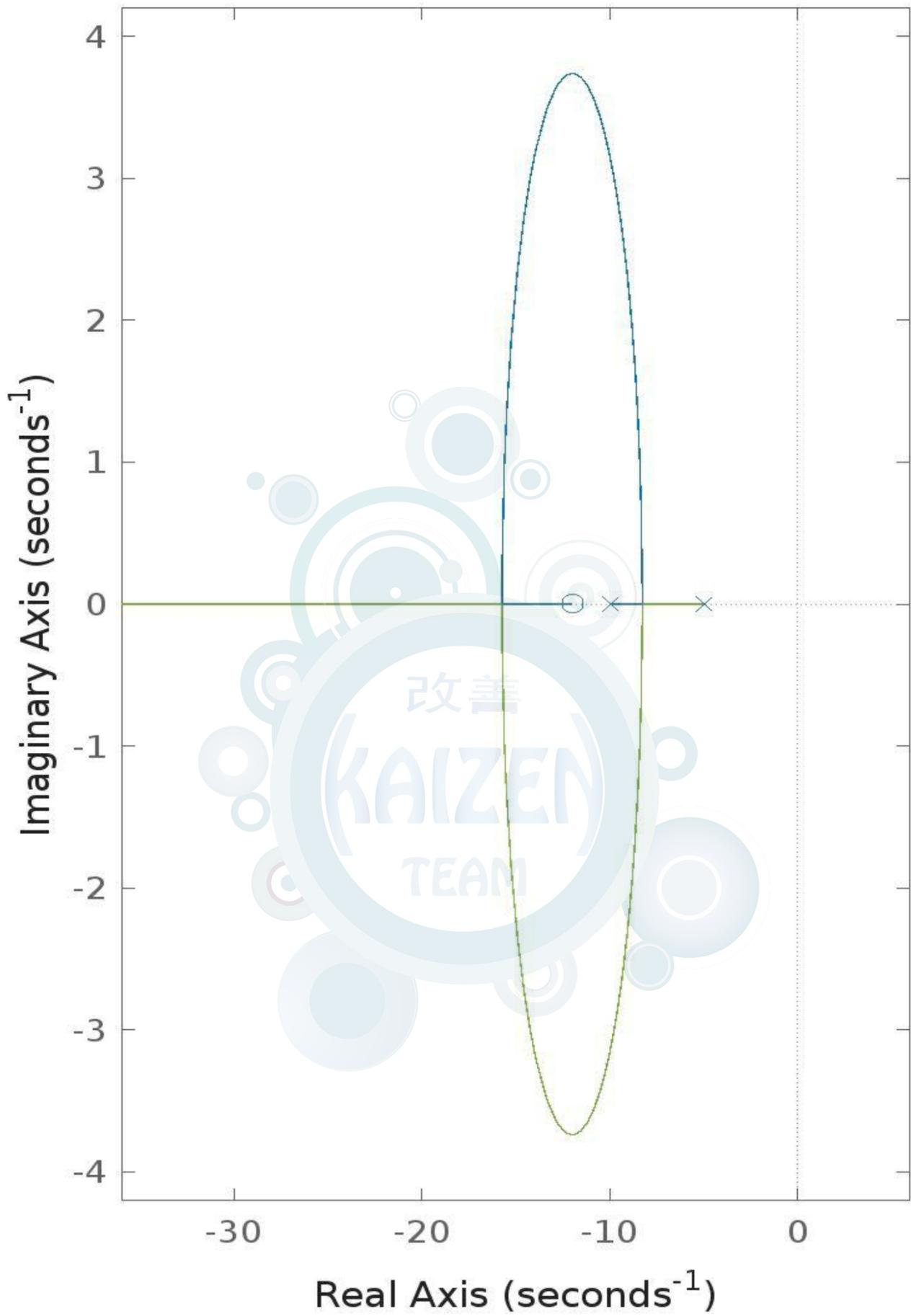
Case 2

no

# Root Locus



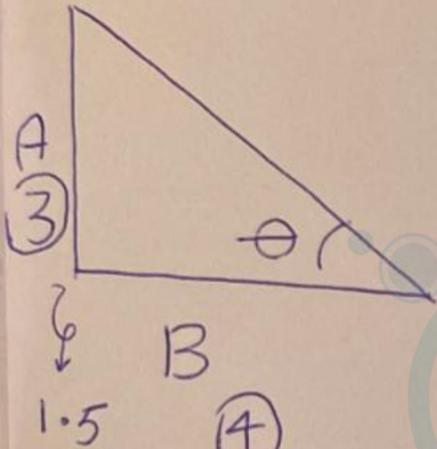
# Root Locus



$$\xi > 0.8$$

$$\theta = \cos^{-1} 0.8 \\ = 36.87^\circ$$

$$\tan \theta = 0.75 = \frac{A}{B}$$



we want  
under the  
line

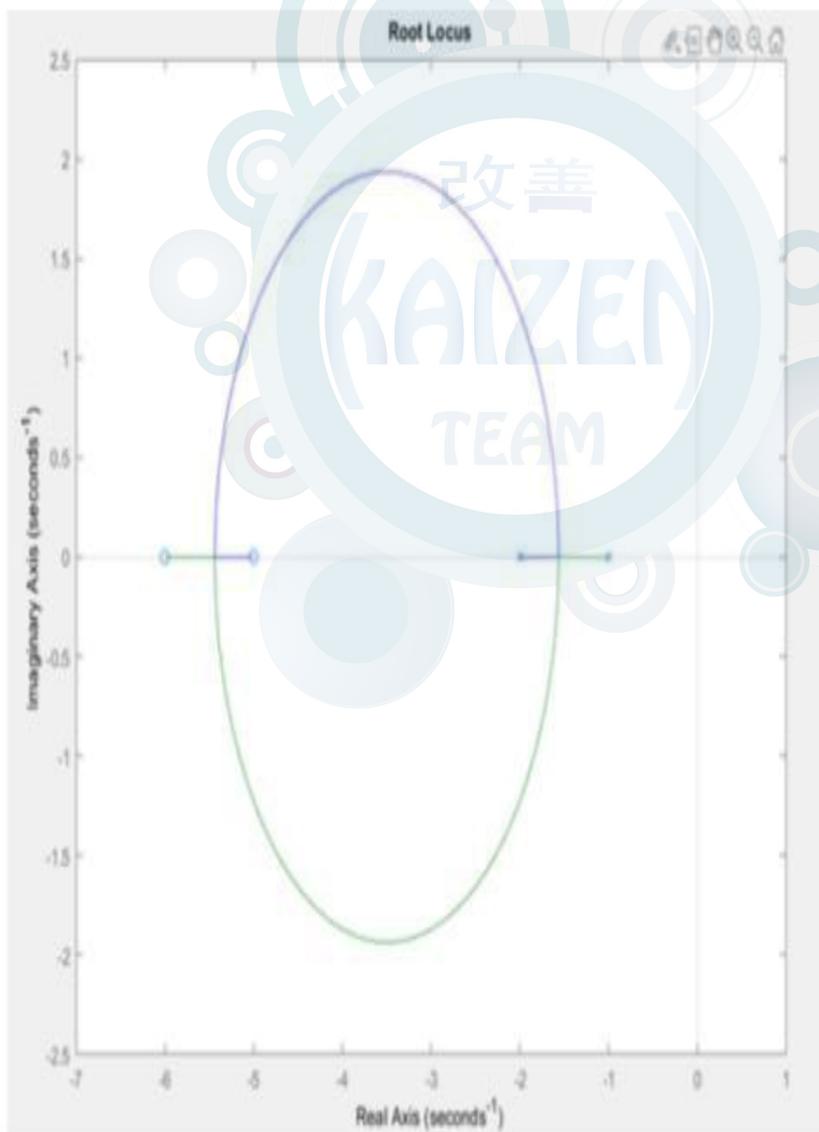
So all  
points

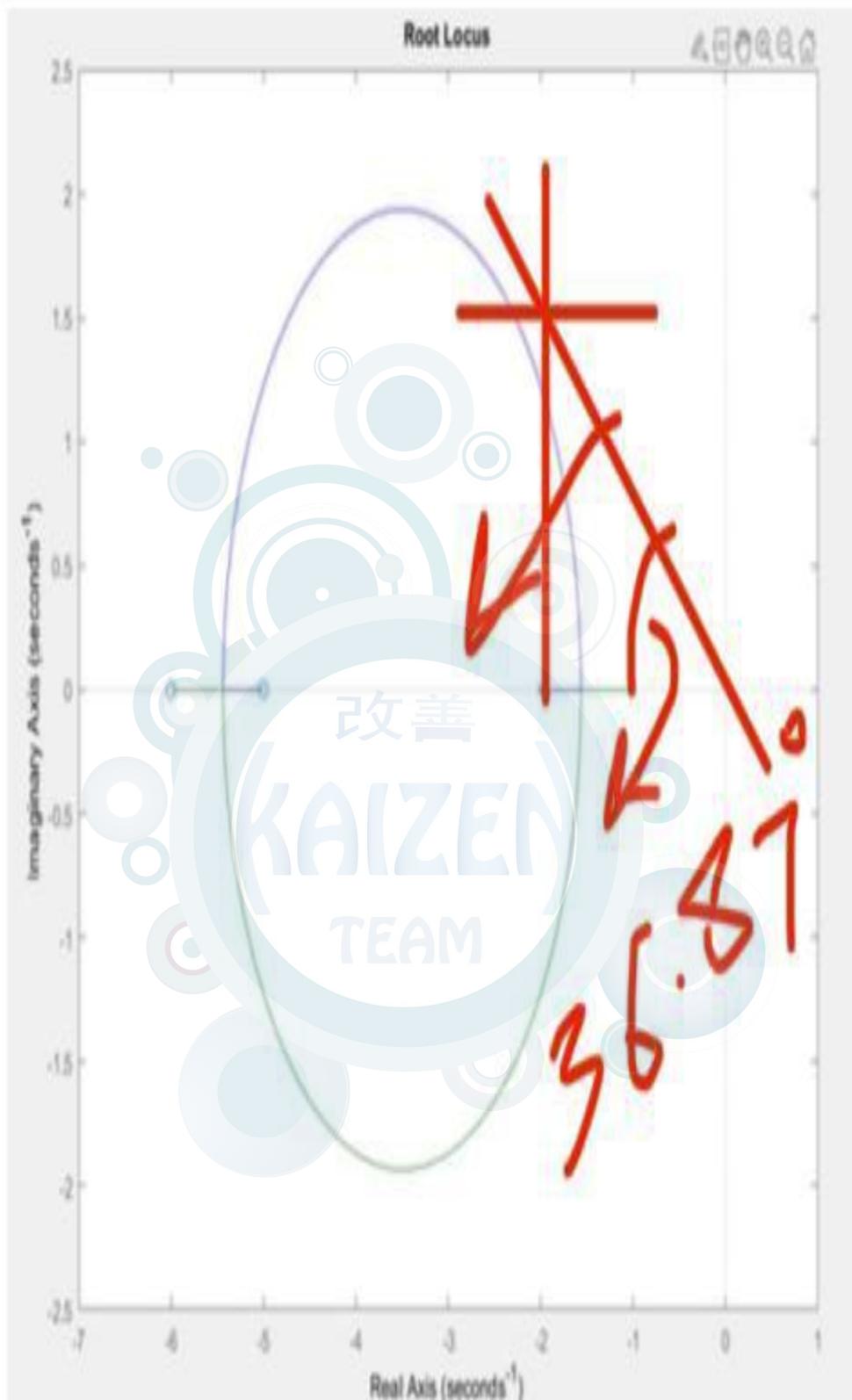
satisfy  
the  
Constraint

$$\text{改善} \frac{(S+5)(S+6)}{(S+1)(S+2)}$$

KAIZEN  
TEAM

Q2) a) For the following system  $G = \frac{(s+5)(s+6)}{(s+1)(s+2)}$ ,  $H=1$  design the feedback controller  $k$  to achieve a damping ratio of  $> 0.8$ . (you must use the root locus figure below) (7.5 points)





45.57

Name

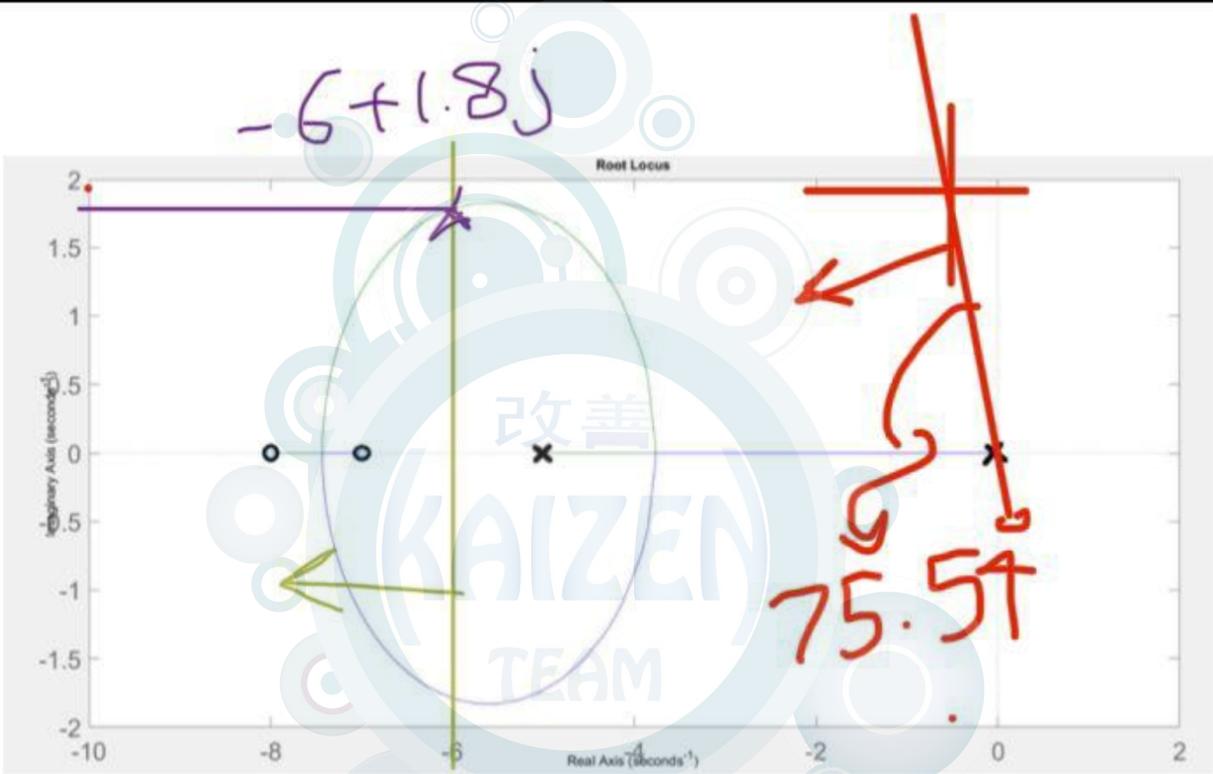
ID

A

For the following system determine K that achieves a damping ratio of  $> 0.7$  and settling time  $< 2$  s

$$GH(s) = \frac{(s+1)}{(s^2 + 3s + 10)}$$

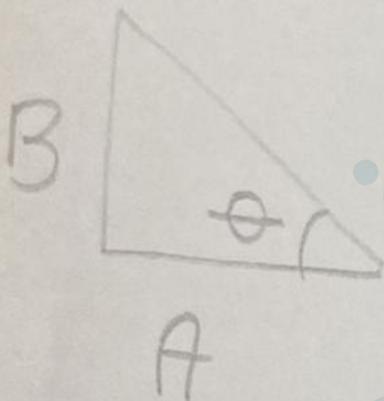




$$\xi > 0.7$$

$$\theta = \cos^{-1} 0.7 = 45.57^\circ$$

$$\tan \theta = 1.02 = \frac{B}{A} \quad 1.02$$



改善  
we want under  
the line  
KAIZEN  
TEAM

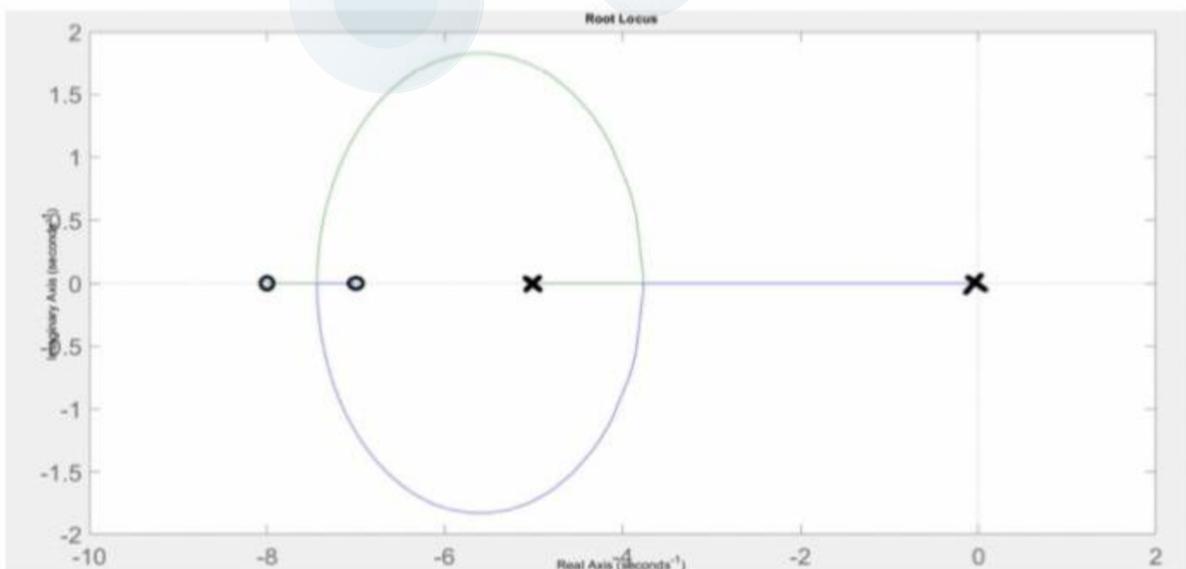
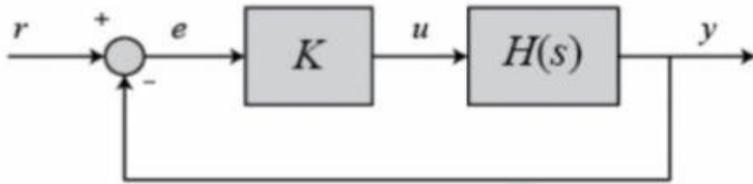
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$$T_s < 2$$

$$\frac{4}{\omega \xi} = 2 \quad \omega \xi = 2$$

Not possible !!

Q6) What is the ) a) For the following system  $H(s) = \frac{(s+7)(s+8)}{s(s+5)}$  design the feedback controller  $k$  to achieve settling time  $< 0.666$ . (you must use the root locus figure below) (5 points)



extra

$$PO\% \leq 25\%$$

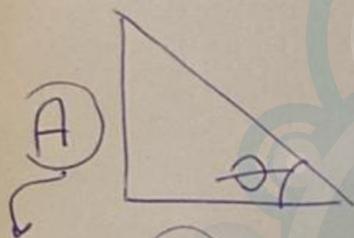
$$0.25 = \exp \frac{-\pi \xi}{\sqrt{1-\xi^2}}$$

$$\xi = 0.404$$

$$\theta = \cos^{-1} 0.404$$

$$\theta = 75.54^\circ$$

$$\tan \theta = 3.88 = \frac{A}{B}$$



$$1.94 \text{ (B)} \rightarrow \text{if } 0.5$$

$$10 \rightarrow 0.5$$

$$? \quad 0.44$$

$$? = 8.8$$

We want below

the line

$$10 \rightarrow 0.5$$
$$6 \quad ?$$

$$T_s < 0.666$$

$$\frac{4}{\omega \xi} = 0.666$$

$$\omega \xi = 6$$

We want to  
the left  
of the line

$$s = -6 + 1.8j$$

$$k \frac{(s+7)(s+8)}{s(s+5)} = 1$$

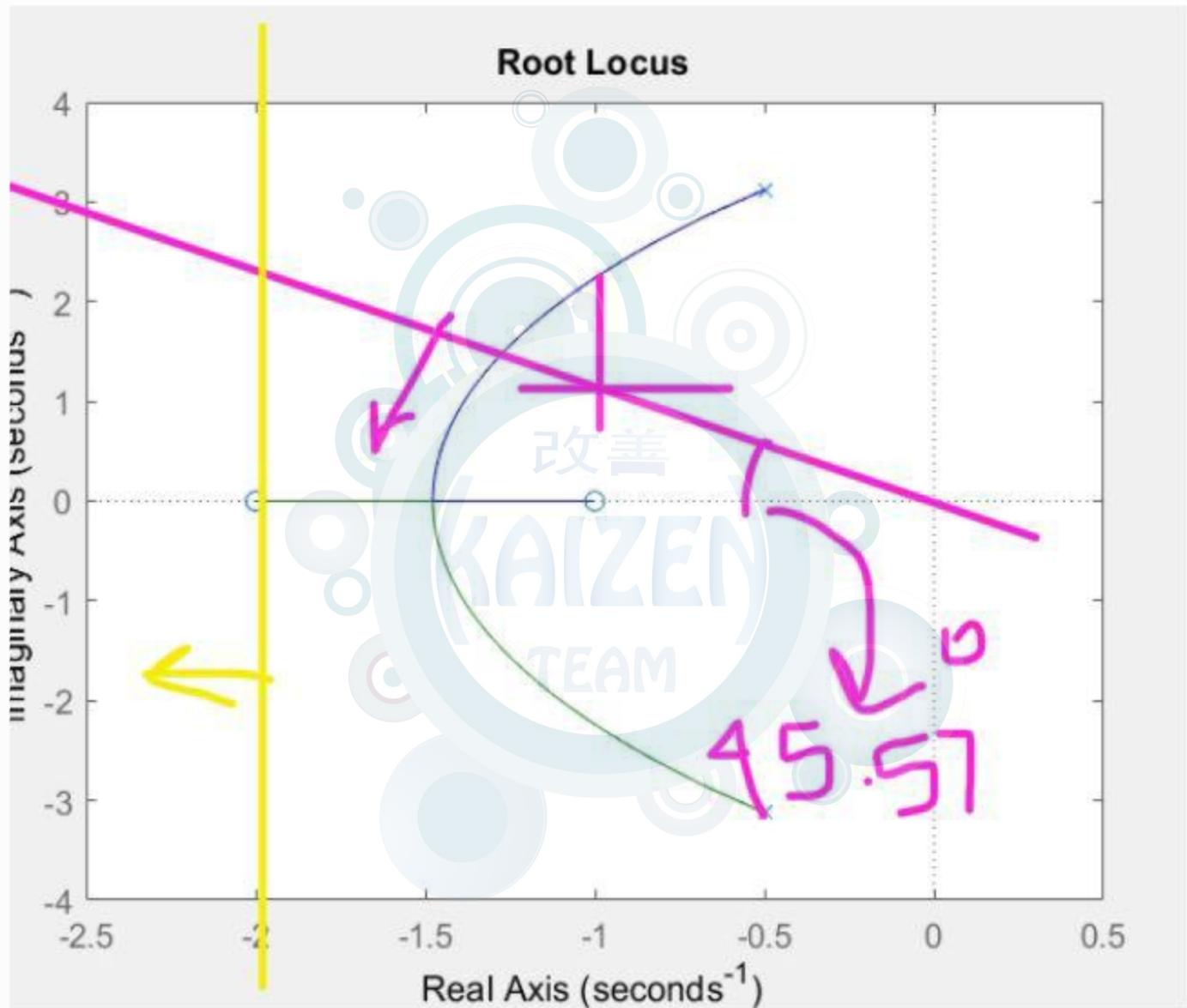
$$k = 2.33$$

$$k = 2.33$$

$$k = 72.33$$

following system determine K that achieves a damping ratio of  $> 0.7$  and settling time  $< 2$  s

$$(s+1)(s+2)/((s^2 + s + 10))$$

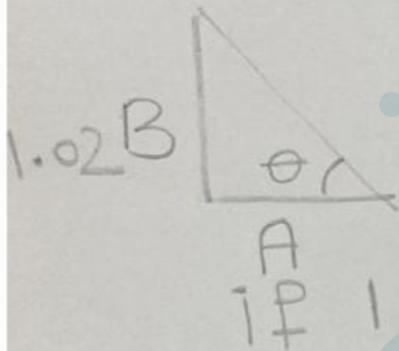


$$\xi > 0.7$$

$$\xi = 0.7$$

$$\theta = \cos^{-1} 0.7 \\ = 45.57^\circ$$

$$\tan \theta = 1.02 = \frac{B}{A}$$



we want  
bellow the  
line

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our point  $\rightarrow$

$$s = -2.33 + 2.5j$$

$\rightarrow$  substitute  
into equation

$$\left. \begin{array}{l} 10 \rightarrow 1 \\ ? \end{array} \right\} 0.02$$

$$t_s < 2$$

$$\frac{4}{\omega \xi} = 2$$

$$\boxed{\omega \xi = 2}$$

we want  
the left  
of the  
line

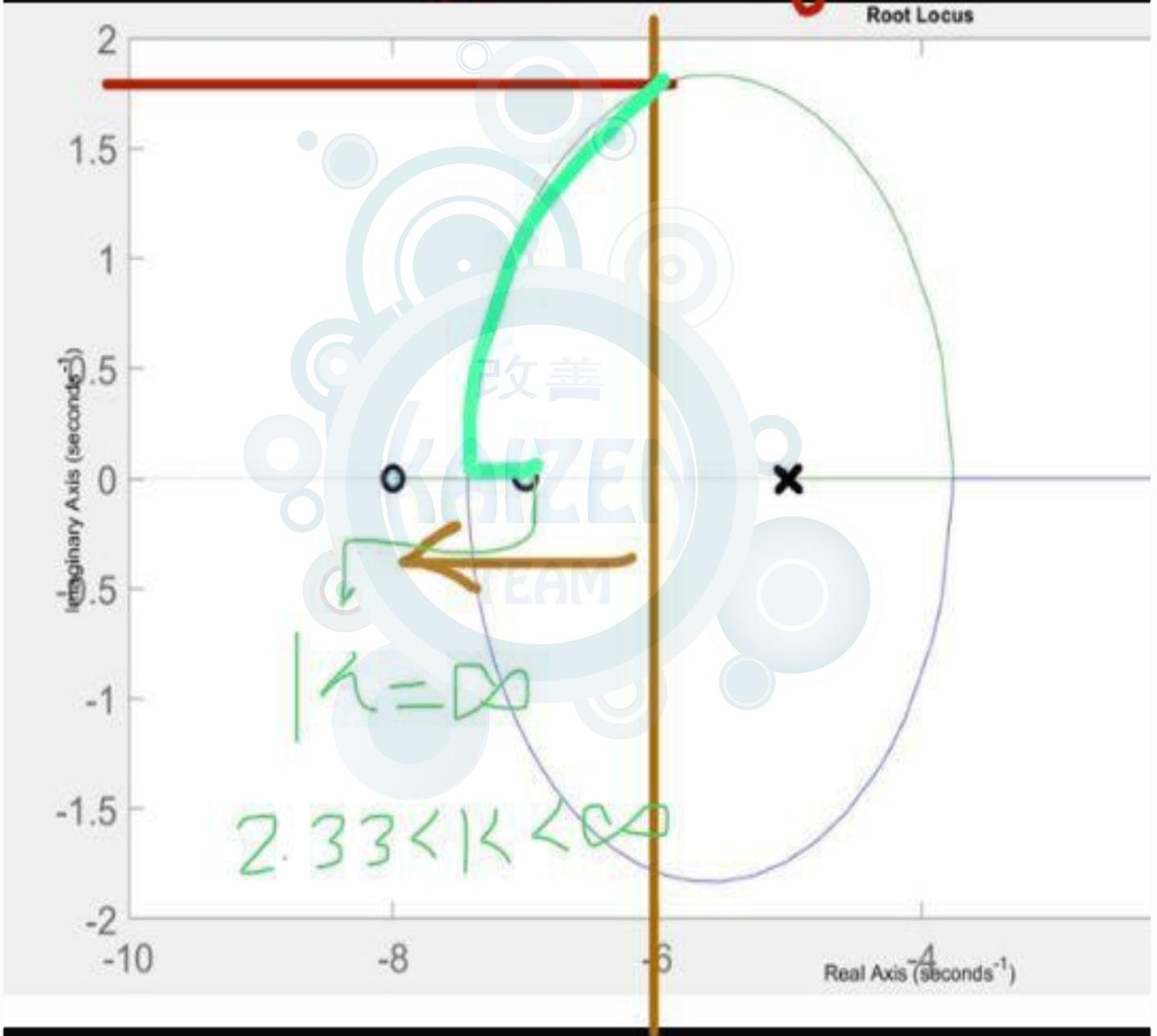
$$\left. \begin{array}{l} 15 \rightarrow 1 \\ 5 \end{array} \right\} ?$$

$$\frac{k(s+1)}{s^2+3s+10} = 1$$

$$k > 1.66$$

$$|k| = 2.33$$

$$-6 + 1.8j$$



45.57

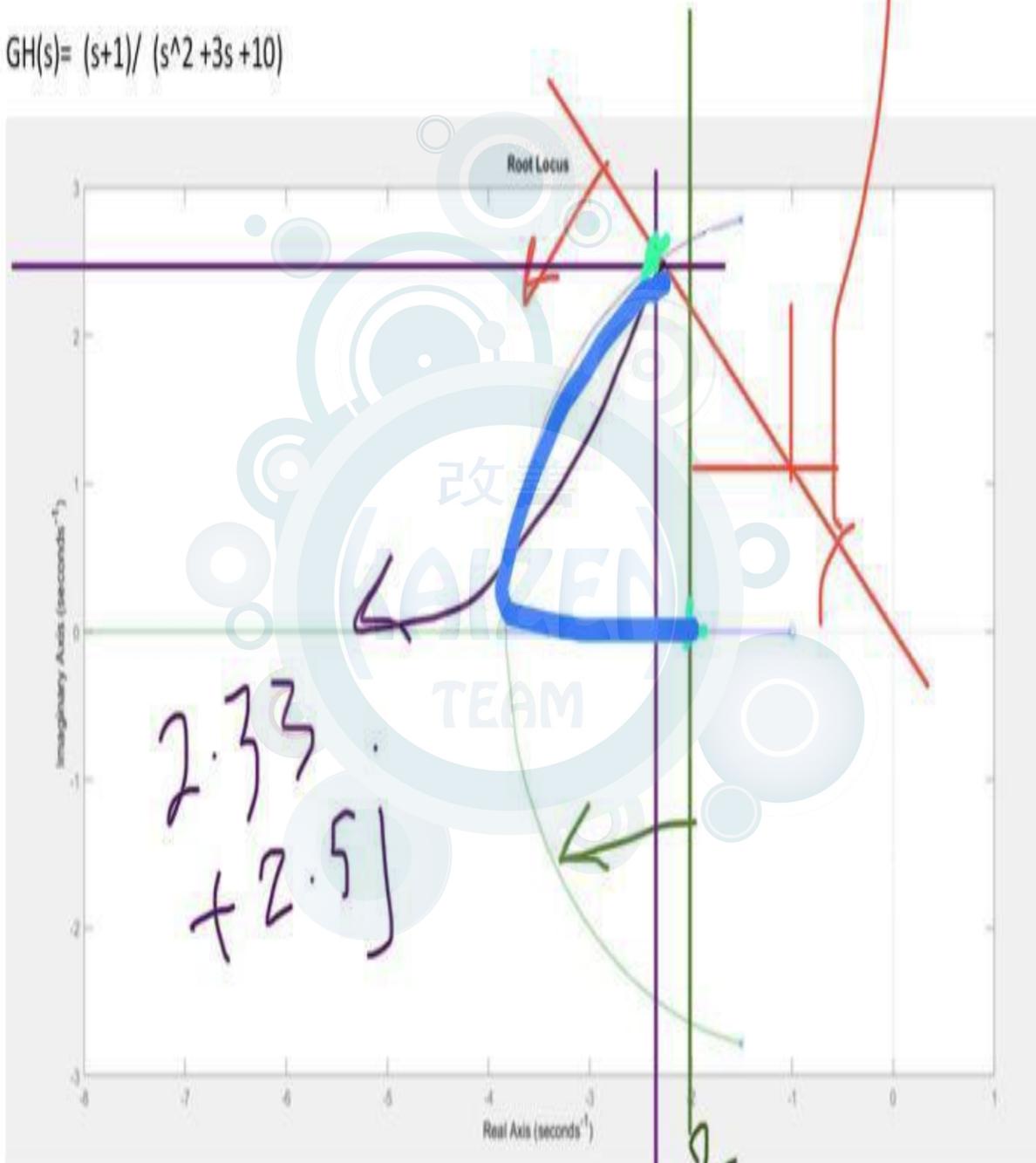
Name

ID

A

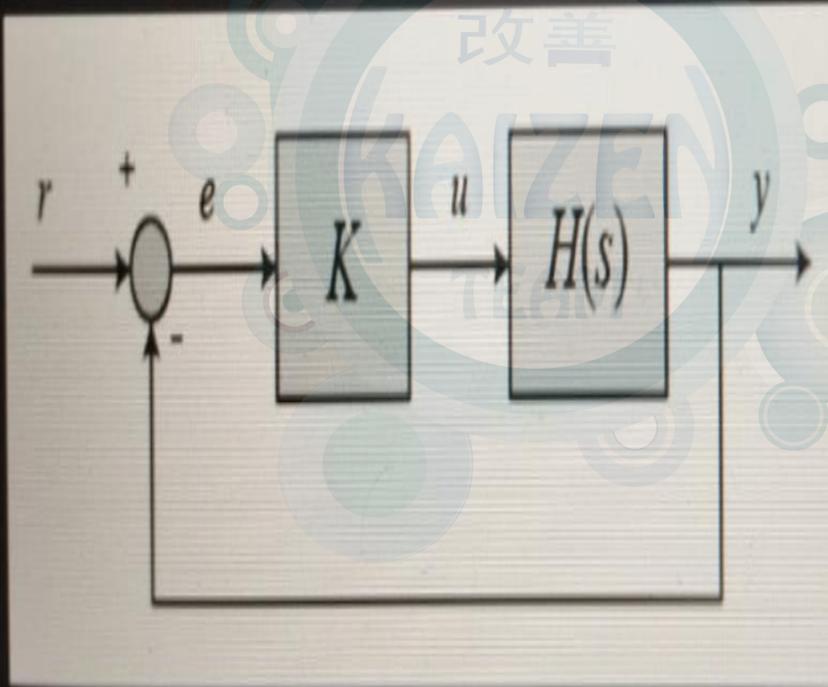
For the following system determine K that achieves a damping ratio of  $> 0.7$  and settling time  $< 2$  s

$$GH(s) = \frac{(s+1)}{(s^2 + 3s + 10)}$$



Q6) What is the ) a) For the following system  $H(s) = \frac{(s+7)(s+8)}{s(s+5)}$  design the

feedback controller  $k$  to achieve settling time  $< 0.666$ . (you must use the root locus figure below) (5 points)



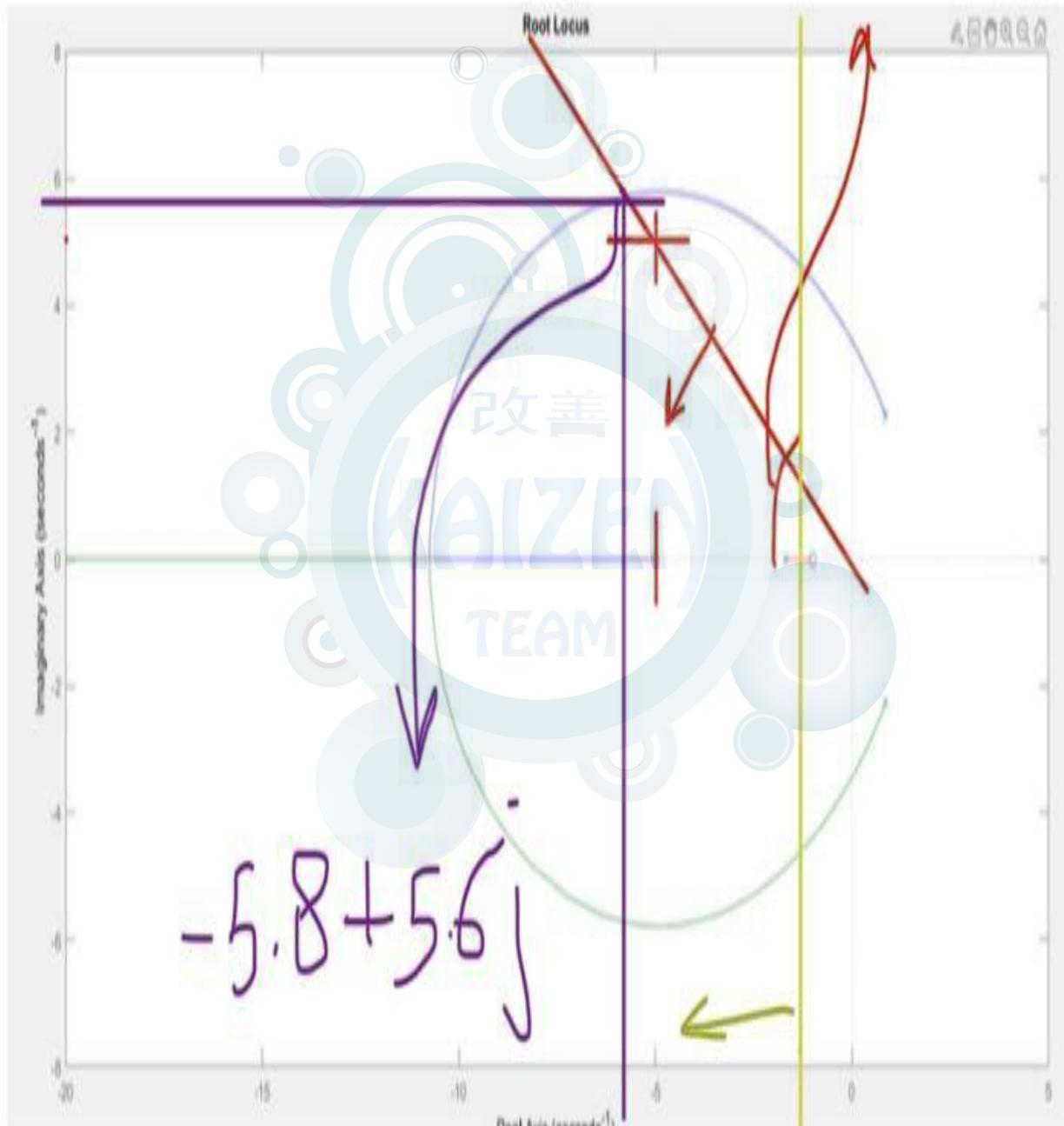
Name

ID

For the following system determine K that achieves a damping ratio of  $> 0.7$  and settling time  $< 3$  s

$$GH(s) = \frac{(s+1)(s+2)}{(s^3 + 3s + 10)}$$

$45.57^\circ$

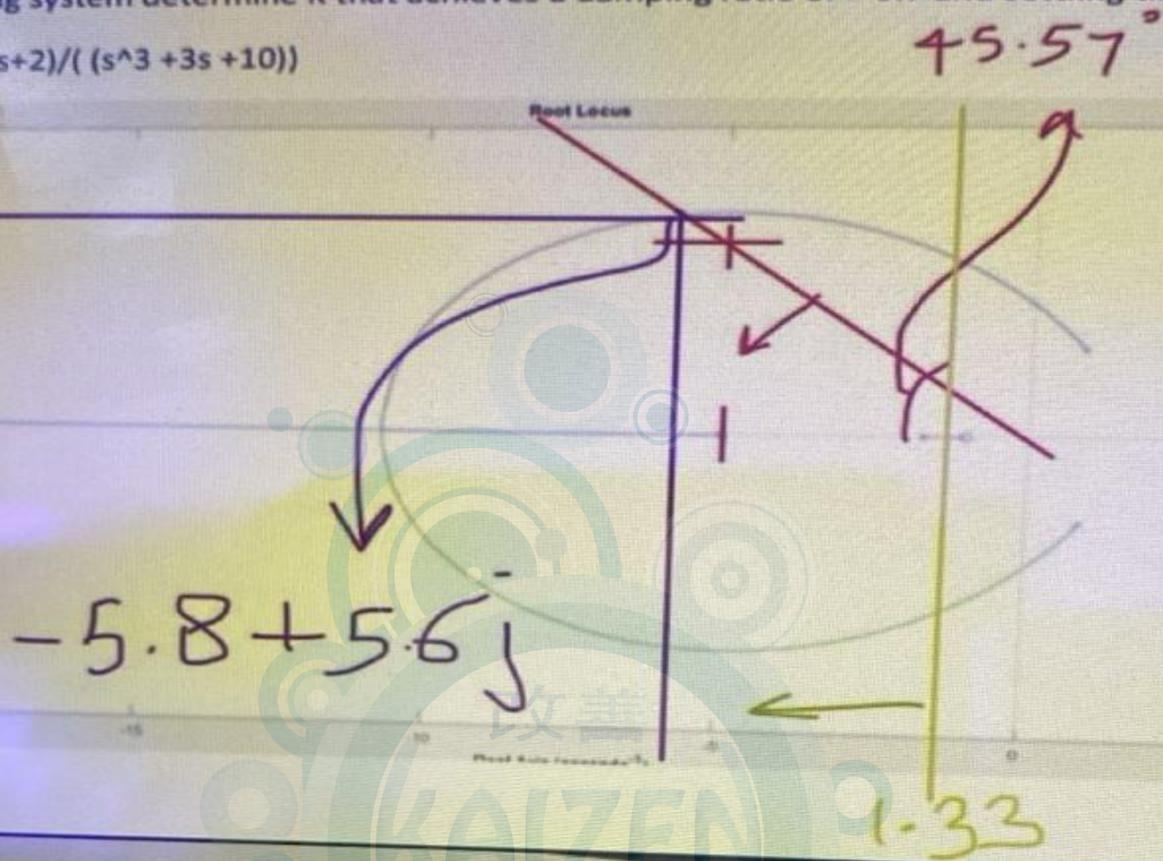


$-5.8 + 5.6j$

1.33

Following system determine K that achieves a damping ratio of  $> 0.7$  and settling time  $< 3$  s

$$(s+1) * (s+2) / ((s^3 + 3s + 10))$$



$$-5.8 + 5.6j$$

$$45.57^\circ$$

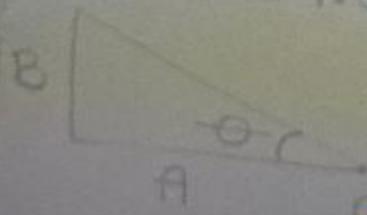
$$1.33$$

$$\zeta = 0.7$$

$$\theta = \cos^{-1} 0.7$$

$$= 45.57^\circ$$

$$\tan \theta = 1.02 = \frac{B}{A}$$



if we assumed



$$A = 5$$

B will be 5.1

for

$$\zeta > 0.7$$

we will take

the Area

under the line

Quiz 8 Industrial control systems

Prof M. Barghash IE Dept Sch of Eng UoJ 22/8/2023

Name:

ID:

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write MATLAB code using ODE45 to solve the following differential equations

$$\ddot{x} + x = \log(t), \quad \dot{x}(0) = 0, x(0) = 0$$

Plot(y) and plot(x) on same figure for a time interval 0 to 20 seconds.

Quiz control 5/1/2025

Name \_\_\_\_\_

ID \_\_\_\_\_

Model the following and find the transfer function

For the following write the control system tool box to find the rootlocus and step response

$$G = \frac{1}{(s+3)(s^2+2)}$$

num = [1];  
den = conv([1 3], [1 0 2]);  
g = tf(num, den);  
rlocus(g)  
step(g)

Quiz control 5/1/2025

Name

ID

Model the following and find the transfer function

For the following write the control system tool box to find

$$G = \frac{1}{(s^2 + 2s + 7)}$$

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num=1;

den=[1 2 7];

g=tf(num,den);

rls=step(g);

step(g)

