

Q2(13p). A gear-reduction unit uses the countershaft depicted in the figure. Find the two bearing reactions. The bearings are to be angular-contact ball bearings, having a desired life of 50 kh when used at 400 rev/min. Use 1.2 for the application factor and a reliability goal for the bearing pair of 0.98.

a-Select the bearings from Table 11-2.

$$R = \sqrt{0.98} = 0.99$$

$$T = 10(180 \cos 40) = -1378.9 \text{ lbf}\cdot\text{in}$$

$$T_1 + T_2 = 0$$

$$F = 1378.9 / 5 \cos 25 = 304.28 \text{ lbf}$$

$$\sum M_O^z = -12(180 \sin 40) - 26(304.28 \sin 25) + 36R_C^y = 0$$

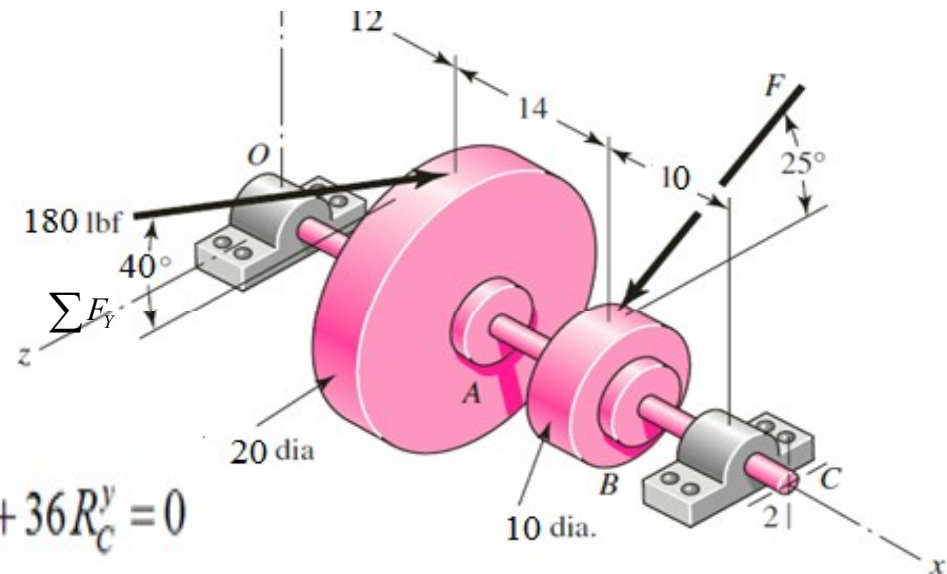
$$R_C^y = 131.4$$

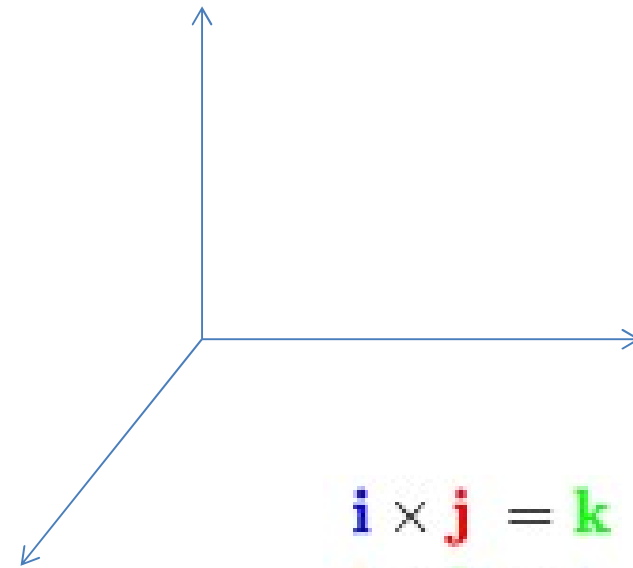
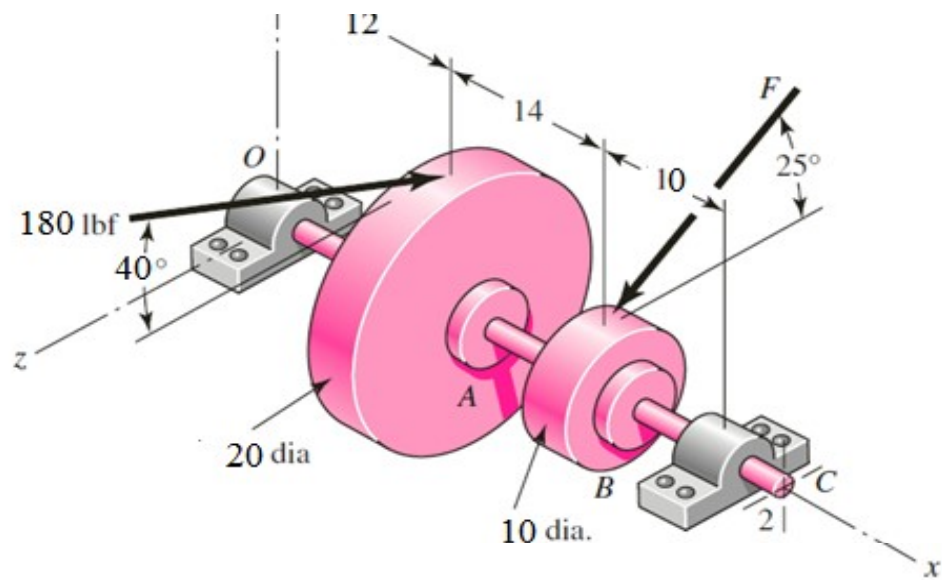
$$\sum F_y = 0$$

$$R_C^y - 180 \sin 40 - F \sin 25 + R_O^y = 0$$

$$R_O^y = 112.86$$

$$\sum M_O^y = 12(180 \cos 40) - 26(F \cos 25) - 36R_C^z = 0$$





$$\mathbf{i} \times \mathbf{j} = \mathbf{k}$$

$$\mathbf{j} \times \mathbf{k} = \mathbf{i}$$

$$\mathbf{k} \times \mathbf{i} = \mathbf{j}$$

$$R_c^z = -153.2$$

$$R_o^z = F \cos 25 - 180 \cos 40 - 153.2 = 15.136$$

$$R_o = 15.1^2 + 112.86^2 = 114$$

$$R_c = 153.2^2 + 131.4^2 = 201.8$$

$$\left| x = \frac{L}{L_{10}} \right. \quad x_D = \frac{50000(400)(60)}{10^6} = 1200$$

$$C_{10} = a_f F_D \left[ \frac{x_D}{x_0 + (\theta - x_0)(\ln 1/R_D)^{1/b}} \right]^{1/a} \quad (11-6)$$

$$C_{10} = (1.2)(201.8) \left[ \frac{1200}{0.02 + 4.439 (1-0.99)^{1/1.483}} \right]^{1/3}$$

$$C_{10} = 242.16 \left[ \frac{1200}{0.02 + 4.439 (0.0448)} \right]^{1/3}$$

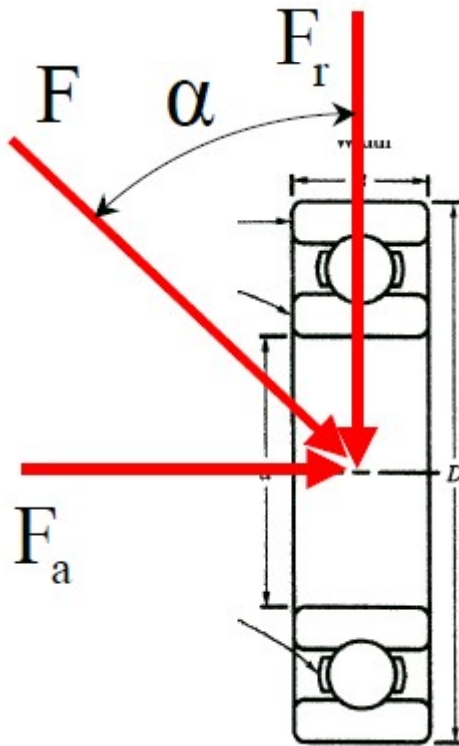
$$C_{10} = 242.16 \left[ 5484.46 \right]^{1/3}$$

$$C_{10} = 18.9 \text{ kN}$$

| Bore,<br>mm | OD,<br>mm | Width,<br>mm | Fillet<br>Radius,<br>mm | Shoulder     |       | Load Ratings, kN |       |                 |       |
|-------------|-----------|--------------|-------------------------|--------------|-------|------------------|-------|-----------------|-------|
|             |           |              |                         | Diameter, mm |       | Deep Groove      |       | Angular Contact |       |
|             |           |              |                         | $d_s$        | $d_H$ | $C_{10}$         | $C_0$ | $C$             | $C_0$ |
| 10          | 30        | 9            | 0.6                     | 12.5         | 27    | 5.07             | 2.24  | 4.94            | 2.12  |
| 12          | 32        | 10           | 0.6                     | 14.5         | 28    | 6.89             | 3.10  | 7.02            | 3.05  |
| 15          | 35        | 11           | 0.6                     | 17.5         | 31    | 7.80             | 3.55  | 8.06            | 3.65  |
| 17          | 40        | 12           | 0.6                     | 19.5         | 34    | 9.56             | 4.50  | 9.95            | 4.75  |
| 20          | 47        | 14           | 1.0                     | 25           | 41    | 12.7             | 6.20  | 13.3            | 6.55  |
| 25          | 52        | 15           | 1.0                     | 30           | 47    | 14.0             | 6.95  | 14.8            | 7.65  |
| 30          | 62        | 16           | 1.0                     | 35           | 55    | 19.5             | 10.0  | 20.3            | 11.0  |
| 35          | 72        | 17           | 1.0                     | 41           | 65    | 25.5             | 13.7  | 27.0            | 15.0  |
| 40          | 80        | 18           | 1.0                     | 46           | 72    | 30.7             | 16.6  | 31.9            | 18.6  |
| 45          | 85        | 19           | 1.0                     | 52           | 77    | 33.2             | 18.6  | 35.8            | 21.2  |
| 50          | 90        | 20           | 1.0                     | 56           | 82    | 35.1             | 19.6  | 37.7            | 22.8  |
| 55          | 100       | 21           | 1.5                     | 63           | 90    | 43.6             | 25.0  | 46.2            | 28.5  |
| 60          | 110       | 22           | 1.5                     | 70           | 99    | 47.5             | 28.0  | 55.9            | 35.5  |
| 65          | 120       | 23           | 1.5                     | 74           | 109   | 55.9             | 34.0  | 63.7            | 41.5  |
| 70          | 125       | 24           | 1.5                     | 79           | 114   | 61.8             | 37.5  | 68.9            | 45.5  |
| 75          | 130       | 25           | 1.5                     | 86           | 119   | 66.3             | 40.5  | 71.5            | 49.0  |
| 80          | 140       | 26           | 2.0                     | 93           | 127   | 70.2             | 45.0  | 80.6            | 55.0  |

## 11-6 Combined Radial and Thrust Loading

- ❖ Bearings are usually operated with some combination of radial and thrust load.
- ❖ Catalog ratings are based only on radial loads. Follow the guideline in catalogs to obtain the equivalent radial load.
- ✓ **In order to choose the bearing, an equivalent radial load  $F_e$  must be found**



## How to handle combined loading

- What about combined radial,  $F_r$ , and axial loading,  $F_a$ ?
  - Use an equivalent load,  $F_e$ , that does the same amount of damage.

$$F_e = X_i V F_r + Y_i F_a$$

- Where  $V = 1.2$  for outer ring rotation and 1 for inner ring
  - This has to do with the fact that outer ring fails more often
- $X_i$  and  $Y_i$  are a function of the
  - Axial load,  $F_a$
  - Static load rating,  $C_o$

$$C_0 = Mn_b d_b^2 \dots\dots (\text{ball\_bearings})$$

$$C_0 = Mn_r l_c d \dots\dots (\text{roller\_bearings})$$

where

$$C_0 = \text{bearing\_static\_load\_rating\_}(lbf, kN)$$

$$n_b = \text{no.\_of\_balls}$$

$$n_r = \text{no.\_of\_rollers}$$

$$d_b = \text{diameter\_of\_balls\_}(in., mm)$$

$$d = \text{diameter\_of\_rollers\_}(in., mm)$$

$$l_c = \text{length\_of\_contact\_line\_}(in., mm)$$

**M is specified as given in this table.**

| <b>M</b>      | <b>in and lbf</b> | <b>mm and kN</b> |
|---------------|-------------------|------------------|
| Radial ball   | $1.78(10)^3$      | $5.11(10)^3$     |
| Ball thrust   | $7.10(10)^3$      | $20.4(10)^3$     |
| Radial roller | $3.13(10)^3$      | $8.99(10)^3$     |
| Roller thrust | $14.2(10)^3$      | $40.7(10)^3$     |

A ball bearing is capable of resisting radial loading and a thrust loading. These can be combined.

- $F_a$  = the axial thrust load.
- $F_r$  = the radial load.
- $F_e$  = equivalent radial load that does the same damage as the combined radial and thrust loads together.
- The abscissa  $e$  is defined by the intersection of the two lines.

$$\frac{F_e}{VF_r} = 1, \frac{F_a}{VF_r} \leq e$$

$$\frac{F_e}{VF_r} = X + Y \frac{F_a}{VF_r} \Rightarrow \frac{F_a}{VF_r} > e,$$

$$F_e = X_i VF_r + Y_i F_a$$

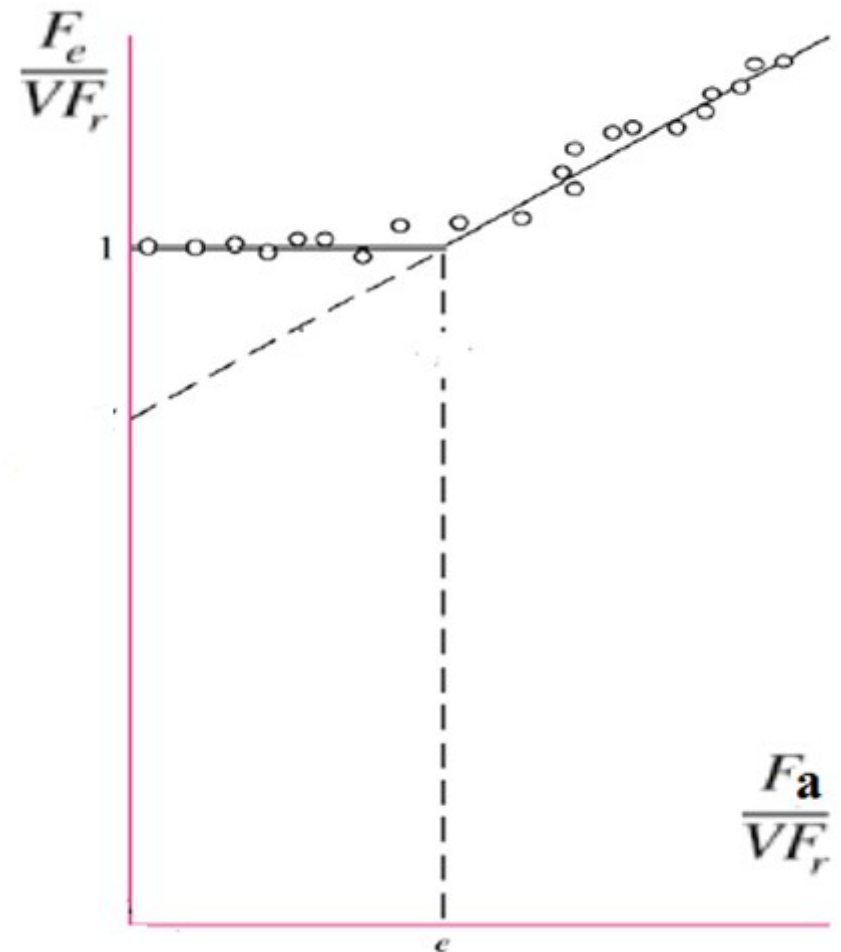
Where  $i=1$  when  $F_a/VF_r < e$

$i=2$  when  $F_a/VF_r > e$

$V=1$  when the inner ring rotates

$V=1.2$  when the outer ring rotates

$X$  > the intercept of the line with vertical





| $F_a/C_0$ | $e$  | $F_a/(VF_r) \leq e$ |       | $F_a/(VF_r) > e$ |       |
|-----------|------|---------------------|-------|------------------|-------|
|           |      | $X_1$               | $Y_1$ | $X_2$            | $Y_2$ |
| 0.014*    | 0.19 | 1.00                | 0     | 0.56             | 2.30  |
| 0.021     | 0.21 | 1.00                | 0     | 0.56             | 2.15  |
| 0.028     | 0.22 | 1.00                | 0     | 0.56             | 1.99  |
| 0.042     | 0.24 | 1.00                | 0     | 0.56             | 1.85  |
| 0.056     | 0.26 | 1.00                | 0     | 0.56             | 1.71  |
| 0.070     | 0.27 | 1.00                | 0     | 0.56             | 1.63  |
| 0.084     | 0.28 | 1.00                | 0     | 0.56             | 1.55  |
| 0.110     | 0.30 | 1.00                | 0     | 0.56             | 1.45  |
| 0.17      | 0.34 | 1.00                | 0     | 0.56             | 1.31  |
| 0.28      | 0.38 | 1.00                | 0     | 0.56             | 1.15  |
| 0.42      | 0.42 | 1.00                | 0     | 0.56             | 1.04  |
| 0.56      | 0.44 | 1.00                | 0     | 0.56             | 1.00  |

\*Use 0.014 if  $F_a/C_0 < 0.014$ .

Ex: An SKF 6210 angular-contact ball bearing ( $a=3$ ) has an axial load  $F_a$  of 1.8 kN applied, a radial load  $F_r$  of 2.2 kN applied with the outer ring stationary. The basic static load rating  $C_0$  is 19.8 kN and the basic load rating  $C_{10}$  is 35 kN.

Estimate the  $L_D$  life at a speed of 720 r/min.

$$V=1 \text{ and } F_a/C_0=1.8/19.8=0.09$$

Interpolate for  $e$  in Table 11-1;  $e=0.285$

$$\text{since } F_a/(VF_r)=1.8/[(1)2.2]=0.818$$

Interpolate  $Y_2$  we get  $Y_2=1.527$

$$F_e=X_2VF_r+Y_2F_a=0.56(1)2.2+1.527(1.8)=3.96 \text{ kN}$$

$$C_{10}L_{10}^{1/a} = F L^{1/a}$$

$$L_D = \frac{60L_R n_R}{60n_D} \left( \frac{C_{10}}{F_e} \right)^3 = \frac{10^6}{60(720)} \left( \frac{35}{3.96} \right)^3 = 15982h$$

## Bearing Specifications

Bearings are defined by a two digit number: **dimension-series code**

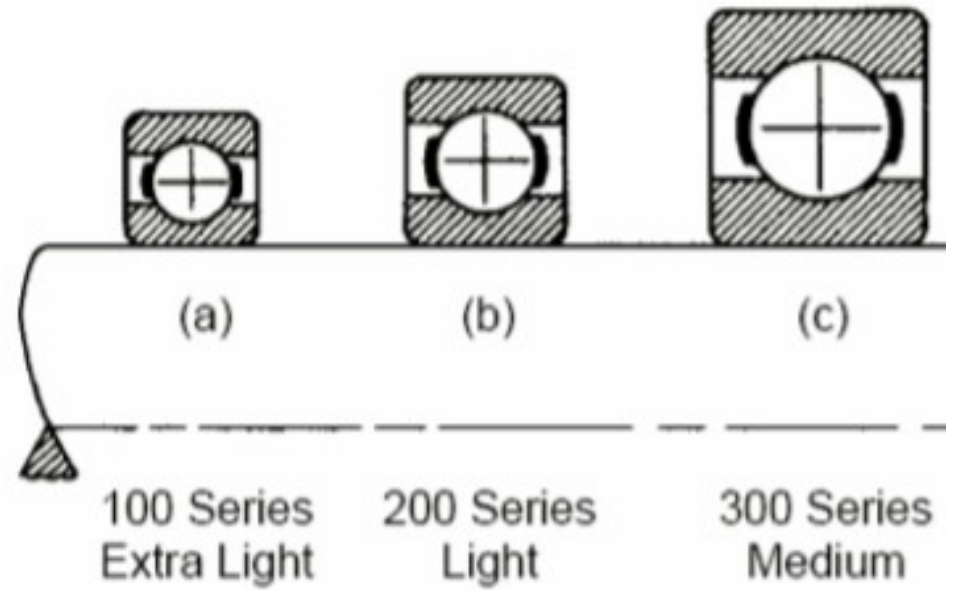
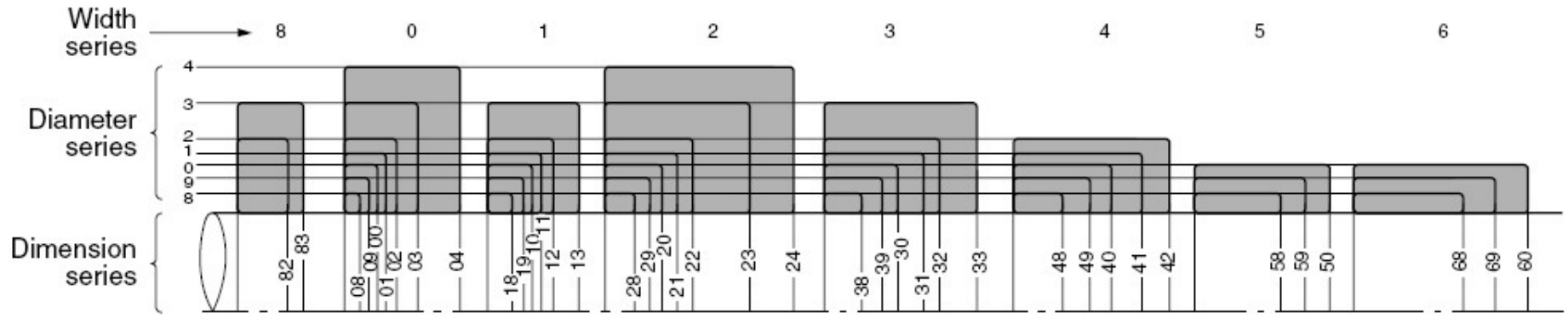
First number is the width series, 0,1,2,3,4,5 and 6

|  | Dimension series |  |                                    |                                      |
|--|------------------|--|------------------------------------|--------------------------------------|
|  |                  | Diameter series<br>(outer diameter dimensions) | Width series<br>(width dimensions) | Height series<br>(height dimensions) |
| Radial bearings<br>(excluding tapered roller bearings) | number           | 7, 8, 9, 0, 1, 2, 3, 4                         | 8, 0, 1, 2, 3, 4, 5, 6             | _____                                |
|  | dimensions       | small $\longleftrightarrow$ large              | small $\longleftrightarrow$ large  |                                      |
| Tapered roller bearings                                | number           | 9, 0, 1, 2, 3                                  | 0, 1, 2, 3                         | _____                                |
|  | dimensions       | small $\longleftrightarrow$ large              | small $\longleftrightarrow$ large  |                                      |
| Thrust bearings  | number           | 0, 1, 2, 3, 4                                  | _____                              | 7, 9, 1, 2                           |
|  | dimensions       | small $\longleftrightarrow$ large              |                                    | small $\longleftrightarrow$ large    |

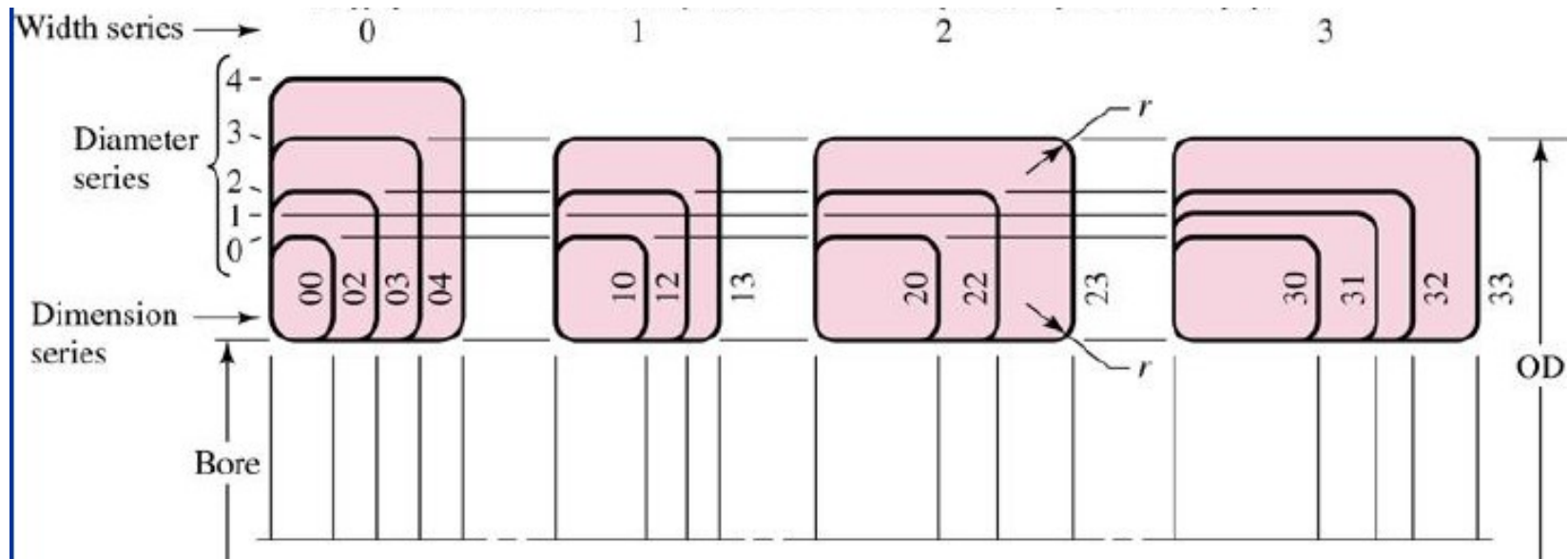
Second number is the diameter series

### Dimension series for radial bearings

# Bearing Specifications



# ABMA Boundary Dimensions

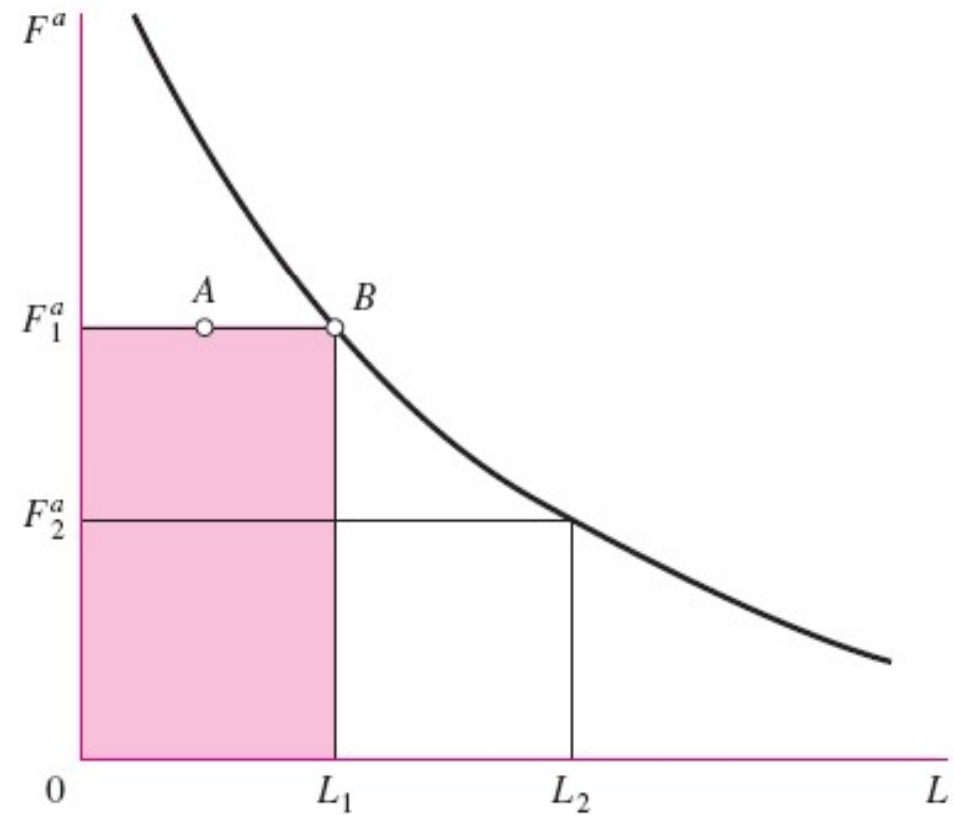


## 11-7 Variable Loading

Equation (11-1) can be written as

$$F^a L = \text{constant} = K$$

If a load level of  $F_1$  is selected and run to the failure criterion, then the area under the  $F_1$ - $L_1$  trace is numerically equal to  $K$ . The same is true for a load level  $F_2$ ; that is, the area under the  $F_2$ - $L_2$  trace is numerically equal to  $K$



load level  $F_1$ , the area from  $L = 0$  to  $L = L_A$  does damage measured by  $F^a L_A = D$ .

- Piecewise constant loading in a cyclic pattern

The damage done by loads  $F_{e1}$ ,  $F_{e2}$ , and  $F_{e3}$  is

$$D = F_{e1}^a l_1 + F_{e2}^a l_2 + F_{e3}^a l_3$$

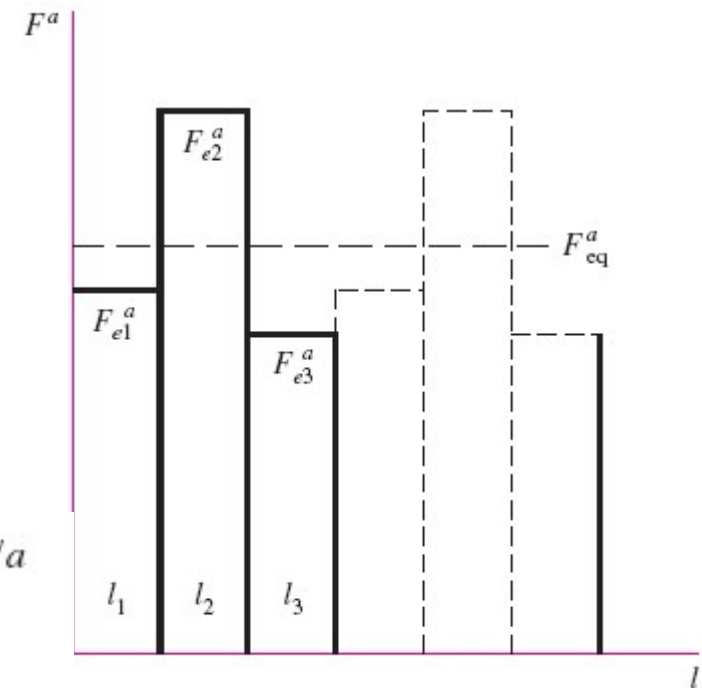
The equivalent steady load  $F_{eq}$  when run for  $l_1 + l_2 + l_3$  revolutions does the same damage  $D$ .

$$D = F_{eq}^a (l_1 + l_2 + l_3)$$

$$F_{eq} = \left[ \frac{F_{e1}^a l_1 + F_{e2}^a l_2 + F_{e3}^a l_3}{l_1 + l_2 + l_3} \right]^{1/a} = \left[ \sum f_i F_{ei}^a \right]^{1/a}$$

$f_i$  is the fraction of revolution run up under load  $F_{ei}$

$F_{ei}$  are equivalent steady radial loads for combined radial–thrust loads



Since  $li$  can be expressed as  $n_i t_i$ , where  $n_i$  is the rotational speed at load  $Fe_i$  and  $t_i$  is the duration of that speed, then it follows that

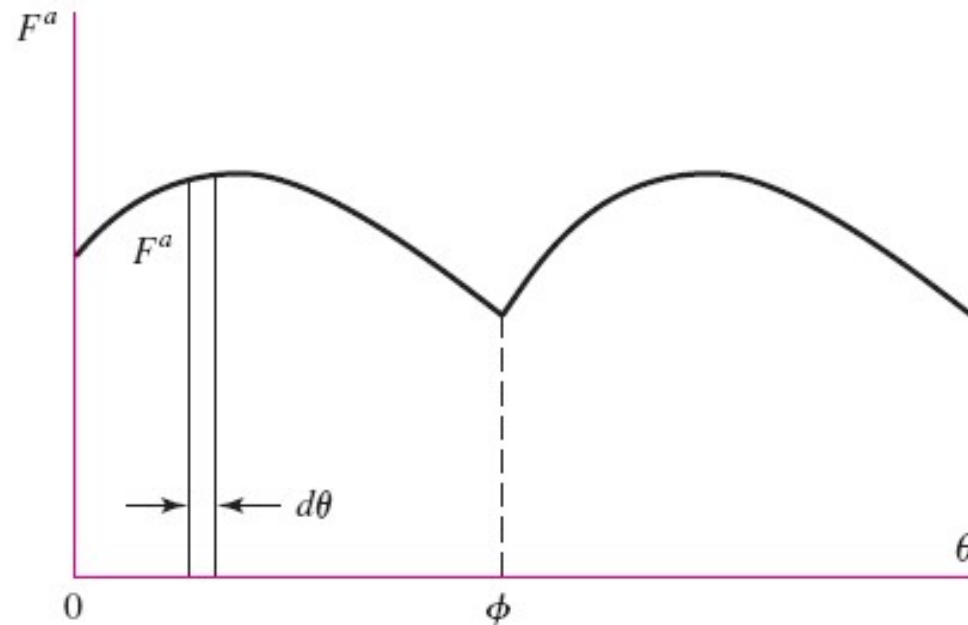
$$F_{eq} = \left[ \frac{\sum n_i t_i F_{ei}^a}{\sum n_i t_i} \right]^{1/a}$$

The character of the individual loads can change, so an application factor ( $a_f$ ) can be prefixed to each  $Fe_i$  as  $(a_{fi} Fe_i)^a$ ;

$$F_{eq} = \left[ \sum f_i (a_{fi} Fe_i)^a \right]^{1/a} \quad L_{eq} = \frac{K}{F_{eq}^a}$$



- Continuously variable loading in a repeatable cyclic pattern



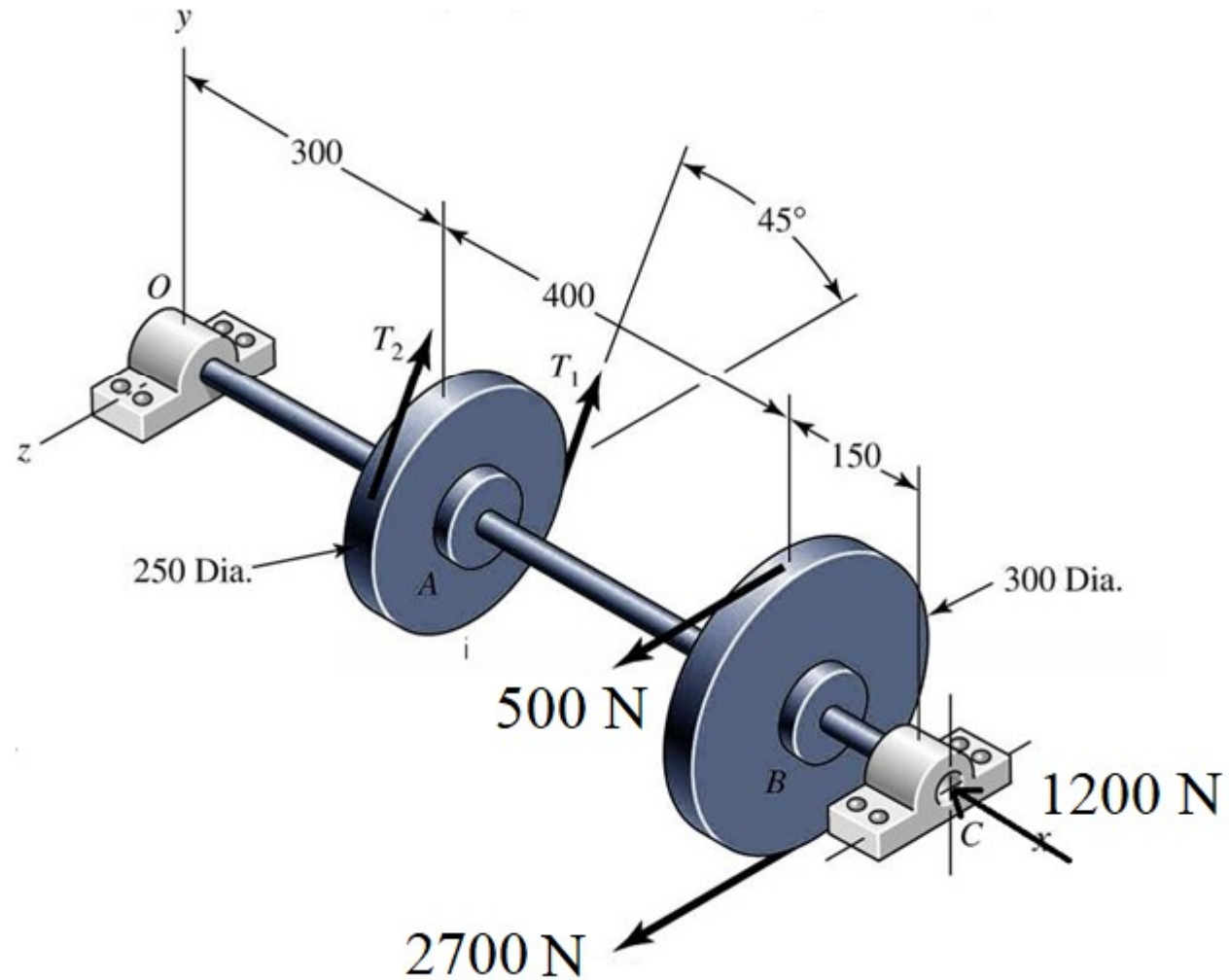
$$F_{\text{eq}} = \left[ \frac{1}{\phi} \int_0^{\phi} F^a d\theta \right]^{1/a} \quad L_{\text{eq}} = \frac{K}{F_{\text{eq}}^a}$$

## Selection of ball and cylindrical roller bearing

This selection procedure contains an iterative process:

- Choose  $Y_2$  from Table 11-1
- Find  $C_{10}$
- Tentatively identify a suitable bearing 11-2, note  $C_o$
- Using  $F_a/C_o$  enter Table 11-1 to obtain a new value of  $Y_2$
- If the same bearing is obtained, stop
- If not, take next bearing and go to step 4.

**Ex:** The figure is a schematic drawing of a countershaft that supports two V- belt pulleys (they are hold in place using keys)The countershaft runs at 1200r/min and the bearings are to have a life of 10 kh at a combined reliability of 0.98. for the Weibull parameters are  $b=1.483$ ,  $X_0= 0.2$ ,  $\theta=4.439+0.2$ . The application factor is to be 1.2. The belt tension on the loose side of pulley A is 15 percent of the tension on the tight side.



$$\sum T = (2700-500) * 150 - (T_1 - 0.15T_1) * 125 = 0$$

$$T_1 = 3106 \text{ N}$$

$$T_2 = 466 \text{ N}$$

$$\sum M_O^Z = 1.15 \times 3106 \times 300 \times \sin 45 + R_C^Y \times 850 = 0$$

$$R_C^Y = -891 \text{ N}$$

$$\sum M_O^Y = -(2700+500) * 700 + (1.15T_1) \times 300 \times \cos 45 + R_C^Z \times 850 = 0$$

$$R_C^Z = 1744 \text{ N}$$

$$\sum F_y = -891 + 1.15 \times 3106 \times \sin 45 + R_O^Y = 0$$

$$R_O^Y = -1634.7 \text{ N}$$

$$\sum F_z = (2700+500) - (1.15T_1) \cos 45 + R_O^Z + 1744 = 0$$

$$R_O^Z = 2418.3 \text{ N}$$

$$F_O = \sqrt{\quad + \quad} = 2918.97 \text{ N}$$

$$F_C = \sqrt{1744^2 + 891^2} = 1958.4 \text{ N}$$

with  $V=1$

$$\frac{F_e}{VF_r} = X + \frac{Y}{V} \frac{F_a}{F_r} = 0.56 + 1.63 \frac{1200}{(1)1958.6} = 1.56$$

$$F_e = 1.56VF_r = 1.56(1)1958.6 = 3052.8\text{N}$$

$$C_{10} = 1.2 * 3.052 \left[ \frac{393.2}{0.02 + 4.439(1 - 0.99)^{1/1.483}} \right]^{1/3} =$$

$$1.2 * 3.052(12.15) = 44.52 \text{ kN}$$

**Table 11-2**

Dimensions and Load Ratings for Single-Row 02-Series Deep-Groove and Angular-Contact Ball Bearings

| Bore,<br>mm | OD,<br>mm | Width,<br>mm | Fillet<br>Radius,<br>mm | Shoulder              |       | Load Ratings, kN |       |                 |       |
|-------------|-----------|--------------|-------------------------|-----------------------|-------|------------------|-------|-----------------|-------|
|             |           |              |                         | Diameter, mm<br>$d_S$ | $d_H$ | Deep Groove      |       | Angular Contact |       |
|             |           |              |                         |                       |       | $C_{10}$         | $C_0$ | $C_{10}$        | $C_0$ |
| 10          | 30        | 9            | 0.6                     | 12.5                  | 27    | 5.07             | 2.24  | 4.94            | 2.12  |
| 12          | 32        | 10           | 0.6                     | 14.5                  | 28    | 6.89             | 3.10  | 7.02            | 3.05  |
| 15          | 35        | 11           | 0.6                     | 17.5                  | 31    | 7.80             | 3.55  | 8.06            | 3.65  |
| 17          | 40        | 12           | 0.6                     | 19.5                  | 34    | 9.56             | 4.50  | 9.95            | 4.75  |
| 20          | 47        | 14           | 1.0                     | 25                    | 41    | 12.7             | 6.20  | 13.3            | 6.55  |
| 25          | 52        | 15           | 1.0                     | 30                    | 47    | 14.0             | 6.95  | 14.8            | 7.65  |
| 30          | 62        | 16           | 1.0                     | 35                    | 55    | 19.5             | 10.0  | 20.3            | 11.0  |
| 35          | 72        | 17           | 1.0                     | 41                    | 65    | 25.5             | 13.7  | 27.0            | 15.0  |
| 40          | 80        | 18           | 1.0                     | 46                    | 72    | 30.7             | 16.6  | 31.9            | 18.6  |
| 45          | 85        | 19           | 1.0                     | 52                    | 77    | 33.2             | 18.6  | 35.8            | 21.2  |
| 50          | 90        | 20           | 1.0                     | 56                    | 82    | 35.1             | 19.6  | 37.7            | 22.8  |
| 55          | 100       | 21           | 1.5                     | 63                    | 90    | 43.6             | 25.0  | 46.2            | 28.5  |
| 60          | 110       | 22           | 1.5                     | 70                    | 99    | 47.5             | 28.0  | 55.9            | 35.5  |
| 65          | 120       | 23           | 1.5                     | 74                    | 109   | 55.9             | 34.0  | 63.7            | 41.5  |
| 70          | 125       | 24           | 1.5                     | 79                    | 114   | 61.8             | 37.5  | 68.9            | 45.5  |
| 75          | 130       | 25           | 1.5                     | 86                    | 119   | 66.3             | 40.5  | 71.5            | 49.0  |
| 80          | 140       | 26           | 2.0                     | 93                    | 127   | 70.2             | 45.0  | 80.6            | 55.0  |
| 85          | 150       | 28           | 2.0                     | 99                    | 136   | 83.2             | 53.0  | 90.4            | 63.0  |
| 90          | 160       | 30           | 2.0                     | 104                   | 146   | 95.6             | 62.0  | 106             | 73.5  |
| 95          | 170       | 32           | 2.0                     | 110                   | 156   | 108              | 69.5  | 121             | 85.0  |

From Table 11-2, angular-contact bearing 02-55 mm has  $C_{10} = 46.2$  kN.  $C_0$  is 28.5 kN. Step 4 becomes, with  $F_a$  in kN,

$$\frac{F_a}{C_0} = \frac{1.2}{28.5} = 0.0421$$



which makes  $e$  from Table 11-1 approximately 0.24.

| $F_a/C_0$ | $e$  | $F_a/(VF_r) \leq e$ |       | $F_a/(VF_r) > e$ |       |
|-----------|------|---------------------|-------|------------------|-------|
|           |      | $X_1$               | $Y_1$ | $X_2$            | $Y_2$ |
| 0.014*    | 0.19 | 1.00                | 0     | 0.56             | 2.30  |
| 0.021     | 0.21 | 1.00                | 0     | 0.56             | 2.15  |
| 0.028     | 0.22 | 1.00                | 0     | 0.56             | 1.99  |
| 0.042     | 0.24 | 1.00                | 0     | 0.56             | 1.85  |
| 0.056     | 0.26 | 1.00                | 0     | 0.56             | 1.71  |
| 0.070     | 0.27 | 1.00                | 0     | 0.56             | 1.63  |
| 0.084     | 0.28 | 1.00                | 0     | 0.56             | 1.55  |
| 0.110     | 0.30 | 1.00                | 0     | 0.56             | 1.45  |
| 0.17      | 0.34 | 1.00                | 0     | 0.56             | 1.31  |
| 0.28      | 0.38 | 1.00                | 0     | 0.56             | 1.15  |
| 0.42      | 0.42 | 1.00                | 0     | 0.56             | 1.04  |
| 0.56      | 0.44 | 1.00                | 0     | 0.56             | 1.00  |

$$F_a/(VF_r) = 1200 / (1 * 1958.4) = 0.61$$

$$Y_2 = 1.85$$

$$\frac{F_e}{V F_r} = X + \frac{Y}{V} \frac{F_a}{F_r} = 0.56 + 1.85 \frac{1200}{(1)1958.6} = 1.69$$

$$F_e = 1.77 V F_r = 1.69(1)1958.6 = 3316.82$$

$$C_{10} = 1.2 * 3.316 (12.15) = 48.35 \text{ kN}$$

From table 11-2 angular contact bearing

02-60 mm has  $C_{10} = 55.9 \text{ kN}$   $C_0 = 35.5 \text{ kN}$

$$F_a / C_0 = 1200 / 35500 = 0.034$$

| $F_a/C_0$    | $e$  | $F_a/(VF_r) \leq e$ |       | $F_a/(VF_r) > e$ |       |
|--------------|------|---------------------|-------|------------------|-------|
|              |      | $X_1$               | $Y_1$ | $X_2$            | $Y_2$ |
| 0.014*       | 0.19 | 1.00                | 0     | 0.56             | 2.30  |
| 0.021        | 0.21 | 1.00                | 0     | 0.56             | 2.15  |
| 0.028        | 0.22 | 1.00                | 0     | 0.56             | 1.99  |
| <b>0.034</b> |      |                     |       |                  |       |
| 0.042        | 0.24 | 1.00                | 0     | 0.56             | 1.85  |

$$e=0.23 \quad Y_2=1.93$$

$$F_e=0.56*1*1958.6+1.93*1200=3412.82 \text{ N}$$

$$C_{10}=1.2*3.412*12.15=49.75 \text{ kN}$$

from table 11-2 an angular contact 02-60 mm is still selected

The ball bearing at *C* involves a thrust component. This selection procedure requires an iterative procedure. Assuming  $F_a/(V F_r) > e$ ,

- 1 Choose  $Y_2$  from Table 11–1.
- 2 Find  $C_{10}$ .
- 3 Tentatively identify a suitable bearing from Table 11–2, note  $C_0$ .
- 4 Using  $F_a/C_0$  enter Table 11–1 to obtain a new value of  $Y_2$ .
- 5 Find  $C_{10}$ .
- 6 If the same bearing is obtained, stop.
- 7 If not, take next bearing and go to step 4.

take the middle entry from Table 11–1:

$$X_2 = 0.56 \quad Y_2 = 1.63.$$

## 11–8 Selection of Ball and Cylindrical Roller Bearings

Ex- The second shaft on a parallel-shaft 25-hp foundry crane speed reducer contains a helical gear with a pitch diameter of 8.08 in.

Helical gears transmit components of force in the tangential, radial, and axial directions. The components of the gear force transmitted to the second shaft are shown in the Figure below at point *A*.

The bearing reactions at *C* and *D*, assuming simple-supports, are also shown. A ball bearing is to be selected for location *C* to accept the thrust, and a cylindrical roller bearing is to be utilized at location *D*.

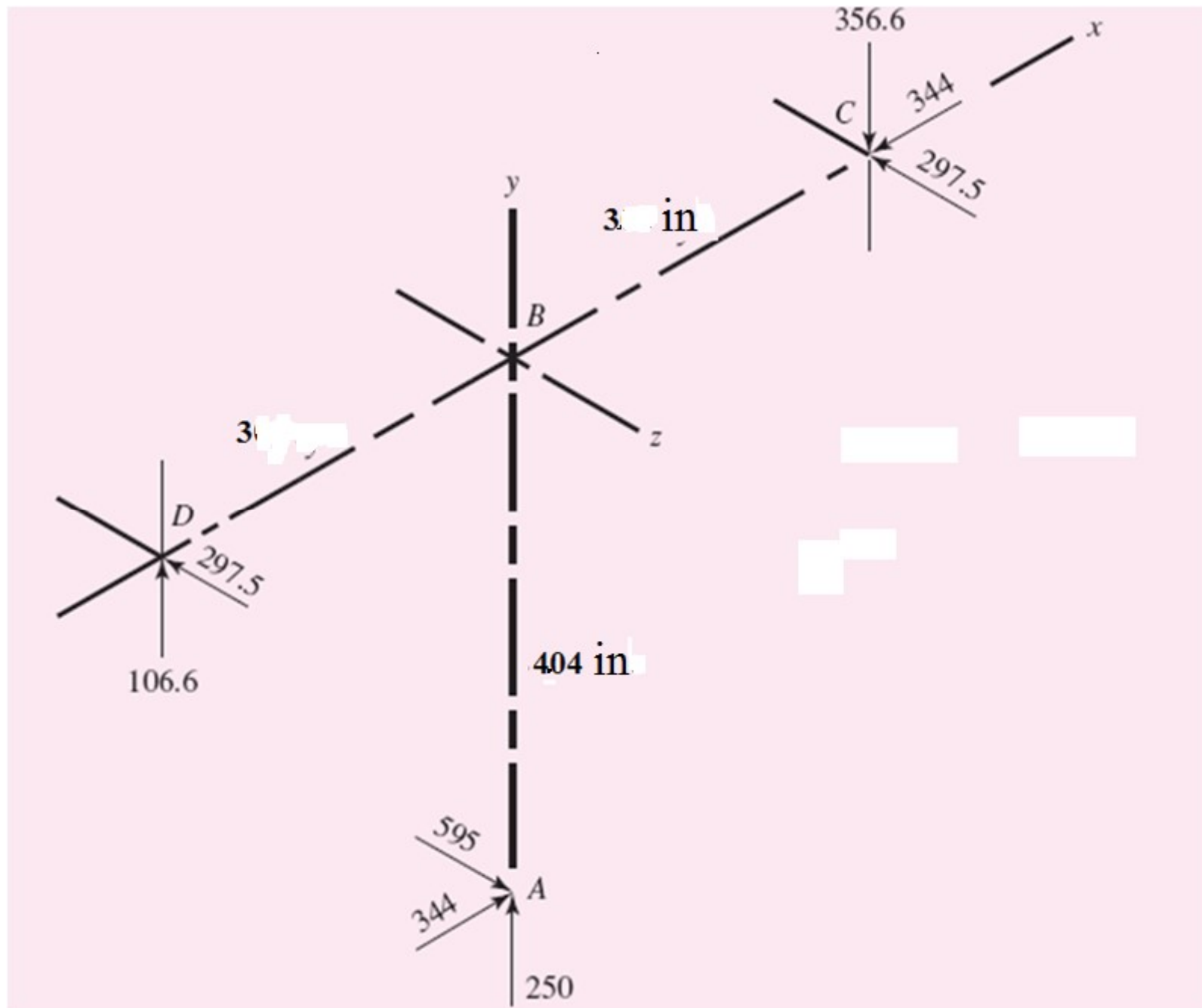
The life goal of the speed reducer is 10 kh, with a reliability factor for the assembly of all four bearings (both shafts) to equal or exceed

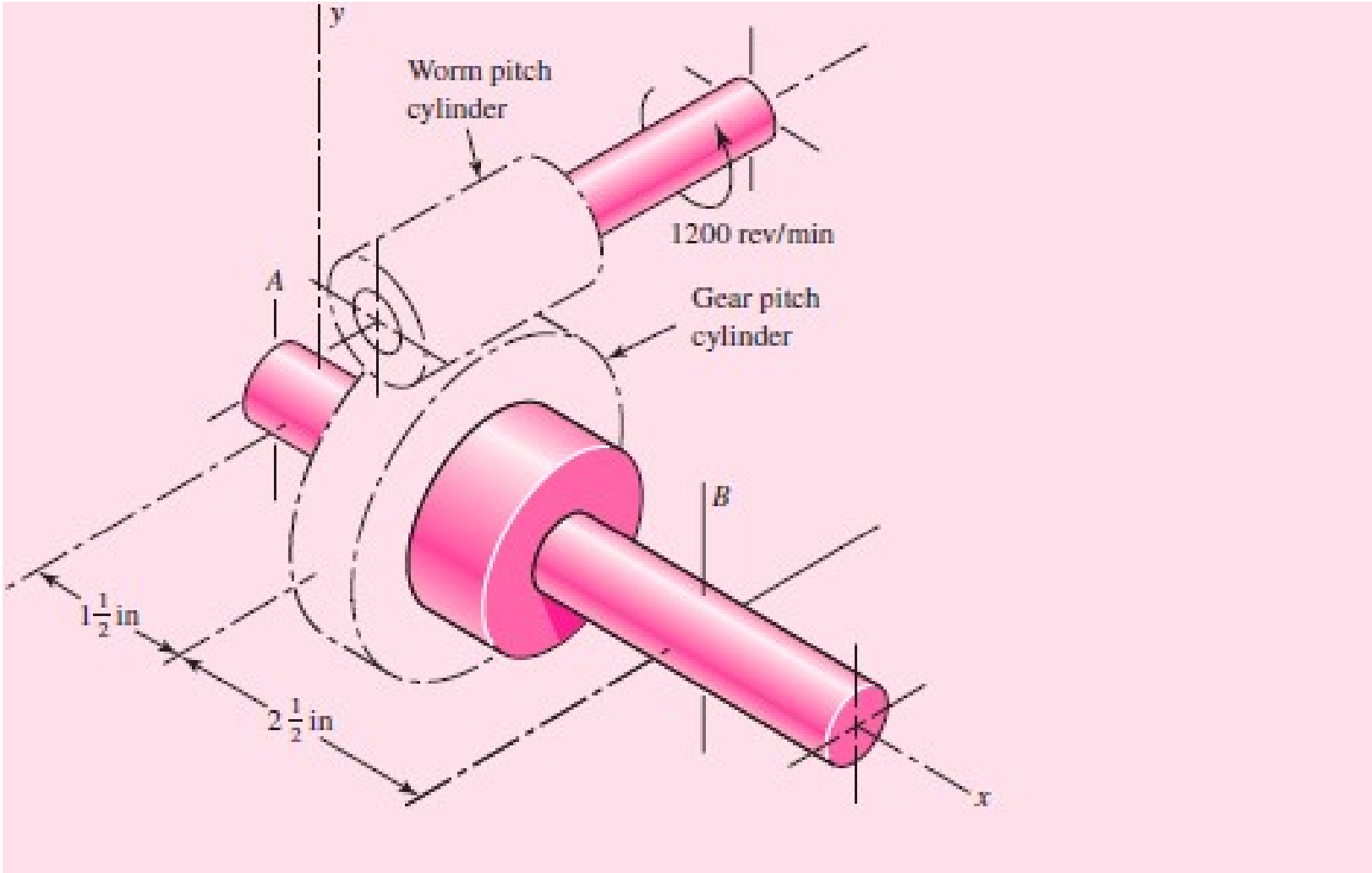
0.96 for the Weibull parameters are  $b=1.483$ ,  $X_0=0.2$ ,

$\theta=4.439+0.2$ . The application factor is to be 1.2.

(a) Select the roller bearing for location *D*.

(b) Select the ball bearing (angular contact) for location *C*, assuming the inner ring rotates.





The torque transmitted is  $T = 595(4.04) = 2404 \text{ lbf.in}$

The speed at the rated horse power,

$$n_D = \frac{63\,025 H}{T} = \frac{63\,025(25)}{2404} = 655.4 \text{ rev/min}$$

-The radial load at  $D$  is  $\sqrt{106.6^2 + 297.5^2} = 316.0 \text{ lbf}$ ,  
-the radial load at  $C$  is

$$\sqrt{356.6^2 + 297.5^2} = 464.4 \text{ lbf}$$

The individual bearing reliabilities, if equal, must be

$$2 \text{ bearing for each shaft so at least } \sqrt[4]{0.96} = 0.98985 \approx 0.99$$

The dimensionless design life for both bearings is

$$x_D = \frac{L}{L_{10}} = \frac{60L_D n_D}{60L_R n_R} = \frac{60(10\,000)655.4}{10^6} = 393.2$$



*a = 10/3 for the roller bearing at D, the catalog rating should be equal to or Greater than*

$$C_{10} = a_f F_D \left[ \frac{x_D}{x_0 + (\theta - x_0)(1 - R_D)^{1/b}} \right]^{1/a}$$
$$= 1.2(316.0) \left[ \frac{393.2}{0.02 + 4.439(1 - 0.99)^{1/1.483}} \right]^{3/10} = 3591 \text{ lbf} = 16.0 \text{ kN}$$

Choose a 02-25 mm series, or a 03-25 mm series cylindrical roller bearing from Table 11-3.

| <b>02-Series</b>    |                   |                      |                        |                      | <b>03-Series</b>  |                      |                        |                      |
|---------------------|-------------------|----------------------|------------------------|----------------------|-------------------|----------------------|------------------------|----------------------|
| <b>Bore,<br/>mm</b> | <b>OD,<br/>mm</b> | <b>Width,<br/>mm</b> | <b>Load Rating, kN</b> |                      | <b>OD,<br/>mm</b> | <b>Width,<br/>mm</b> | <b>Load Rating, kN</b> |                      |
|                     |                   |                      | <b>C<sub>10</sub></b>  | <b>C<sub>0</sub></b> |                   |                      | <b>C<sub>10</sub></b>  | <b>C<sub>0</sub></b> |
| 25                  | 52                | 15                   | 16.8                   | 8.8                  | 62                | 17                   | 28.6                   | 15.0                 |
| 30                  | 62                | 16                   | 22.4                   | 12.0                 | 72                | 19                   | 36.9                   | 20.0                 |
| 35                  | 72                | 17                   | 31.9                   | 17.6                 | 80                | 21                   | 44.6                   | 27.1                 |
| 40                  | 80                | 18                   | 41.8                   | 24.0                 | 90                | 23                   | 56.1                   | 32.5                 |
| 45                  | 85                | 19                   | 44.0                   | 25.5                 | 100               | 25                   | 72.1                   | 45.4                 |
| 50                  | 90                | 20                   | 45.7                   | 27.5                 | 110               | 27                   | 88.0                   | 52.0                 |
| 55                  | 100               | 21                   | 56.1                   | 34.0                 | 120               | 29                   | 102                    | 67.2                 |
| 60                  | 110               | 22                   | 64.4                   | 43.1                 | 130               | 31                   | 123                    | 76.5                 |
| 65                  | 120               | 23                   | 76.5                   | 51.2                 | 140               | 33                   | 138                    | 85.0                 |
| 70                  | 125               | 24                   | 79.2                   | 51.2                 | 150               | 35                   | 151                    | 102                  |
| 75                  | 130               | 25                   | 93.1                   | 63.2                 | 160               | 37                   | 183                    | 125                  |
| 80                  | 140               | 26                   | 106                    | 69.4                 | 170               | 39                   | 190                    | 125                  |
| 85                  | 150               | 28                   | 119                    | 78.3                 | 180               | 41                   | 212                    | 149                  |
| 90                  | 160               | 30                   | 142                    | 100                  | 190               | 43                   | 242                    | 160                  |

The ball bearing at *C* involves a thrust component. This selection procedure requires an iterative procedure. Assuming  $F_a/(V F_r) > e$ ,

- 1 Choose  $Y_2$  from Table 11-1.
- 2 Find  $C_{10}$ .
- 3 Tentatively identify a suitable bearing from Table 11-2, note  $C_0$ .
- 4 Using  $F_a/C_0$  enter Table 11-1 to obtain a new value of  $Y_2$ .
- 5 Find  $C_{10}$ .
- 6 If the same bearing is obtained, stop.
- 7 If not, take next bearing and go to step 4.

take the middle entry from Table 11-1:

$$X_2 = 0.56 \quad Y_2 = 1.63.$$

with  $V = 1$ ,

$$\frac{F_e}{V F_r} = X + \frac{Y F_a}{V F_r} = 0.56 + 1.63 \frac{344}{(1)464.4} = 1.77$$

$$F_e = 1.77 V F_r = 1.77(1)464.4 = 822 \text{ lbf} \quad \text{or} \quad 3.66 \text{ kN}$$

From Eq. (11-7), with  $a = 3$ ,

$$C_{10} = 1.2(3.66) \left[ \frac{393.2}{0.02 + 4.439(1 - 0.99)^{1/1.483}} \right]^{1/3} = 53.4 \text{ kN}$$

From Table 11-2, angular-contact bearing 02-60 mm has  $C_{10} = 55.9$  kN.  $C_0$  is 35.5 kN. Step 4 becomes, with  $F_a$  in kN,

$$\frac{F_a}{C_0} = \frac{344(4.45)10^{-3}}{35.5} = 0.0431$$

which makes  $e$  from Table 11-1 approximately 0.24. Now  $F_a/[VF_r] = 344/[(1)464.4] = 0.74$ , which is greater than 0.24, so we find  $Y_2$  by interpolation:

| $F_a/C_0$ | $Y_2$                         |
|-----------|-------------------------------|
| 0.042     | 1.85                          |
| 0.043     | $Y_2$ from which $Y_2 = 1.84$ |
| 0.056     | 1.71                          |

**Table 11-2**

Dimensions and Load Ratings for Single-Row 02-Series Deep-Groove and Angular-Contact Ball Bearings

| Bore,<br>mm | OD,<br>mm | Width,<br>mm | Fillet<br>Radius,<br>mm | Shoulder              |       | Load Ratings, kN |       |                 |       |
|-------------|-----------|--------------|-------------------------|-----------------------|-------|------------------|-------|-----------------|-------|
|             |           |              |                         | Diameter, mm<br>$d_S$ | $d_H$ | Deep Groove      |       | Angular Contact |       |
|             |           |              |                         |                       |       | $C_{10}$         | $C_0$ | $C_{10}$        | $C_0$ |
| 10          | 30        | 9            | 0.6                     | 12.5                  | 27    | 5.07             | 2.24  | 4.94            | 2.12  |
| 12          | 32        | 10           | 0.6                     | 14.5                  | 28    | 6.89             | 3.10  | 7.02            | 3.05  |
| 15          | 35        | 11           | 0.6                     | 17.5                  | 31    | 7.80             | 3.55  | 8.06            | 3.65  |
| 17          | 40        | 12           | 0.6                     | 19.5                  | 34    | 9.56             | 4.50  | 9.95            | 4.75  |
| 20          | 47        | 14           | 1.0                     | 25                    | 41    | 12.7             | 6.20  | 13.3            | 6.55  |
| 25          | 52        | 15           | 1.0                     | 30                    | 47    | 14.0             | 6.95  | 14.8            | 7.65  |
| 30          | 62        | 16           | 1.0                     | 35                    | 55    | 19.5             | 10.0  | 20.3            | 11.0  |
| 35          | 72        | 17           | 1.0                     | 41                    | 65    | 25.5             | 13.7  | 27.0            | 15.0  |
| 40          | 80        | 18           | 1.0                     | 46                    | 72    | 30.7             | 16.6  | 31.9            | 18.6  |
| 45          | 85        | 19           | 1.0                     | 52                    | 77    | 33.2             | 18.6  | 35.8            | 21.2  |
| 50          | 90        | 20           | 1.0                     | 56                    | 82    | 35.1             | 19.6  | 37.7            | 22.8  |
| 55          | 100       | 21           | 1.5                     | 63                    | 90    | 43.6             | 25.0  | 46.2            | 28.5  |
| 60          | 110       | 22           | 1.5                     | 70                    | 99    | 47.5             | 28.0  | 55.9            | 35.5  |
| 65          | 120       | 23           | 1.5                     | 74                    | 109   | 55.9             | 34.0  | 63.7            | 41.5  |
| 70          | 125       | 24           | 1.5                     | 79                    | 114   | 61.8             | 37.5  | 68.9            | 45.5  |
| 75          | 130       | 25           | 1.5                     | 86                    | 119   | 66.3             | 40.5  | 71.5            | 49.0  |
| 80          | 140       | 26           | 2.0                     | 93                    | 127   | 70.2             | 45.0  | 80.6            | 55.0  |
| 85          | 150       | 28           | 2.0                     | 99                    | 136   | 83.2             | 53.0  | 90.4            | 63.0  |
| 90          | 160       | 30           | 2.0                     | 104                   | 146   | 95.6             | 62.0  | 106             | 73.5  |
| 95          | 170       | 32           | 2.0                     | 110                   | 156   | 108              | 69.5  | 121             | 85.0  |

| $F_a/C_0$ | $e$  | $F_a/(VF_r) \leq e$ |       | $F_a/(VF_r) > e$ |       |
|-----------|------|---------------------|-------|------------------|-------|
|           |      | $X_1$               | $Y_1$ | $X_2$            | $Y_2$ |
| 0.014*    | 0.19 | 1.00                | 0     | 0.56             | 2.30  |
| 0.021     | 0.21 | 1.00                | 0     | 0.56             | 2.15  |
| 0.028     | 0.22 | 1.00                | 0     | 0.56             | 1.99  |
| 0.042     | 0.24 | 1.00                | 0     | 0.56             | 1.85  |
| 0.056     | 0.26 | 1.00                | 0     | 0.56             | 1.71  |
| 0.070     | 0.27 | 1.00                | 0     | 0.56             | 1.63  |
| 0.084     | 0.28 | 1.00                | 0     | 0.56             | 1.55  |
| 0.110     | 0.30 | 1.00                | 0     | 0.56             | 1.45  |
| 0.17      | 0.34 | 1.00                | 0     | 0.56             | 1.31  |
| 0.28      | 0.38 | 1.00                | 0     | 0.56             | 1.15  |
| 0.42      | 0.42 | 1.00                | 0     | 0.56             | 1.04  |
| 0.56      | 0.44 | 1.00                | 0     | 0.56             | 1.00  |

\*Use 0.014 if  $F_a/C_0 < 0.014$ .

From Eq. (11-8*b*),

$$\frac{F_e}{VF_r} = 0.56 + 1.84 \frac{344}{464.4} = 1.92$$

$$F_e = 1.92 VF_r = 1.92(1)464.4 = 892 \text{ lbf} \quad \text{or} \quad 3.97 \text{ kN}$$

The prior calculation for  $C_{10}$  changes only in  $F_e$ , so

$$C_{10} = \frac{3.97}{3.66} 53.4 = 57.9 \text{ kN}$$

From Table 11-2 an angular contact bearing 02-65 mm has  $C_{10} = 63.7$  kN and  $C_0$  of 41.5 kN. Again,

$$\frac{F_a}{C_0} = \frac{344(4.45)10^{-3}}{41.5} = 0.0369$$

making  $e$  approximately 0.23. Now from before,  $F_a/VF_r = 0.74$ , which is greater than 0.23. We find  $Y_2$  again by interpolation:

| $F_a/C_0$ | $Y_2$                         |
|-----------|-------------------------------|
| 0.028     | 1.99                          |
| 0.0369    | $Y_2$ from which $Y_2 = 1.90$ |
| 0.042     | 1.85                          |

From Eq. (11-8*b*),

$$\frac{F_e}{VF_r} = 0.56 + 1.90 \frac{344}{464.4} = 1.967$$

$$F_e = 1.967 VF_r = 1.967(1)464.4 = 913.5 \text{ lbf} \quad \text{or} \quad 4.065 \text{ kN}$$

The prior calculation for  $C_{10}$  changes only in  $F_e$ , so

$$C_{10} = \frac{4.07}{3.66} 53.4 = 59.4 \text{ kN}$$

**Answer** From Table 11–2 an angular-contact 02-65 mm is still selected, so the iteration is complete.

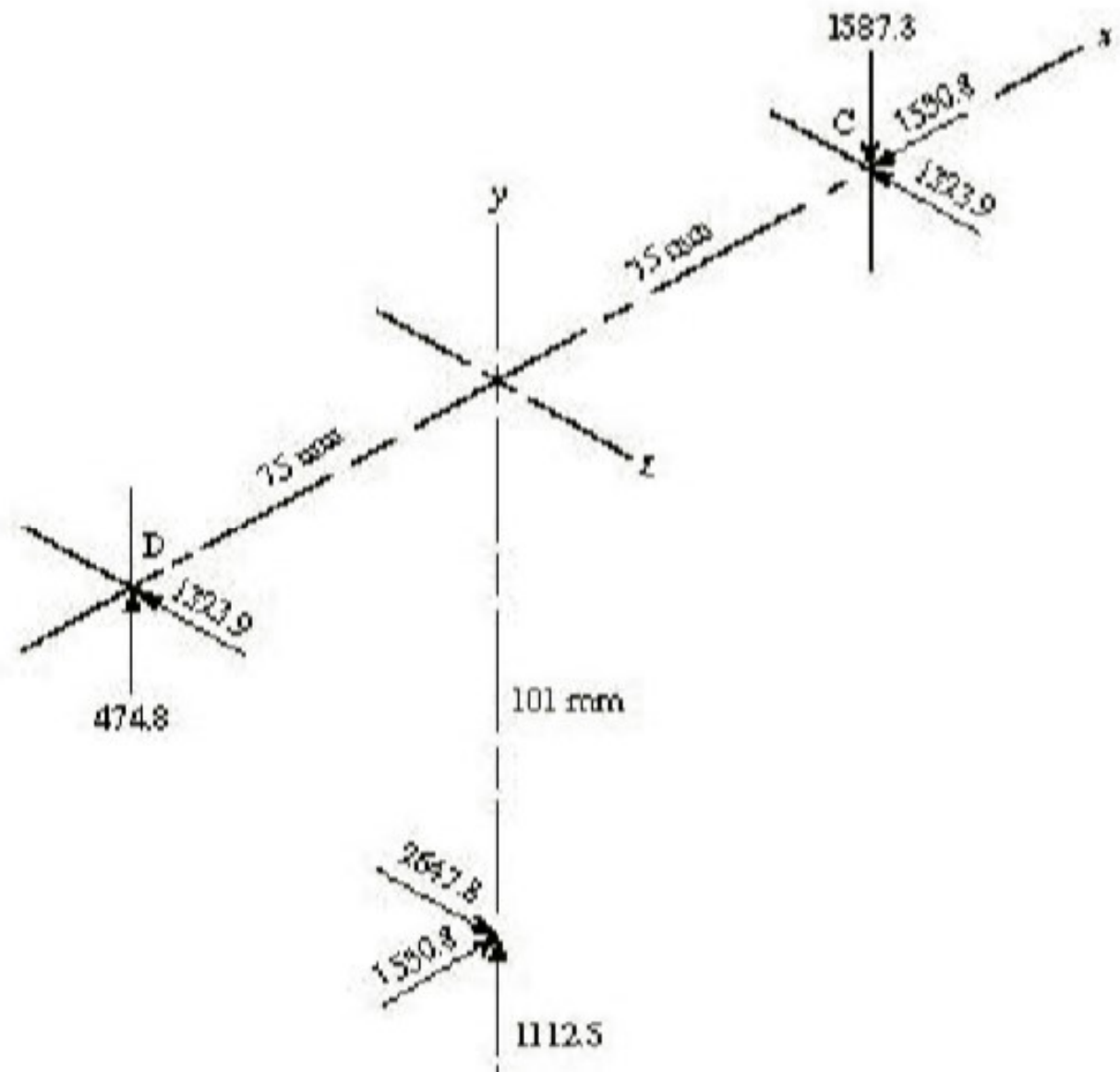


Ex

The second shaft on a parallel-shaft 18.5kW foundry crane speed reducer has bearing reaction as shown in Fig . A ball bearing is to be selected for location C to accept the thrust, and a cylindrical roller bearing is to be utilized at location D. The life goal equal or exceed 0.96. The application factor is to be 1.2

- Select the roller bearing for location D
- Select the ball bearing (angular contact) for location C.

□ The life goal of the speed reducer is 10kh. The desired speed is 656 rev/min.



The radial load at D is  $\sqrt{474.8^2 + 1323.9^2} = 1406.5N$

The radial load at C is  $\sqrt{1587.3^2 + 1323.9^2} = 2066.9N$

At D desired life is

$$x_D = \frac{L}{L_{10}} = \frac{60L_D n_D}{60L_R n_R} = \frac{60(10000)656}{10^6} = 393.6$$

$$C_{10} = 1.2(1406.5) \left[ \frac{393.6}{0.02 + 4.439(1 - 0.99)^{1/1.483}} \right]^{3/10} = 15986N = 16kN$$

Choose a 02-25 mm series, or a 03-25mm series cylindrical roller bearing from Table 11-3

From Table 11-1, we find  $X_2=0.056$   $Y_2=1.63$ , from

$$\text{Eq. (11-7), } \frac{F_e}{VFr} = 0.56 + 1.63 \frac{1530.8}{(1)2066.9} = 1.77$$

$$F_e = 1.77 Vfr = 1.77 (1)2066.9 = 3.658 \text{ kN}$$

From Eq. (11-6),

$$C_{10} = 1.2(3.658) \left[ \frac{393.6}{0.02 + 4.439(1 - 0.99)^{1/483}} \right]^{1/3} = 53.37 \text{ kN}$$

From Table 11-2, angular-contact bearing 02-60mm has

$$C'_{10}=55.9\text{kN}. C_{10}=35.5\text{kN}$$

$$\frac{F_a}{[VF_r]} = \frac{1530.8}{[(1)2066.9]} = 0.74$$

$e=0.24$  from Table 11-1.

$$\frac{F_a}{C_o} = \frac{1530.810^{-3}}{35.5} = 0.043$$

| $F_a/C_o$ | $Y_2$ |
|-----------|-------|
| 0.042     | 1.85  |
| 0.043     | $Y_2$ |
| 0.056     | 1.71  |

$$\frac{0.043 - 0.042}{0.056 - 0.042} = \frac{Y_2 - 1.85}{1.71 - 1.85}$$

$$Y_2 = 1.84$$

$$\frac{Fe}{VFr} = 0.56 + 1.84 \frac{1530.8}{2066.9} = 1.922$$

$$Fe = 1.922 VFr = 1.922 (1)2066.9 = 3.972 \text{ kN}$$

$$C_{10} = \frac{3.972}{3.658} 53.37 = 57.95 \text{ kN}$$

From Table 11-2 an angular contact bearing 02-65 mm has

$$C'_{10} = 63.7 \text{ kN and } C'_0 = 41.5 \text{ kN} \quad \frac{F_a}{C_0} = \frac{1530.8 \cdot 10^{-3}}{41.5} = 0.0369$$

e approximately 0.23, now 
$$\frac{F_a}{(VF_r)} = \frac{1530.8}{[1(2066.9)]} = 0.74$$

$$\frac{0.039 - 0.028}{0.042 - 0.028} = \frac{Y_2 - 1.99}{1.85 - 1.99}$$

Which is greater than 0.23. We find  $Y_2$ ;

$$Y_2 = 1.90$$

$$\frac{Fe}{VFr} = 0.56 + 1.90 \frac{1530.8}{2066.9} = 1.967$$

$$Fe = 1.967 VFr = 1.967(1)2066.9 = 4.066 \text{ kN}$$

$$C_{10} = \frac{4.066}{3.658} 53.37 = 59.32 \text{ kN}$$

---

From Table 11-2 an angular contact 02-65mm is still selected, so iteration is complete.