

Quiz1

Industrial control

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Name: saleem bouri

ID:

Find the inverse laplace transform for $Y(s) = \frac{1}{s(s^2+1)}$

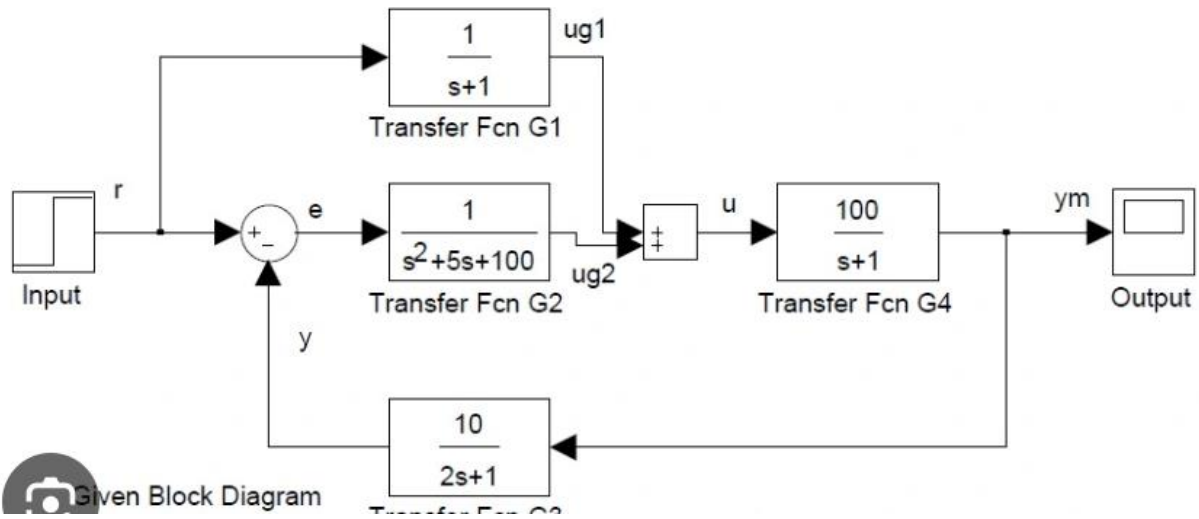
Solution

1-cos(t)

Name:

ID:

Find the equivalent transfer function for



Solution

$$1 + \frac{\frac{100}{(s^2 + 5s + 100)(s + 1)} + \frac{100}{(s + 1)^2}}{\frac{1000}{(s^2 + 5s + 100)(s + 1)(2s + 1)}}$$

NAME:

ID:

For the following system find the rise time, settling time and percent overshoot

$$\frac{C}{R} = \frac{s + 3}{s^2 + s + 4.25}$$

Tr=0.91second

Ts=8 second

Mp=45.58

NAME:

ID:

For the following system find the rise time, settling time and percent overshoot

$$\frac{c}{R} = \frac{s + 3}{s^2 + 4s + 13}$$

Tr=0.71

Ts=2 second

Mp=12.64

NAME:

ID:

For the following system find the rise time, settling time and percent overshoot

$$\frac{C}{R} = \frac{s + 3}{s^2 + 9s + 18}$$

Tr=0.3666

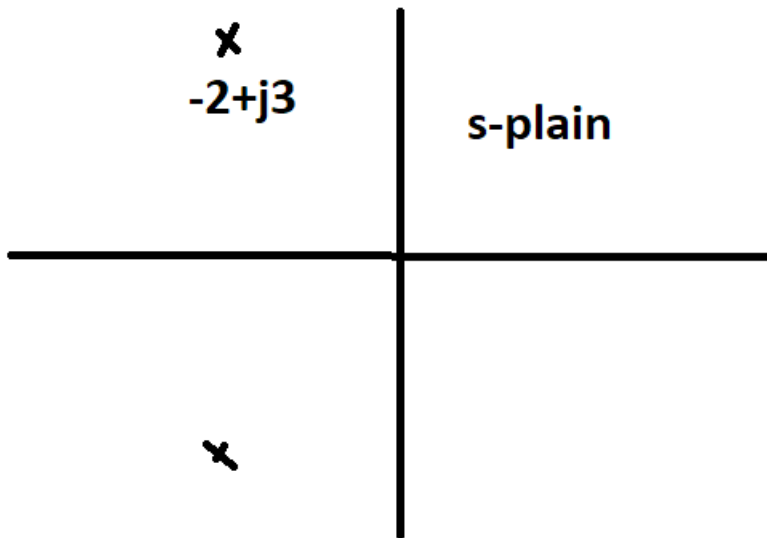
Ts=0.6666

Mp=0

NAME:

ID:

For the following system with roots shown in the following s-plane find the rise time, settling time and percent overshoot



$T_r=0.719$

$T_s=2$

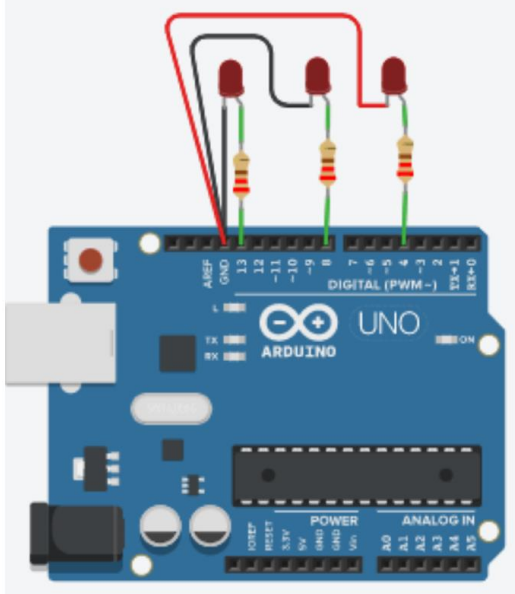
$M_p=12.3$

Name:

ID:

Write the code for the following Arduino such that we have the following lighting sequence (5 points)

| Sequence step | 1 | 2 | 3 | 4 |
|---------------|-------|-------|-------|-----|
| LED1 | off | Light | Off | Off |
| LED2 | light | off | Light | Off |
| LED3 | light | off | Light | off |



```
Const int LED1=13;
```

```
Const int LED2=8;
```

```
Const int LED3=4;
```

```
Void setup(){
```

```
pinMode(LED1,OUTPUT);
```

```
PinMode(LED2,OUTPUT);
```

```
pinMode(LED3,OUTPUT);
```

```
}
```

```
Void loop(){ digitalWrite(LED1,LOW); digitalWrite(LED2,HIGH); digitalWrite(LED3,HIGH); delay(1000);
```

```
digitalWrite(LED1,HIGH); digitalWrite(LED2,LOW); digitalWrite(LED3,LOW);delay(1000);
```

```
digitalWrite(LED1,LOW); digitalWrite(LED2,HIGH); digitalWrite(LED3,HIGH); delay(1000);
```

```
digitalWrite(LED1,LOW); digitalWrite(LED2,LOW); digitalWrite(LED3,LOW); delay(1000);}
```

Name:

ID:

write MATLAB code using ODE45 to solve the following differential equations

$$\ddot{x} + x = \log(t), \quad \dot{x}(0) = 0, \quad x(0) = 0$$

Plot(y) and plot(x) on same figure for a time interval 0 to 20 seconds.

```
Function dx=diff(t,x);
```

```
[m n]=size(x);
```

```
Dx=zeros(m,n);
```

```
Dx(1)=x(2);
```

```
Dx(2)=log10(t)-x(1);
```

```
Clear
```

```
Clc
```

```
Tspan=[0 20];
```

```
X0=[0;0];
```

```
[t,x]=ode45(@diff,tspan,x0);
```

```
Plot(x)
```


Name: _____

ID: _____

write MATLAB symbolic code to solve the following differential equations

$$\ddot{x}y + y = \log(t), \quad \ddot{y}x + \dot{y} = t, \quad \dot{x}(0) = 0, \dot{y}(0) = 0, x(0) = 0, y(0) = 0$$

```
Syms x(t) y(t)
```

```
Eqn=[diff(x,t,2)==(log10(t)-y)/y, diff(y,t,2)==(t-diff(y,t))/x];
```

```
Dx=diff(x,t);
```

```
Dy=diff(y,t);
```

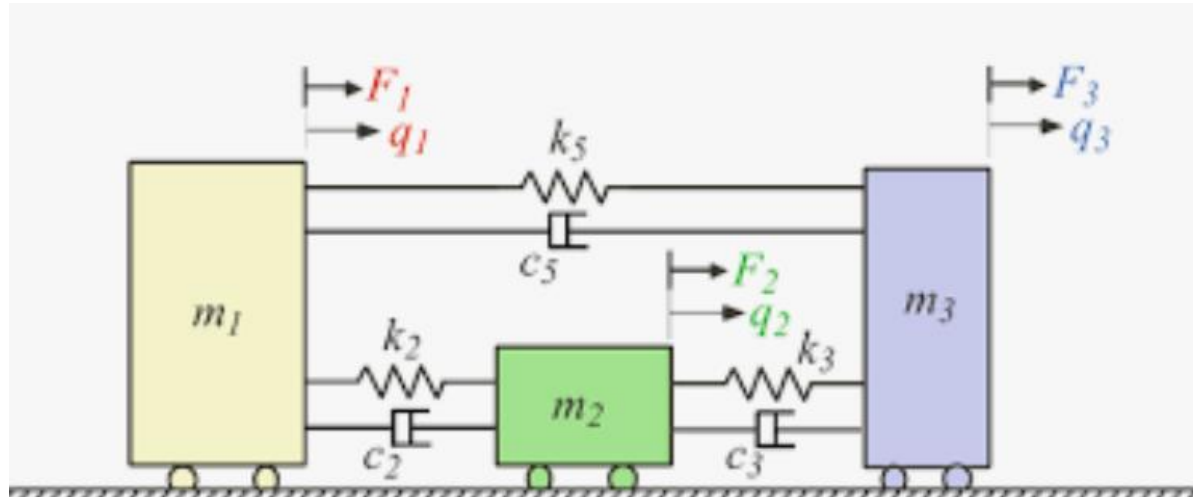
```
Cond=[x(0)==0,y(0)==0,dx(0)==0,dy(0)==0];
```

```
[x,y]=dsolve(Eqn,Cond)
```

Name:

ID:

Write the differential equations describing the following system



$$F_1 = m_1 q_1'' + k_2(q_1 - q_2) + c_2(q_1' - q_2') + k_5(q_1 - q_3) + c_5(q_1' - q_3')$$

$$F_2 = m_2 q_2'' + k_2(q_2 - q_1) + c_2(q_2' - q_1') + k_3(q_2 - q_3) + c_3(q_2' - q_3')$$

$$F_3 = m_3 q_3'' + k_3(q_3 - q_2) + c_3(q_3' - q_2') + k_5(q_3 - q_1) + c_5(q_3' - q_1')$$

Name

ID

Q1)a) Find the solution of the following differential equation using inverse laplace transform (4 points)

$$\ddot{X} + 3\dot{X} + 2X = t^2$$

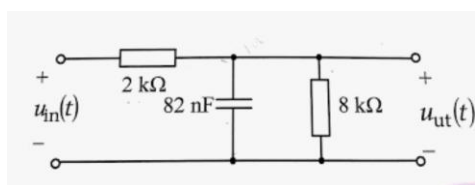
| | | | |
|---|---|---|---|
| 1. 1 | $\frac{1}{s}$ | 2. e^{at} | $\frac{1}{s-a}$ |
| 3. $t^n, n=1,2,3,\dots$ | $\frac{n!}{s^{n+1}}$ | 4. $t^p, p > -1$ | $\frac{\Gamma(p+1)}{s^{p+1}}$ |
| 5. \sqrt{t} | $\frac{\sqrt{\pi}}{2s^{3/2}}$ | 6. $t^{n-1/2}, n=1,2,3,\dots$ | $\frac{1 \cdot 3 \cdot 5 \cdots (2n-1)\sqrt{\pi}}{2^n s^{n+1/2}}$ |
| 7. $\sin(at)$ | $\frac{a}{s^2+a^2}$ | 8. $\cos(at)$ | $\frac{s}{s^2+a^2}$ |
| 9. $t \sin(at)$ | $\frac{2as}{(s^2+a^2)^2}$ | 10. $t \cos(at)$ | $\frac{s^2-a^2}{(s^2+a^2)^2}$ |
| 11. $\sin(at) - at \cos(at)$ | $\frac{2a^3}{(s^2+a^2)^2}$ | 12. $\sin(at) + at \cos(at)$ | $\frac{2as^2}{(s^2+a^2)^2}$ |
| 13. $\cos(at) - at \sin(at)$ | $\frac{s(s^2-a^2)}{(s^2+a^2)^2}$ | 14. $\cos(at) + at \sin(at)$ | $\frac{s(s^2+3a^2)}{(s^2+a^2)^2}$ |
| 15. $\sin(at+b)$ | $\frac{s \sin(b) + a \cos(b)}{s^2+a^2}$ | 16. $\cos(at+b)$ | $\frac{s \cos(b) - a \sin(b)}{s^2+a^2}$ |
| 17. $\sinh(at)$ | $\frac{a}{s^2-a^2}$ | 18. $\cosh(at)$ | $\frac{s}{s^2-a^2}$ |
| 19. $e^{at} \sin(bt)$ | $\frac{b}{(s-a)^2+b^2}$ | 20. $e^{at} \cos(bt)$ | $\frac{s-a}{(s-a)^2+b^2}$ |
| 21. $e^{at} \sinh(bt)$ | $\frac{b}{(s-a)^2-b^2}$ | 22. $e^{at} \cosh(bt)$ | $\frac{s-a}{(s-a)^2-b^2}$ |
| 23. $t^n e^{at}, n=1,2,3,\dots$ | $\frac{n!}{(s-a)^{n+1}}$ | 24. $f(ct)$ | $\frac{1}{c} F\left(\frac{s}{c}\right)$ |
| 25. $u_c(t) = u(t-c)$ Heaviside Function | $\frac{e^{-cs}}{s}$ | 26. $\delta(t-c)$ Dirac Delta Function | e^{-cs} |
| 27. $u_c(t) f(t-c)$ | $e^{-cs} F(s)$ | 28. $u_c(t) g(t)$ | $e^{-cs} \mathcal{L}\{g(t+c)\}$ |
| 29. $e^{at} f(t)$ | $F(s-c)$ | 30. $t^n f(t), n=1,2,3,\dots$ | $(-1)^n F^{(n)}(s)$ |
| 31. $\frac{1}{t} f(t)$ | $\int_s^\infty F(u) du$ | 32. $\int_0^t f(v) dv$ | $\frac{F(s)}{s}$ |
| 33. $\int_0^t f(t-\tau) g(\tau) d\tau$ | $F(s)G(s)$ | 34. $f(t+T) = f(t)$ | $\frac{\int_0^T e^{-st} f(t) dt}{1-e^{-sT}}$ |
| 35. $f'(t)$ | $sF(s) - f(0)$ | 36. $f''(t)$ | $s^2F(s) - sf'(0) - f''(0)$ |
| 37. $f^{(n)}(t)$ | $s^n F(s) - s^{n-1} f(0) - s^{n-2} f'(0) \cdots - sf^{(n-2)}(0) - f^{(n-1)}(0)$ | | |

$$\exp(-2*t)/4 - 2*\exp(-t) - (3*t)/2 + t^2/2 + 7/4$$

B) what is the final value for $y(s)$ in part $y(s) = \frac{1}{s^2 + 2s + 3}$ (2 points)

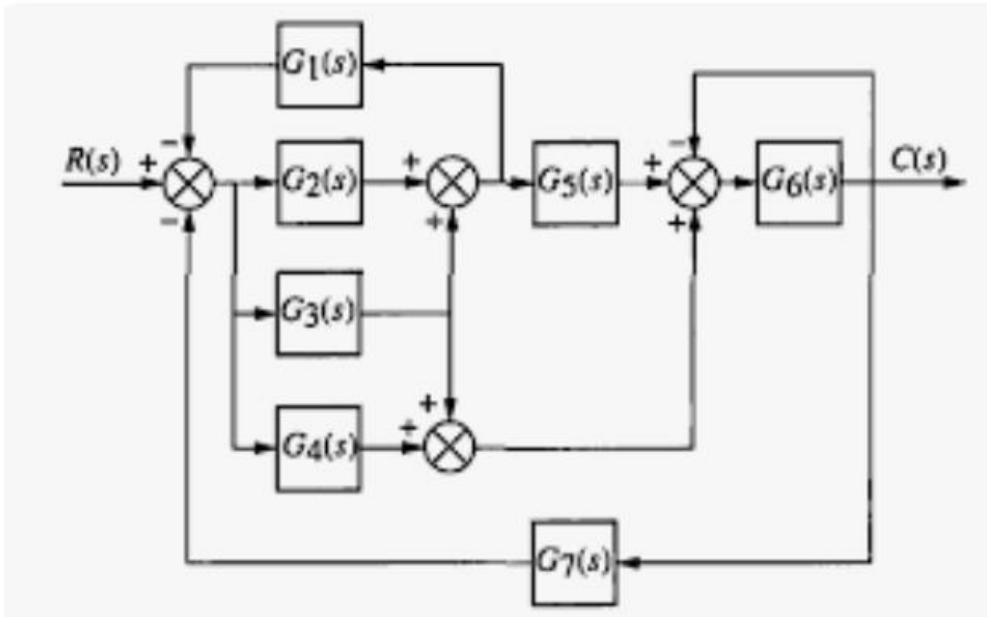
0

Q2) find the transfer function for the following a) U_{ut}/U_{in} (4 points)



$$= \frac{8000}{1.3s + 10000}$$

Q3) Find the equivalent transfer function for (5 points)

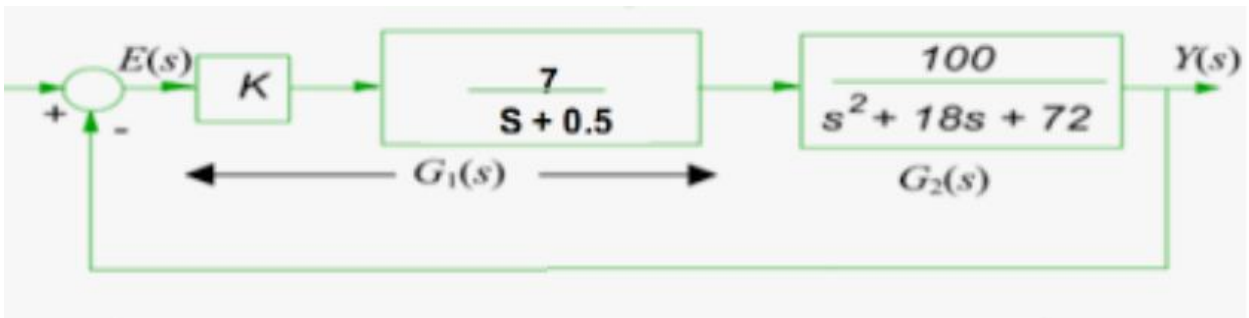


4 path

7 loop

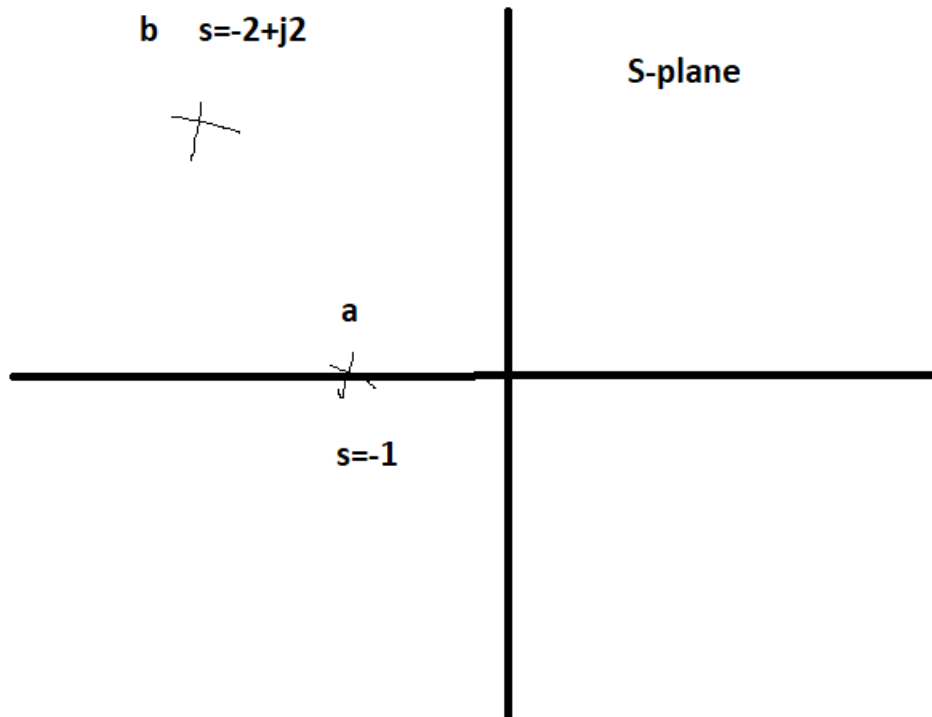
2 non touching

Q4) Find the steady state error for a step input (5 points)



0.05

Q5) a) For a and b poles in the following find the associated damping ratio and percent overshoot (5 points)



For a

Damping ratio = 1

$M_p = 0$

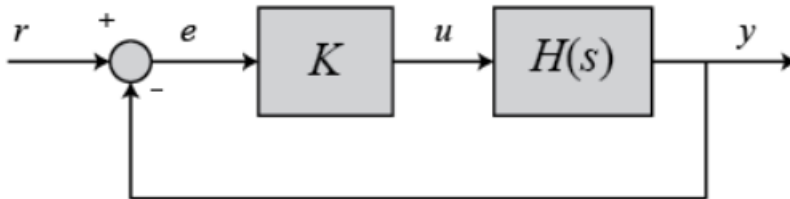
For b

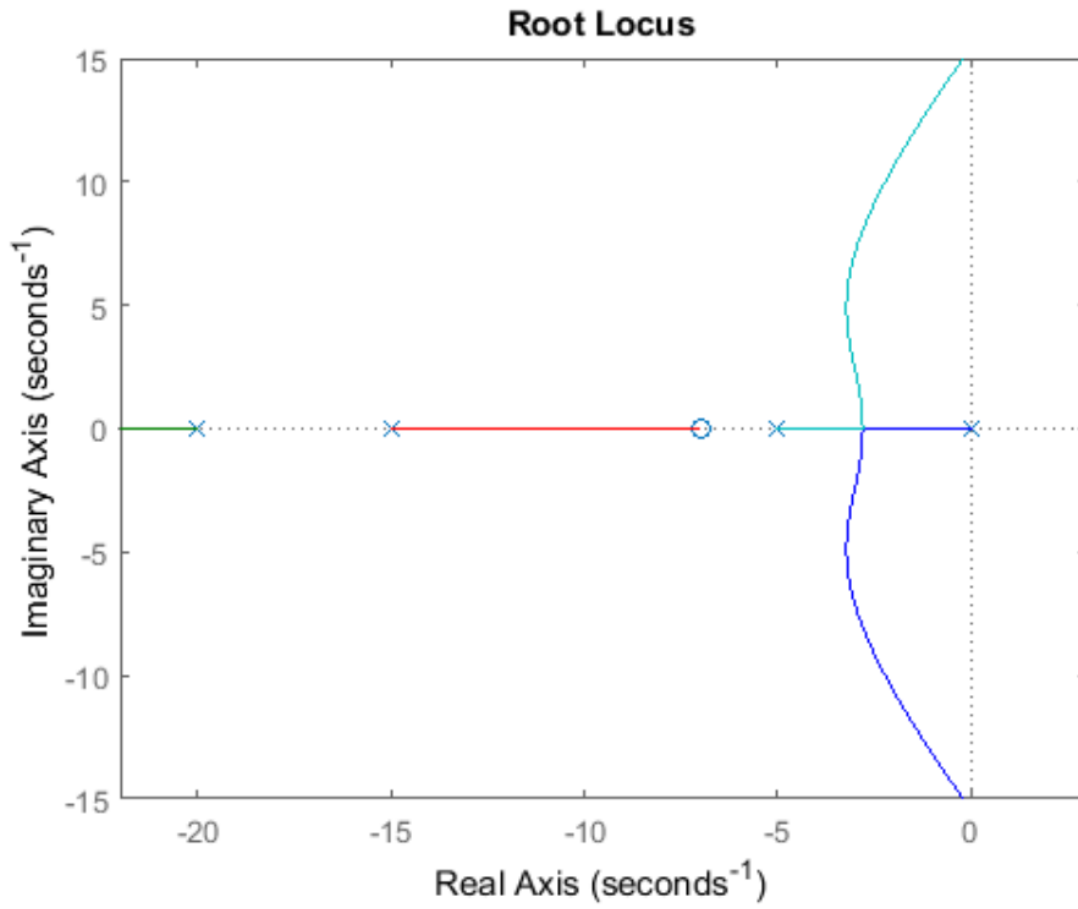
Damping ratio = 0.7071

$M_p = 4.33$

$$H(s) = \frac{Y(s)}{U(s)} = \frac{s + 7}{s(s + 5)(s + 15)(s + 20)}$$

Q6) What is the) a) For the following system design the feedback controller k to achieve a damping ratio of > 0.6 . (you must use the root locus figure below) (5 points)





$s = -3 + 5j$

$K = 1130$